

(Radio) Recombination lines (RRLs)

Divakara Mayya (INAOE)



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1. Why discuss atomic lines in a molecular astrophysics workshop?

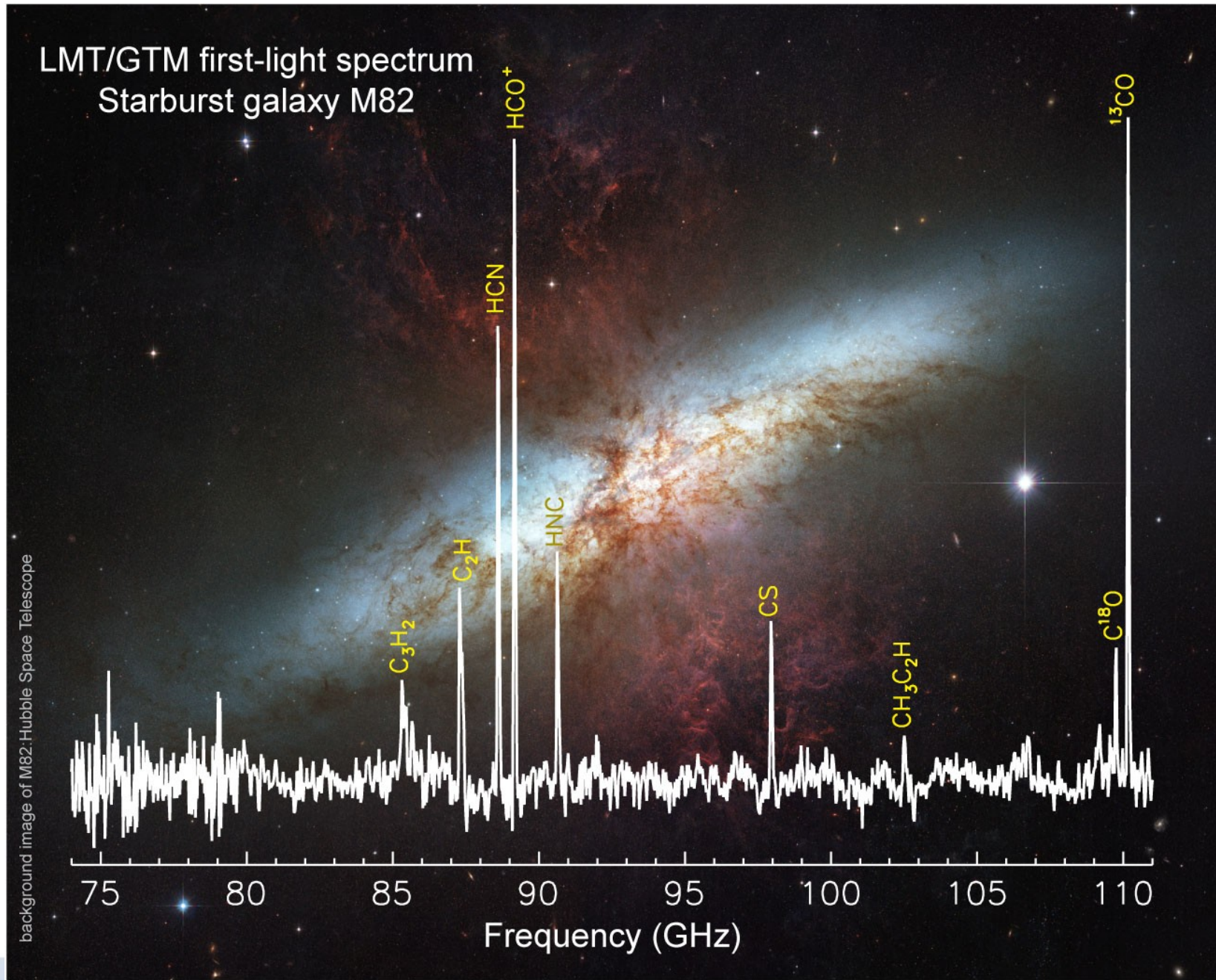
Molecular lines and RRLs are linked through:

- **Star formation**
 - MCs
 - HII regions

- **MM Observations**
 - molecular lines
 - MM RRLs

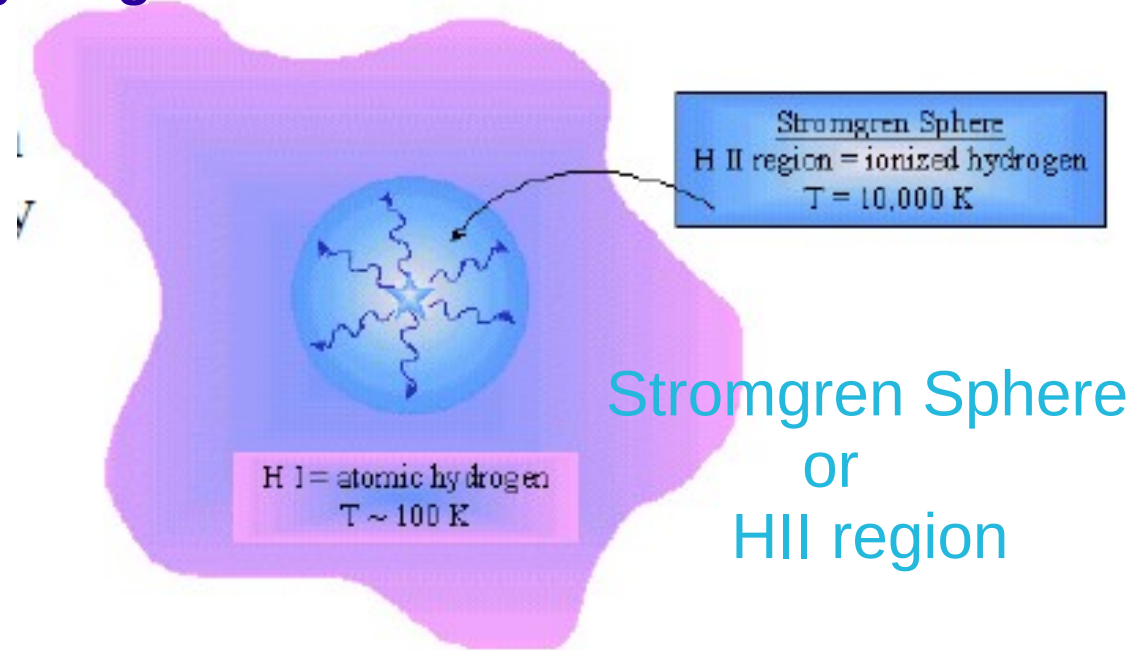
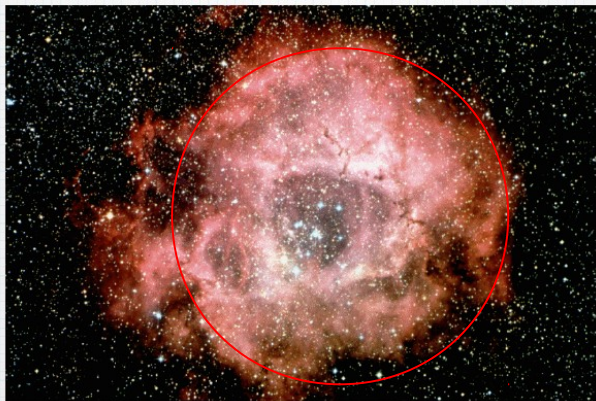


1.1 LMT/RSR spectrum of the starburst nucleus of M82



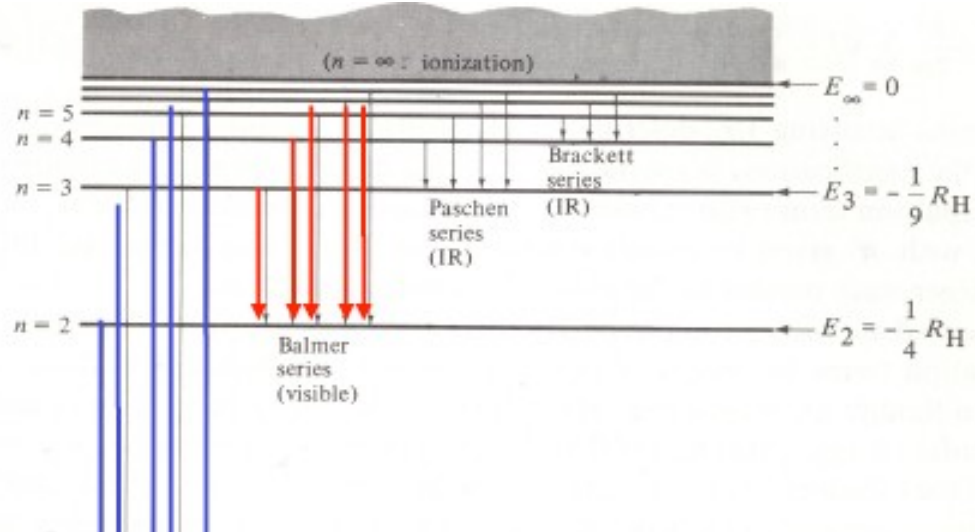
2. HII regions and recombination lines

Ionization of a Pure Hydrogen Cloud



$$\begin{aligned} \# \text{ of photoionizations/s} \\ = \\ \# \text{ of recombinations/s} \end{aligned}$$

