



*Lecture:*

# *CALIBRATION OF MM AND SUBMM OBSERVATIONS: ATMOSPHERIC EFFECTS*