2.1 Atomic Structure of a Hydrogen Atom

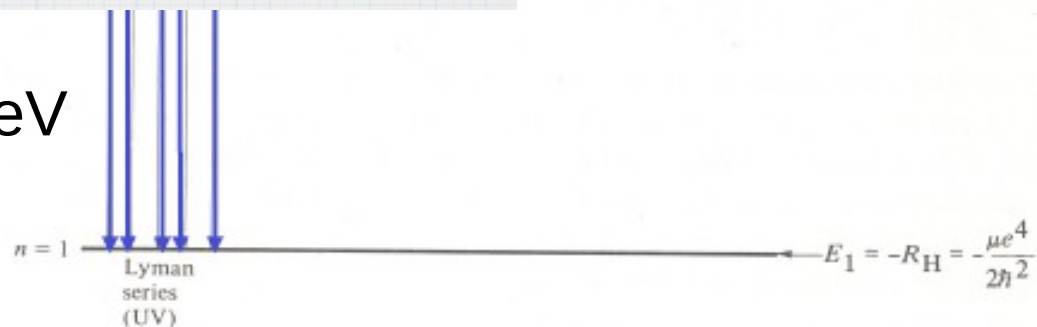


$$E = -\frac{\mu e^4}{2\hbar^2} \frac{1}{n^2} \equiv -hcR_H \frac{1}{n^2}$$

H spectrum

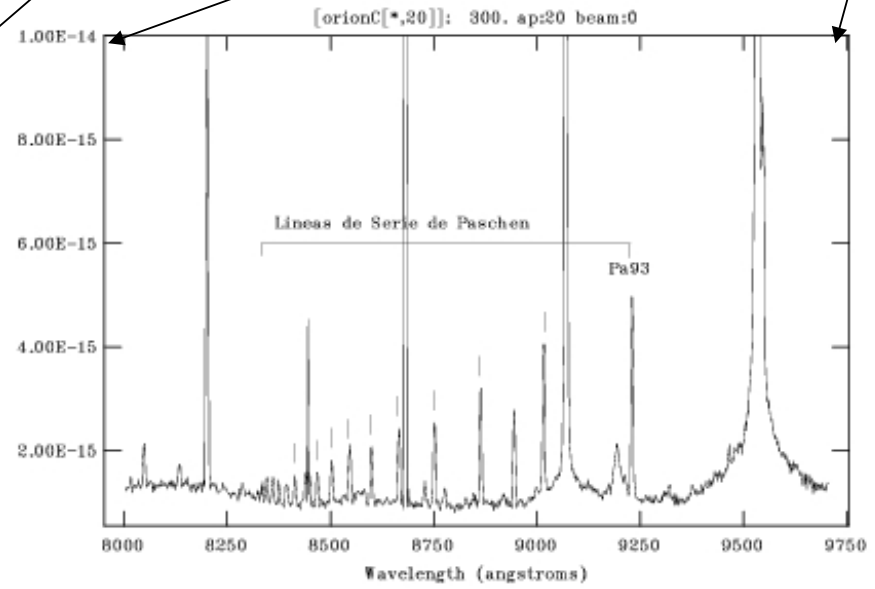
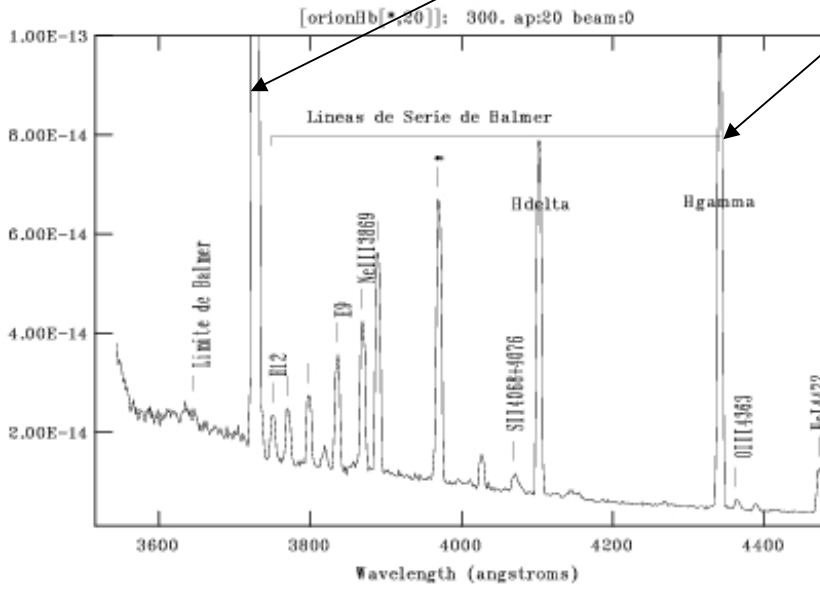
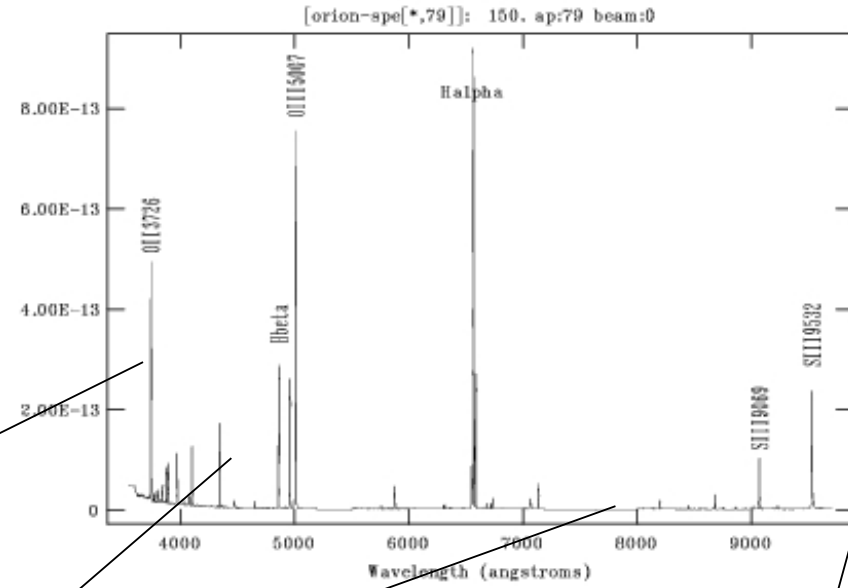
with $R_H = 109,677.585 \text{ cm}^{-1}$: Rydberg constant for H

E (ionization) = 13.6 eV

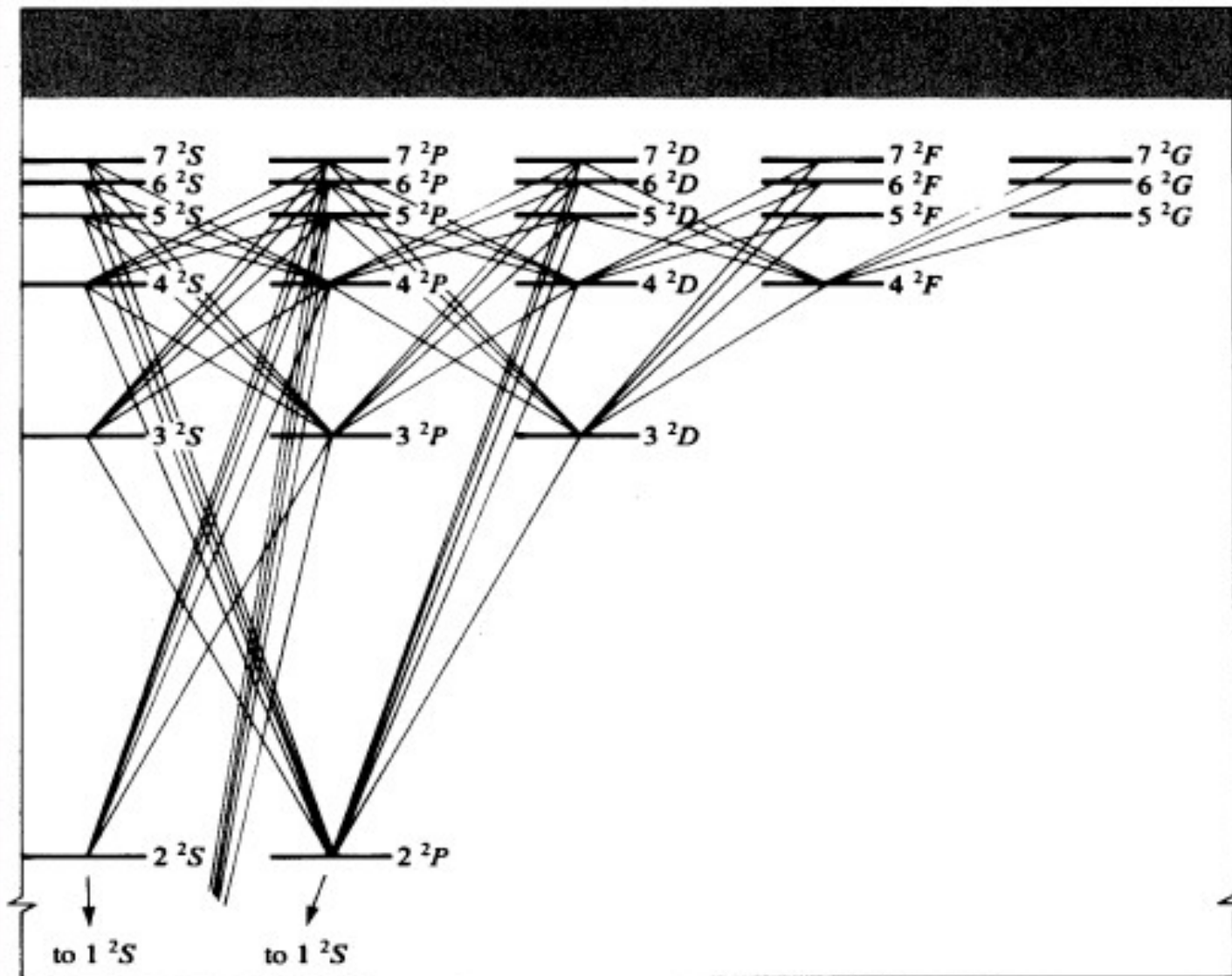


Wavelengths of important H Lines

- * Ly α : $\lambda_{vac} = 1215.68 \text{ \AA}$ (space UV)
 - * H α : $\lambda_{air} = 6562.73 \text{ \AA}$ (red) 3-2
 - * H β : $\lambda_{air} = 4861.33 \text{ \AA}$ (blue) 4-2
 - * H γ : $\lambda_{air} = 4340.47 \text{ \AA}$ (blue) 5-2
 - * H δ : $\lambda_{air} = 4101.47 \text{ \AA}$ (violet) 6-2
- } Balmer
- * Pa α : $\lambda_{air} = 1.875 \mu\text{m}$ (poor transmission)
 - * Br α : $\lambda_{air} = 4.051 \mu\text{m}$ (difficult)
 - * Br γ : $\lambda_{air} = 2.166 \mu\text{m}$ (in infrared K band)



H spectrum: permitted transitions



3. Transitions between higher quantum levels: Calculated frequencies

The H spectrum

Bohr 1913

$$\begin{aligned}1/\lambda &= R_H(1 - 1/n^2) & n = 2, 3, 4, \dots & \text{Lyman series} \\1/\lambda &= R_H(1/2^2 - 1/n^2) & n = 3, 4, 5, \dots & \text{Balmer series} \\1/\lambda &= R_H(1/3^2 - 1/n^2) & n = 4, 5, 6, \dots & \text{Paschen series} \\1/\lambda &= R_H(1/4^2 - 1/n^2) & n = 5, 6, 7, \dots & \text{Brackett series} \\1/\lambda &= R_H(1/5^2 - 1/n^2) & n = 6, 7, 8, \dots & \text{Pfund series}\end{aligned}$$

Brackett α line (**H4 α**) at 4.05 μm (Brackett 1922)

Pfund α line (**H5 α**) at 7.46 μm (Pfund 1924)

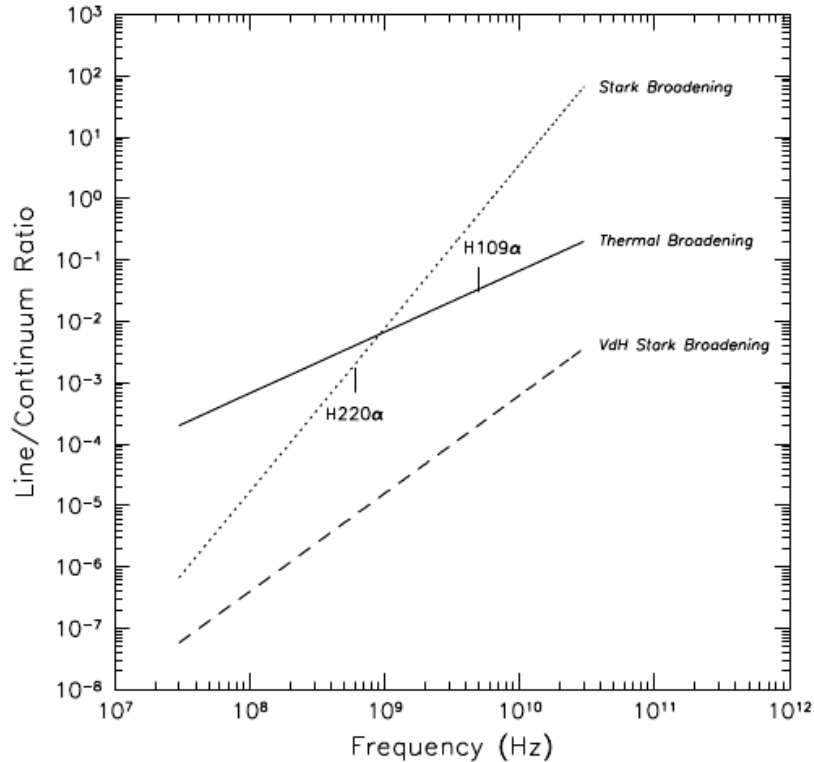
Humphreys α line (**H6 α**) at 12.3 μm (Humphreys 1953)

Hn α line \implies transition from **n+1** to **n**

Hn β line \implies transition from **n+2** to **n**

Are there transitions involving higher n?

3.1 Transitions between higher quantum levels: Effect of Stark broadening



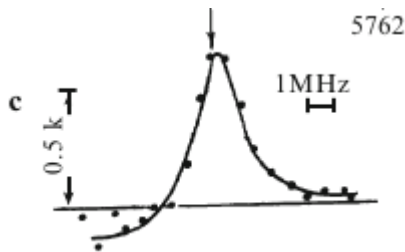
van de Hulst 1945

RRLs are too weak to be detectable at all radio frequencies

Kardashev 1959

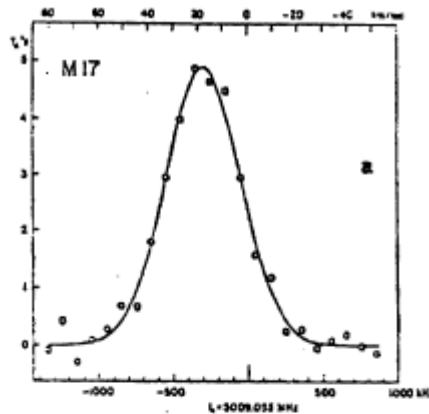
Stark broadening
negligible for $\nu > 10$ GHz

$> \Delta\nu(\text{thermal})$, but detectable even at lower frequencies



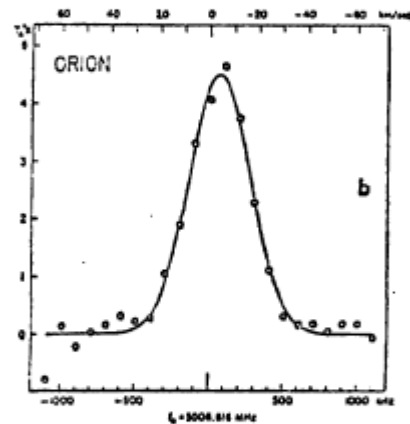
Detection of H90 α at 8.8 GHz by Sorochenko & Borodzich (1965)

3.2 Transitions from higher quantum levels: H109 α detection



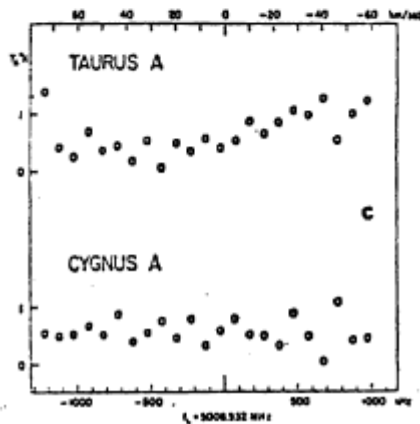
Hoglund & Mezger 1965

using 43-m NRAO Green Bank telescope

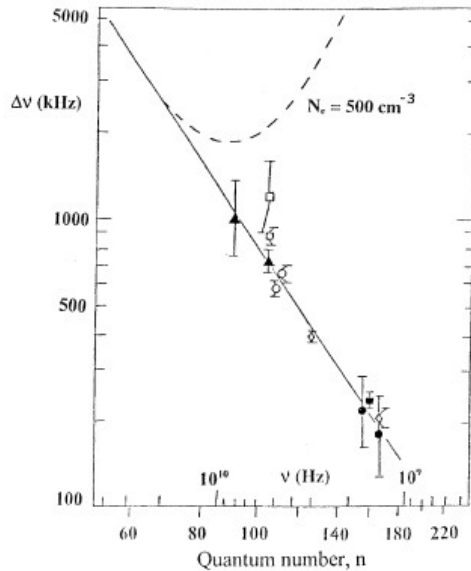


Many other studies conclusively detected
RRLs from a number of n levels

e.g. H253 α at 400 MHz by
Pefield, Palmer and Zuckerman (1967)



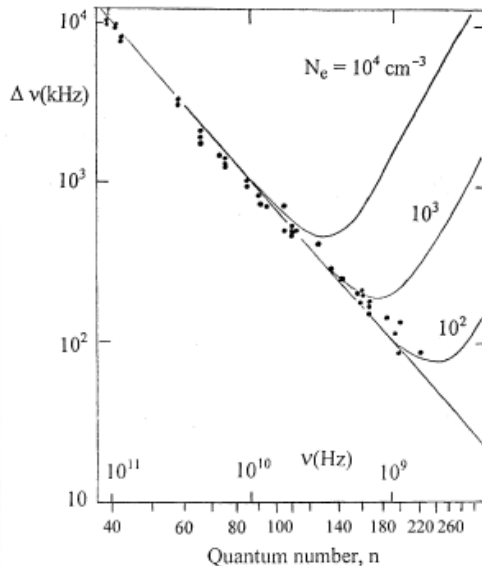
3.3 Transitions between higher quantum levels: Understanding Stark broadening through astrophysics



The observed line widths up to $n=166$ suggested Thermal, rather than, Stark broadening!!!

Does Stark broadening exist in astrophysical plasmas?

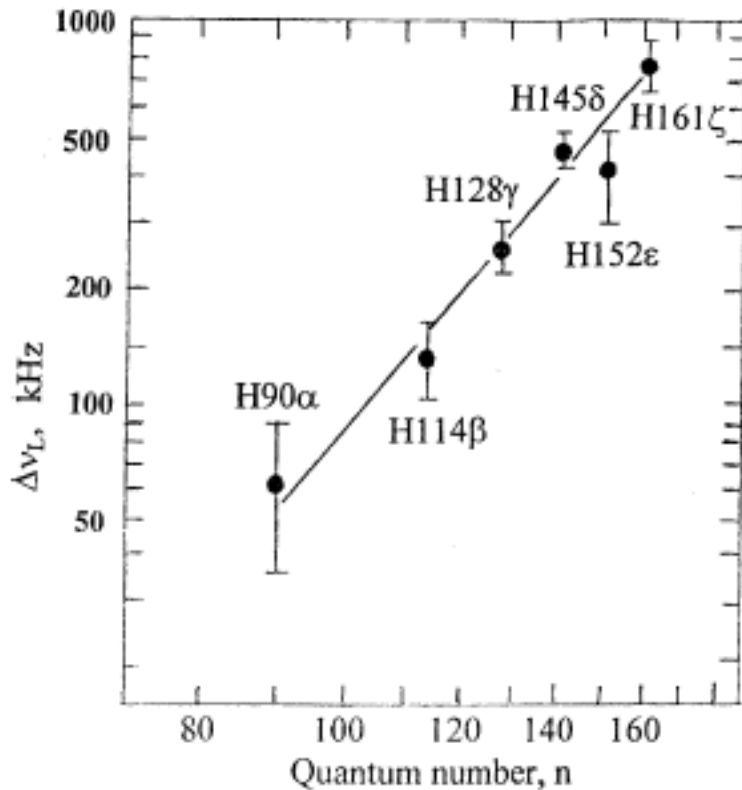
- Improved theoretical calculations explained the observed trend.
- However, theoretical densities $<$ inferred densities from optical lines.



====>

1. Density is not uniform in HII regions
2. high density gas that produces stark broadening doesn't contribute to the Line profile
Because: high n lines are at low frequency====> **Opaque**
3. Require beam-matched observations

3.4 Transitions between higher quantum levels: Understanding Stark broadening through astrophysics



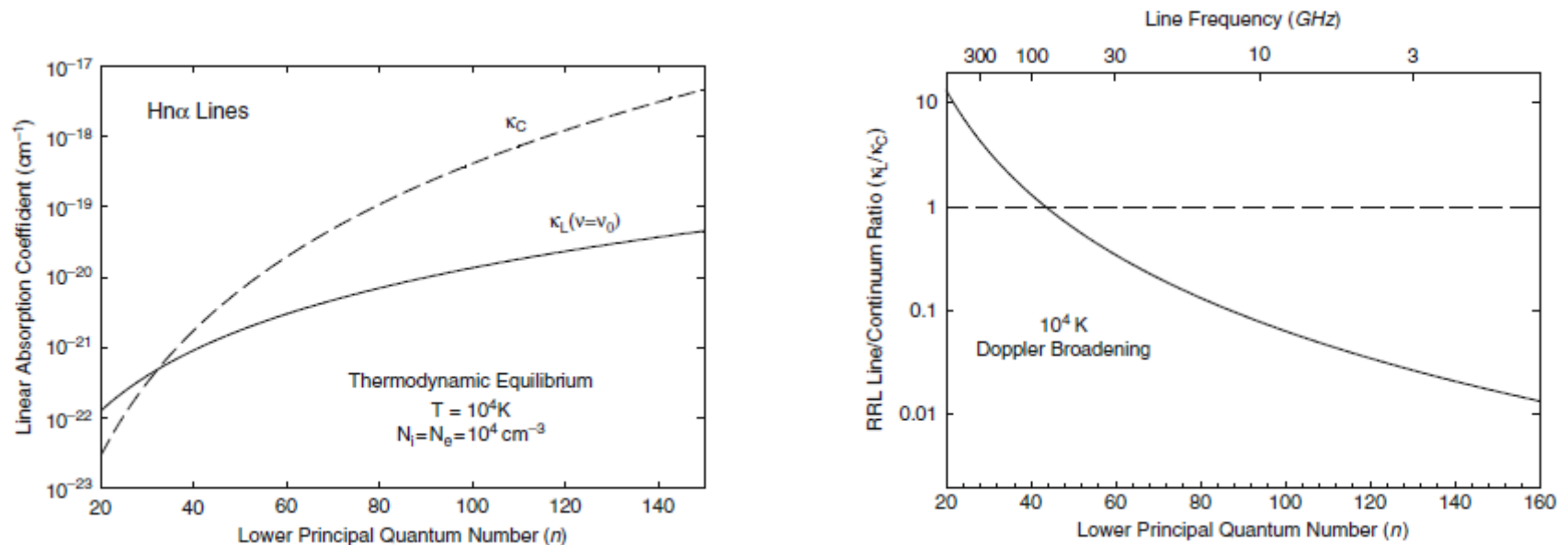
Beam-matched observations
At 9 and 36.5 GHz by Smirnov et al. (1984)
Established the existence and the correct
Theoretical framework of Stark broadening

$$\Delta\nu_L^e = 8.2N_e \left(\frac{n}{100}\right)^\gamma \left(1 + \frac{\gamma}{2} \frac{\Delta n}{n}\right).$$

- **Inelastic (n-changing) electron collisions** are the principal contributor of Stark broadening in astrophysical Plasmas with $\gamma \sim 4$
- i.e. ion collisions and elastic (l-changing) collisions don't contribute significantly.
- Impact approximation (interaction duration \ll the Time between interactions) is adequate for astrophysical plasmas.

4. Calculations of RRL line intensities (LTE)

$$\int_{\text{line}} \frac{I_L}{I_C} d\nu \approx 1.301 \times 10^5 \Delta n \frac{f_{n_1 n_2}}{n_1} \frac{\nu^{2.1}}{T^{1.15}} F \exp\left(\frac{1.579 \times 10^5}{n_1^2 T}\right).$$

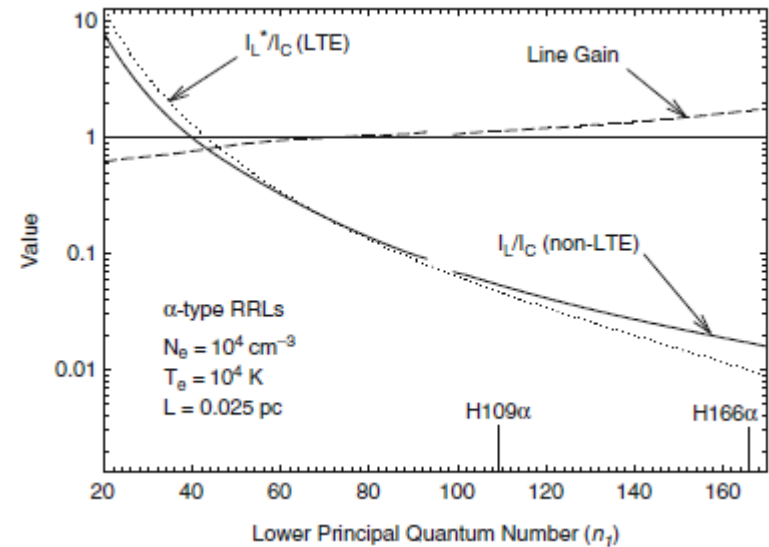
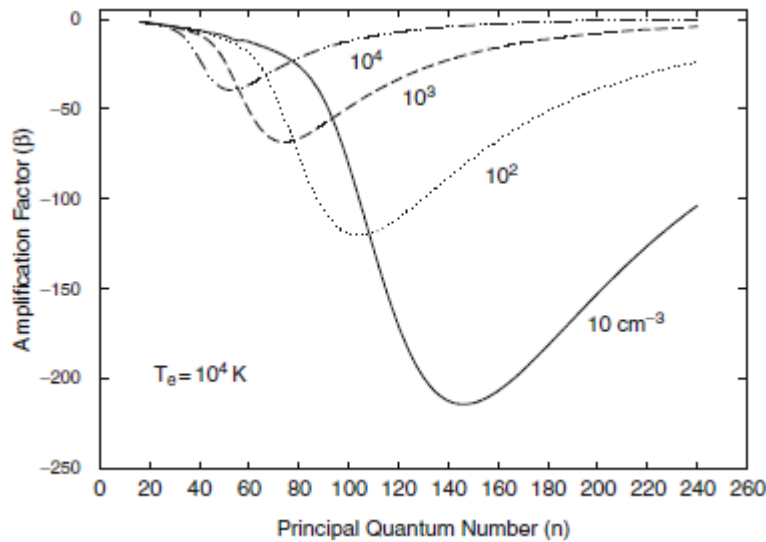


Line strength exceeds the continuum emission for $n < 43$ ($\nu > 79$ GHz)
 ==> Relatively easy to detect at mm wavelengths

4.1 Calculations of RRL line intensities (non-LTE): Line amplification

$$K_L(\text{non-LTE}) = K_L(\text{LTE}) * \beta$$

$$\text{Where } \beta = b_{n_1} \left(1 - \frac{kT_e}{h\nu} \frac{d \ln b_{n_2}}{dn} \Delta n \right)$$

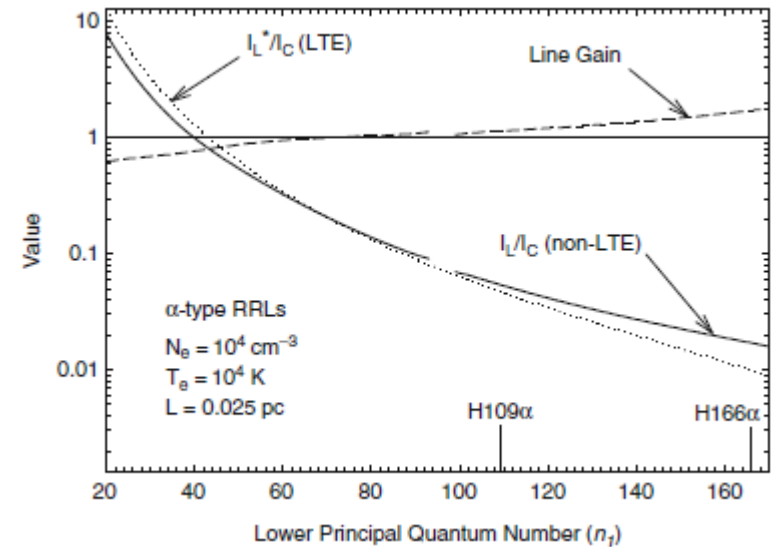
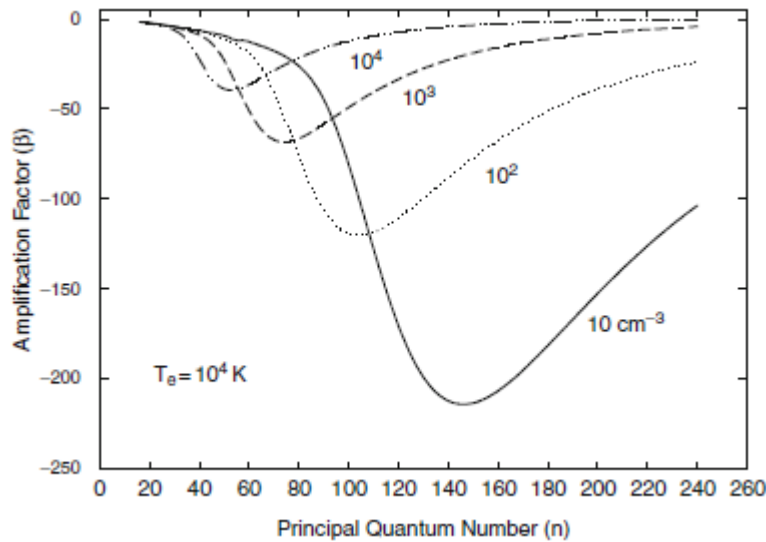


At large densities, greatest amplification occurs for mm-RRLs

4.1 Calculations of RRL line intensities (non-LTE): Line amplification

$$K_L(\text{non-LTE}) = K_L(\text{LTE}) * \beta$$

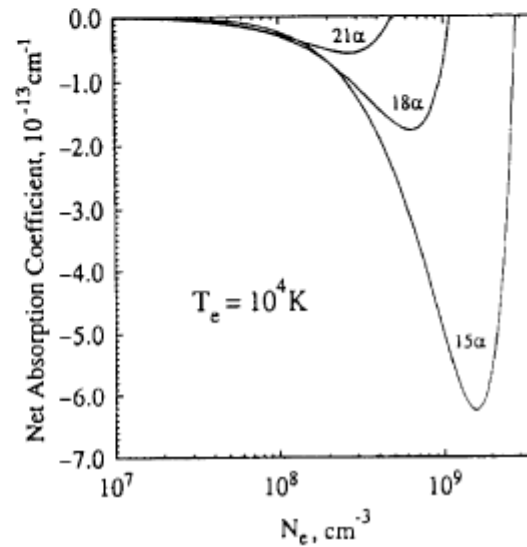
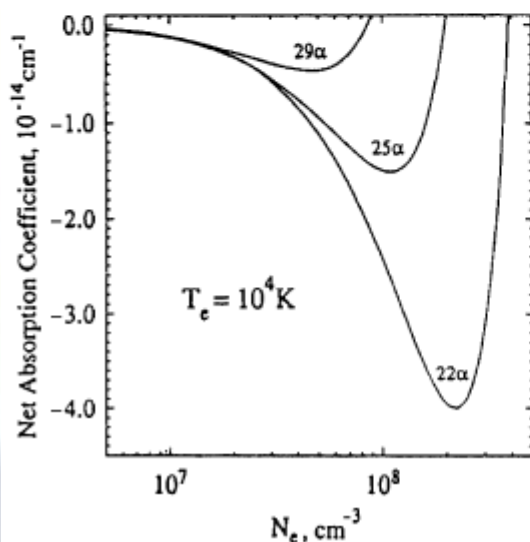
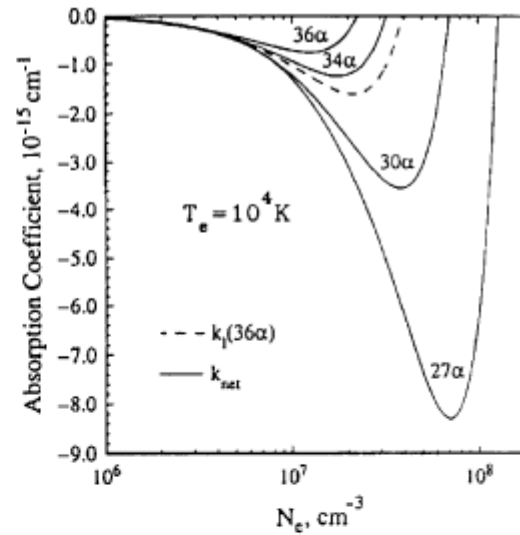
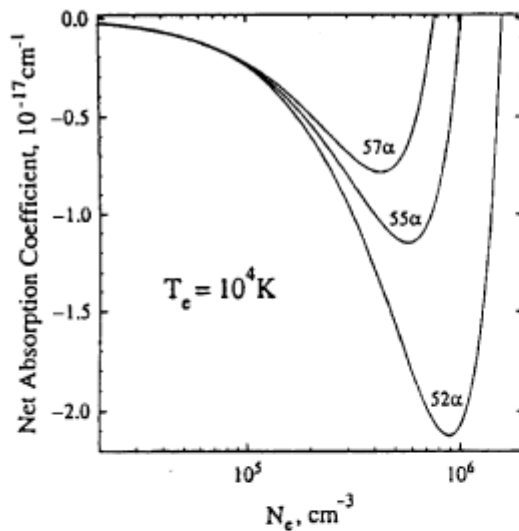
$$\text{Where } \beta = b_{n_1} \left(1 - \frac{kT_e}{h\nu} \frac{d \ln b_{n_2}}{dn} \Delta n \right)$$



At large densities, greatest amplification occurs for mm-RRLs

4.2 Calculations of RRL line intensities (non-LTE): maser

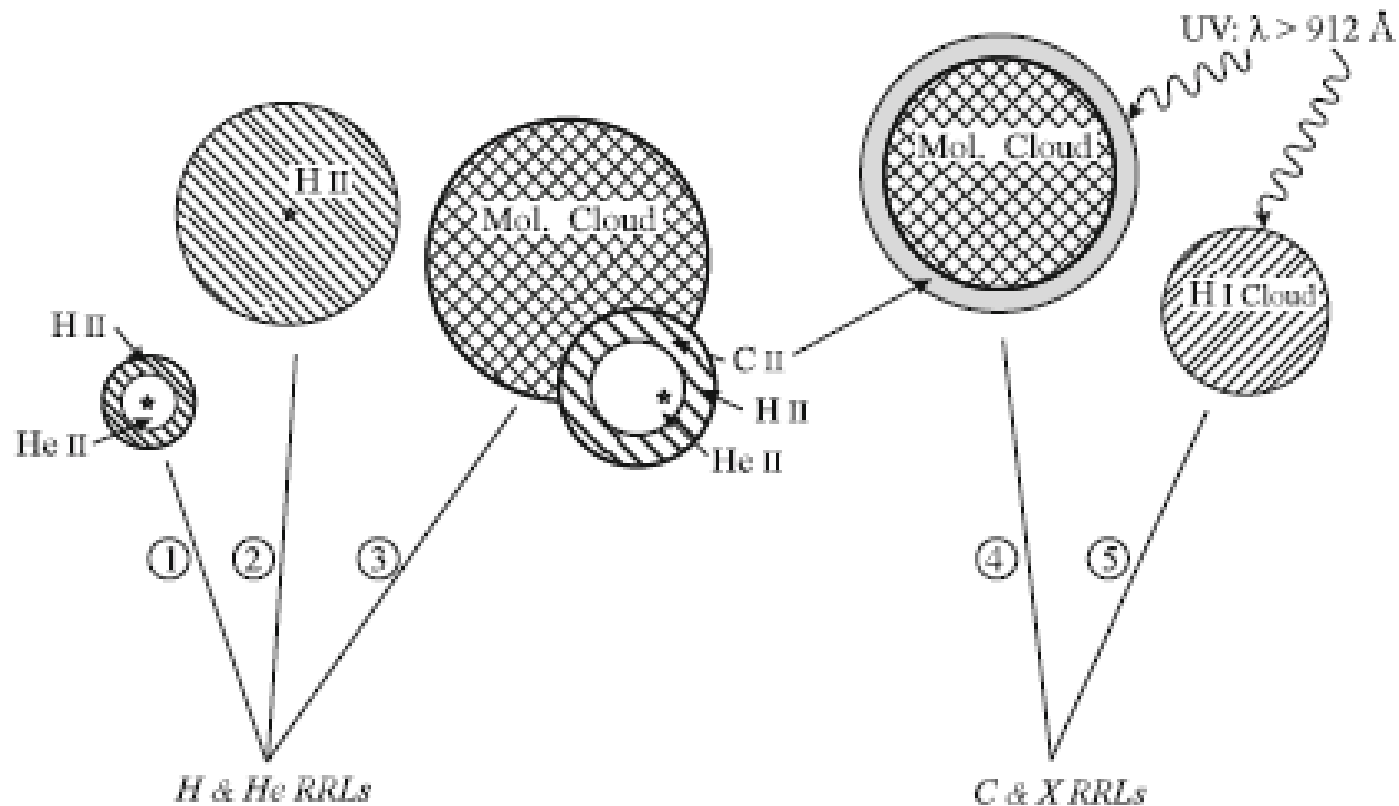
$\beta \ll 0$ and $\tau_V = \tau_C + \tau_L < 0$



For each group of lines, there exists a narrow range of densities, where the maser gain is maximum

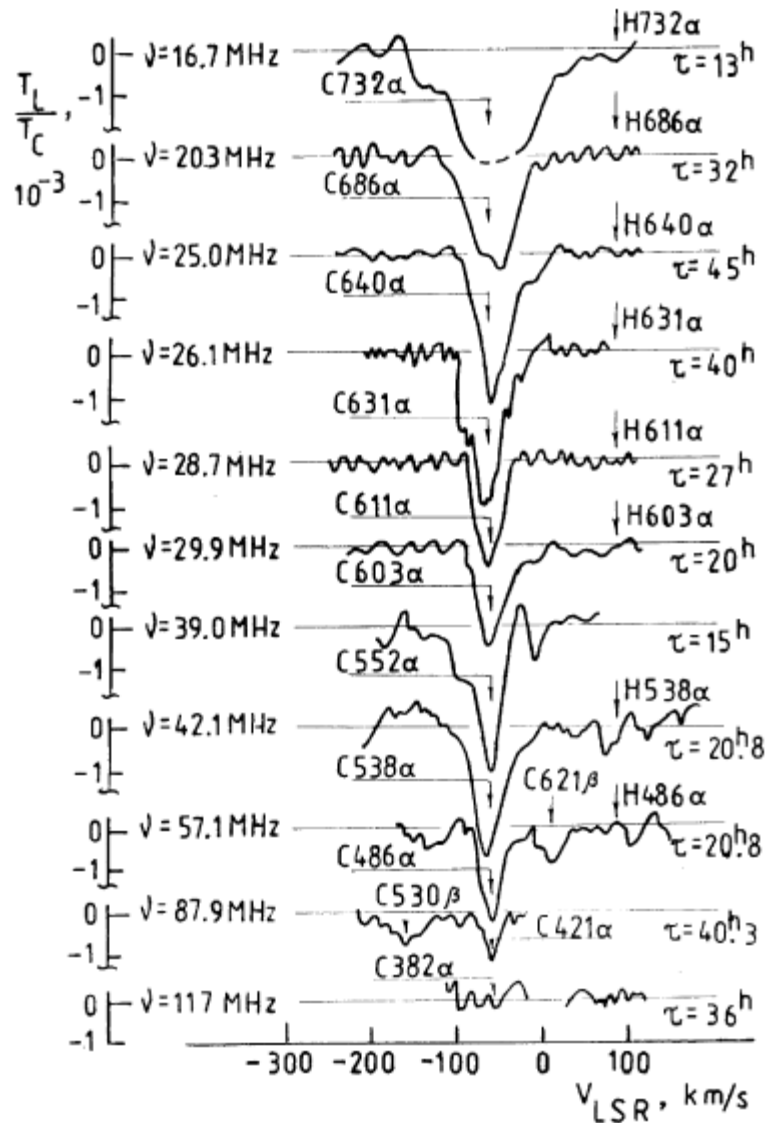
- Observed in MWC349 and η Carina
- Difficult to satisfy phase coherence over large emitting regions

5. Other regions from where RRLs can originate



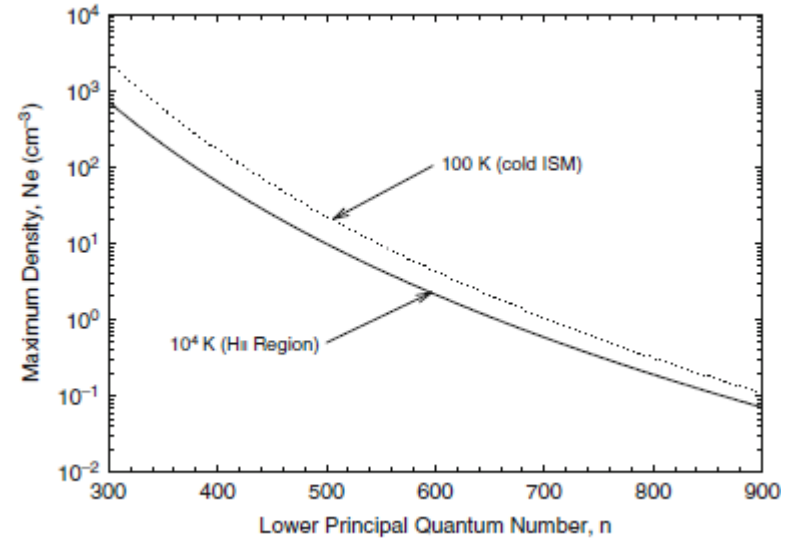
- 1 & 2 High and low density HII regions
3. CII region at the interface between HII and MC
4. CII region at the boundary of MC and diffuse ISM
5. CII region within HI clouds

5.1 Carbon RRLs



Sorochenko & Smirnov 1990

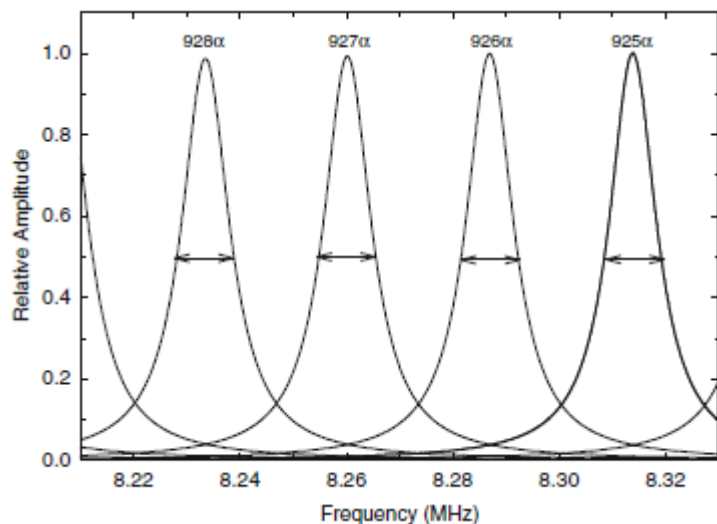
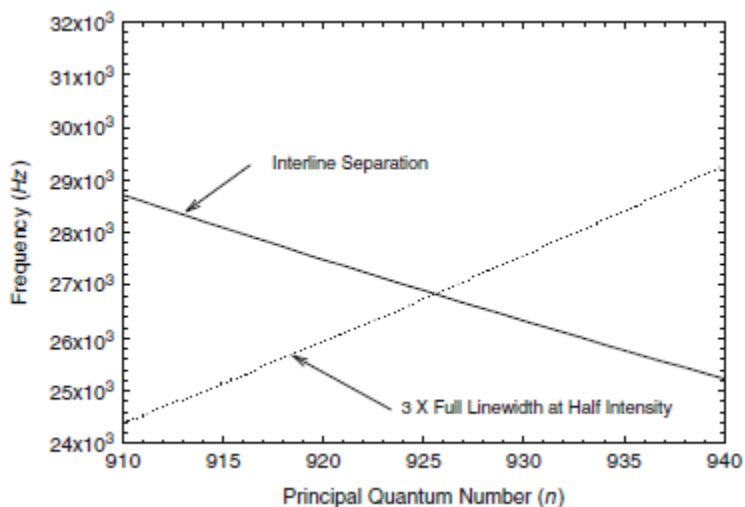
Why high-n CII lines are detected, but not high-n ($n > 300$) H lines?



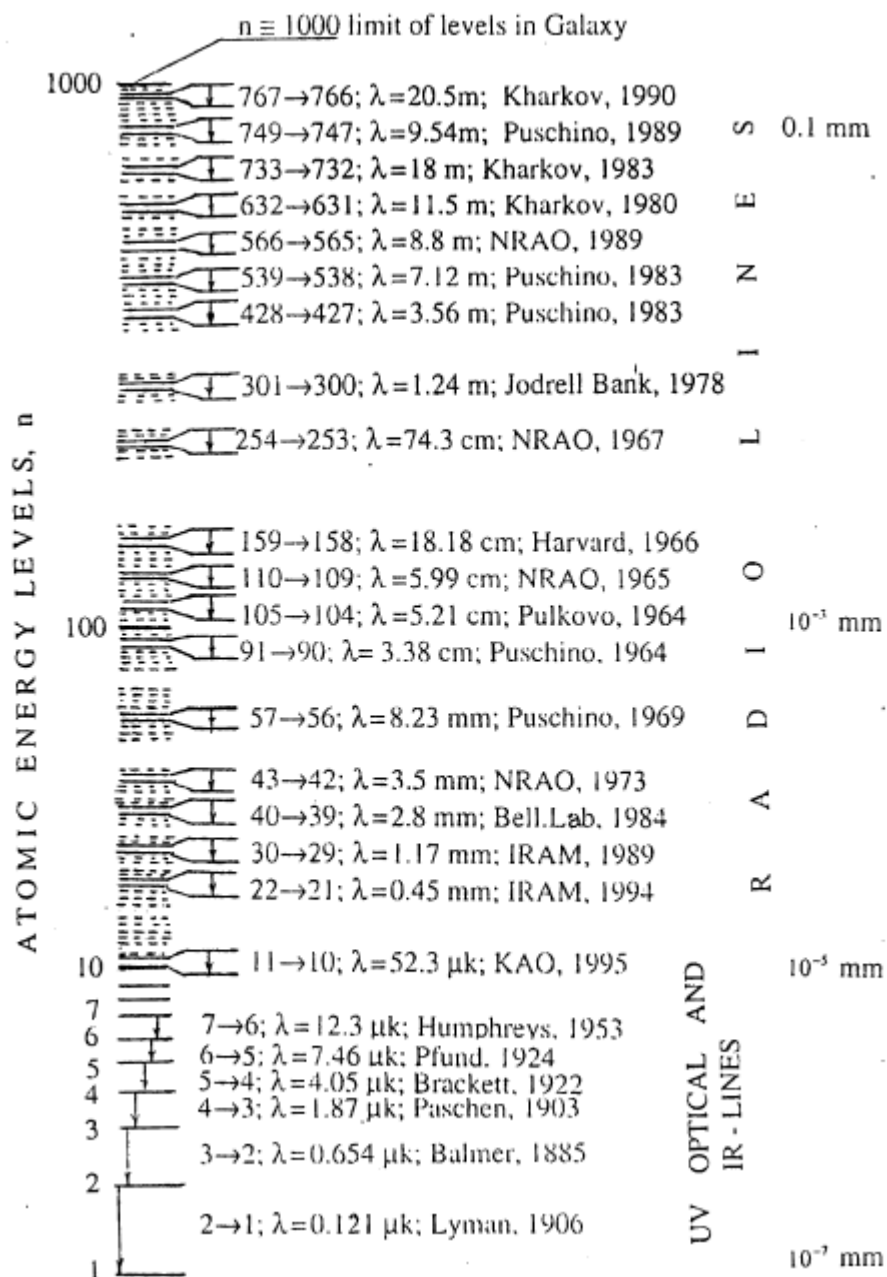
- Stark broadening
- at high-n
- $\nu(n_2) - \nu(n_1) \sim \Delta\nu(\text{Stark})$
- $\Delta\nu(\text{Stark})$ increases with densities
- ====> low-density cold ionized regions are required for high-n RRLs

**Ionized C present in diffuse, cold ISM
But not ionized Hydrogen**

6. Existence and detectability of the high quantum numbers



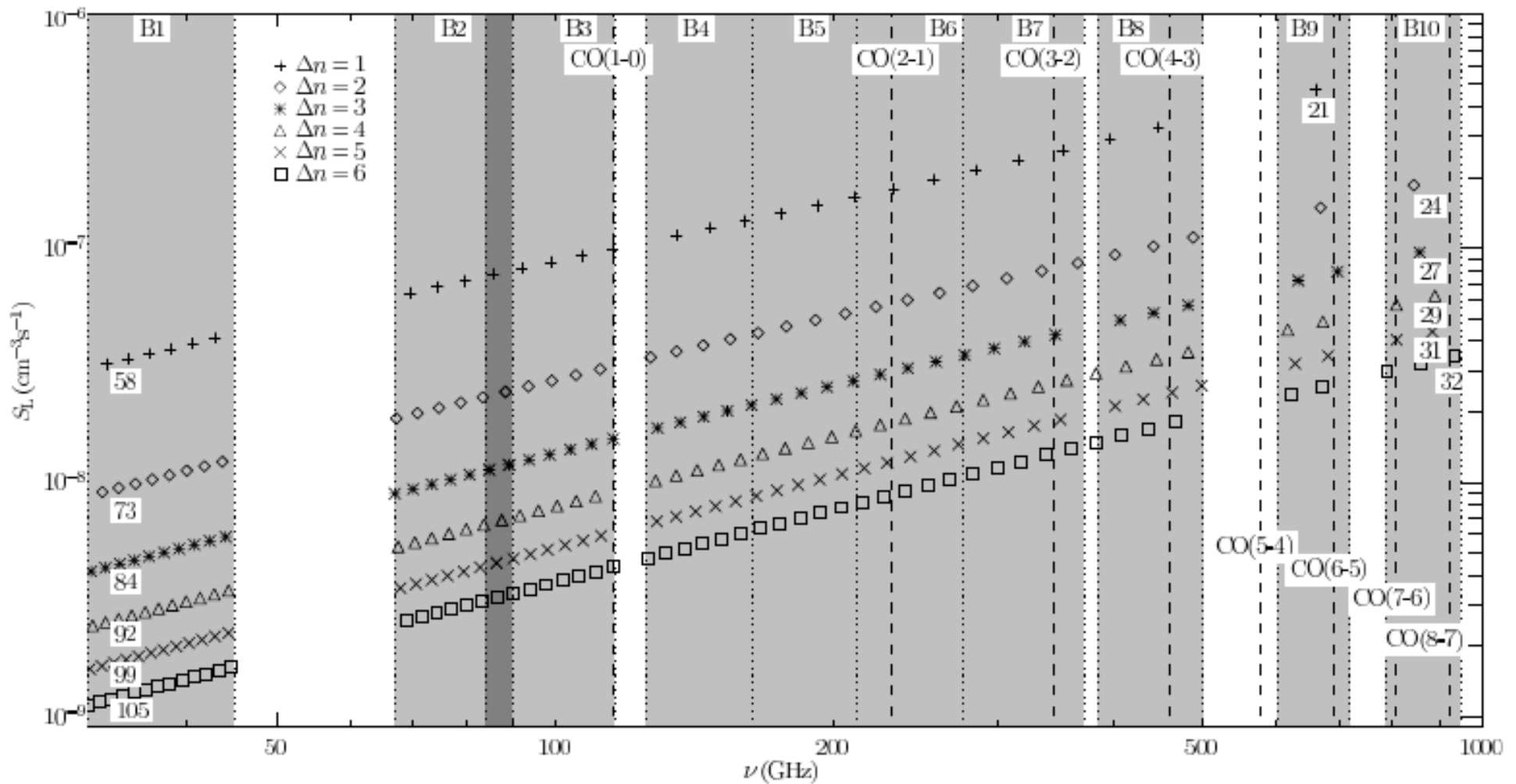
N=926 seems to be the limiting n value



7. Astrophysics using mm-wave RRLs

ALMA & EVLA

Peters et al. 2012



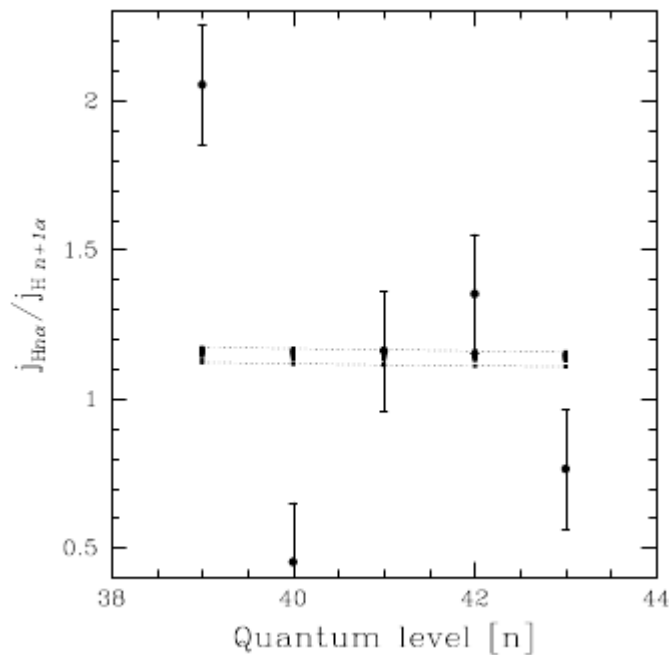
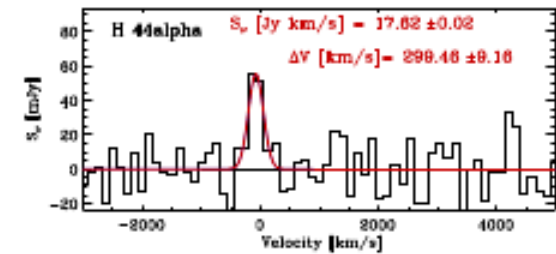
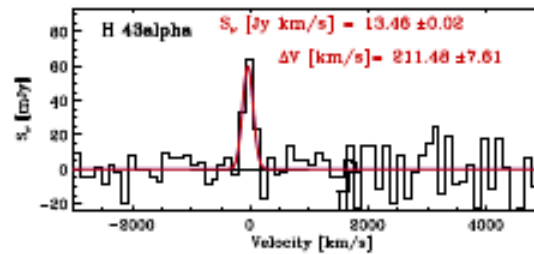
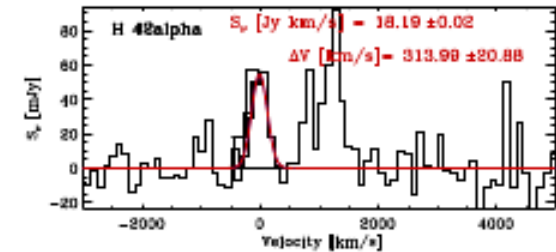
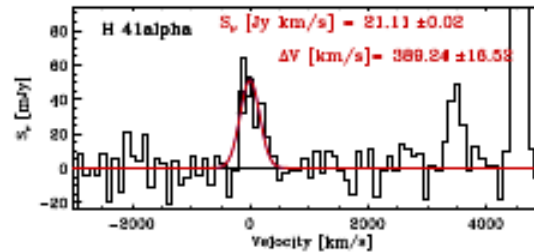
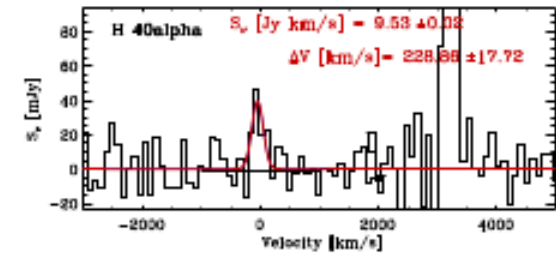
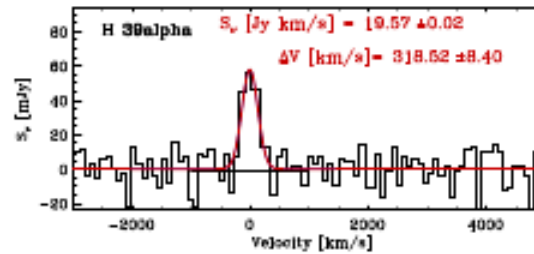
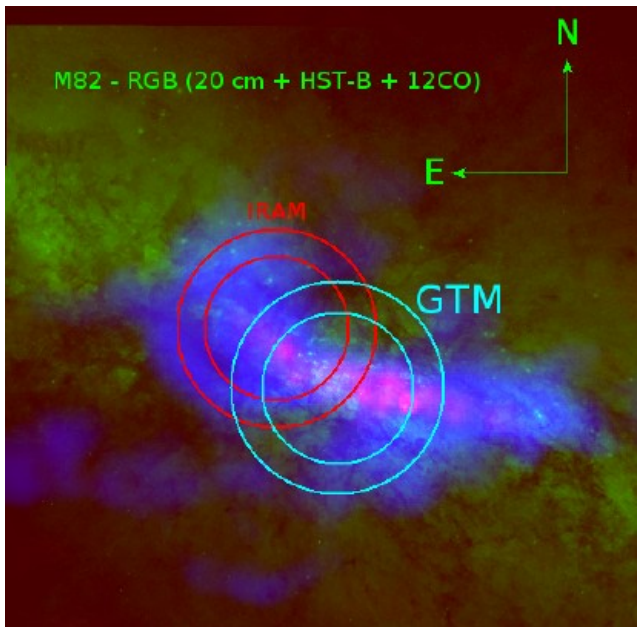
8. RRLs from external galaxies

Table 3.9 RRLs detected from extragalactic objects

| Galaxy | Type | Dist. (Mpc) | RRL | $I_L \Delta \nu_L$ ($10^{-19} \text{ W m}^{-2}$) | V_{Helio} (km s^{-1}) | ΔV_L (km s^{-1}) | References |
|----------------------|----------|----------------|---------------|---|--|--|--------------------------------|
| M82 | Ir | 3.25 | H27 α | 21.1 \pm 4.3 | | | Seaquist et al. (1996) |
| | | | H30 α | 5.12 \pm 1.0 | | | Seaquist et al. (1994) |
| | | | H41 α | 1.32 \pm 0.22 | | | Seaquist et al. (1996) |
| | | | H53 α | 0.22 \pm 0.06 | | | Puxley et al. (1989) |
| | | | H85 α | (4.6 \pm 0.7) $\times 10^{-3}$ | 180 \pm 10 | 149 \pm 25 | Bell and Seaquist (1978) |
| | | | H102 α | (8.5 \pm 1.4) $\times 10^{-3}$ | 173 \pm 10 | 174 \pm 20 | Bell and Seaquist (1978) |
| | | | H110 α | (1.05 \pm 0.1) $\times 10^{-2}$ | 163 \pm 10 | 293 \pm 20 | Shaver et al. (1978) |
| | | | H166 α | > 1.7 $\times 10^{-3}$ | 150 \pm 40 | 250 \pm 40 | Shaver et al. (1977; 1978) |
| | | | H166 α | (5.1 \pm 0.8) $\times 10^{-3}$ | 254 \pm 20 | 338 \pm 40 | Shaver et al. (1978) |
| NGC253 | Spiral | 3.4 | H92 α | (4.0 \pm 0.4) $\times 10^{-3}$ | 217 \pm 8 | 189 \pm 19 | Anantharamaiah and Goss (1990) |
| | | | H102 α | (1.3 \pm 0.3) $\times 10^{-2}$ | 132 \pm 25 | 309 \pm 65 | Seaquist and Bell (1977) |
| | | | H110 α | (2.9 \pm 0.6) $\times 10^{-3}$ | 209 \pm 13 | 185 \pm 32 | Anantharamaiah and Goss (1990) |
| | | | H166 α | (3.8 \pm 1.0) $\times 10^{-3}$ | 195 \pm 36 | 220 \pm 87 | Anantharamaiah and Goss (1990) |
| NGC2146 | Spiral | 13 | H53 α | (9.5 \pm 1.7) $\times 10^{-2}$ | \approx 880 | \approx 300 | Puxley et al. (1991) |
| | | | H92 α | 2.7 $\times 10^{-4}$ | 960 \pm 7 | 200 \pm 95 | Zhao et al. (1996) |
| NGC1365 | Seyf. II | 22.0 | H92 α | (12 \pm 2) $\times 10^{-4}$ | 1,670 \pm 80 | 310 \pm 110 | Anantharamaiah et al. (1993) |
| NGC3628 | S3 pec | 11.5 | H92 α | (8.6 \pm 1.5) $\times 10^{-4}$ | 864 \pm 56 | 170 \pm 70 | Anantharamaiah et al. (1993) |
| IC694 ^a | Sc | 40.3 | H92 α | (3.9 \pm 1.0) $\times 10^{-4}$ | 3,020 \pm 90 | 350 \pm 110 | Anantharamaiah et al. (1993) |
| NGC3690 ^a | Sc | | H92 α | (1.5 \pm 0.2) $\times 10^{-4}$ | 3,080 \pm 40 | 210 \pm 30 | Zhao et al. (1997) |
| Arp 220 | FIR | 73 | H31 α | >1.65 \pm 0.1 | | | Anantharamaiah et al. (2000) |
| | | | H40 α | 0.39 \pm 0.05 | 5,513 | 179 | Anantharamaiah et al. (2000) |
| | | | H42 α | 0.22 \pm 0.02 | 5,424 | 210 | Anantharamaiah et al. (2000) |
| | | | H92 α | 3.5 $\times 10^{-4}$ | 5,560 \pm 70 | 320 \pm 120 | Zhao et al. (1996) |
| | | | H92 α | (8 \pm 1.5) 10^{-4} | 5,450 \pm 20 | 363 \pm 45 | Anantharamaiah et al. (2000) |
| M83 | SBc/b | 5 | H92 α | 2.8 $\times 10^{-4}$ | 500 \pm 30 | 95 \pm 30 | Zhao et al. (1996) |
| NGC660 | SBa pec | 11.3 | H92 α | 5.6 $\times 10^{-4}$ | 850 | 377 | Phookun et al. (1998) |

^aIC694 and NGC3690 are an interacting system

8.2 RRLs from LMT/RSR from external galaxies: M82



- 6 RRLs are detected in M82
- Line ratios for some lines agree with the expected values
- require higher SNR to analyze profiles

Reference:

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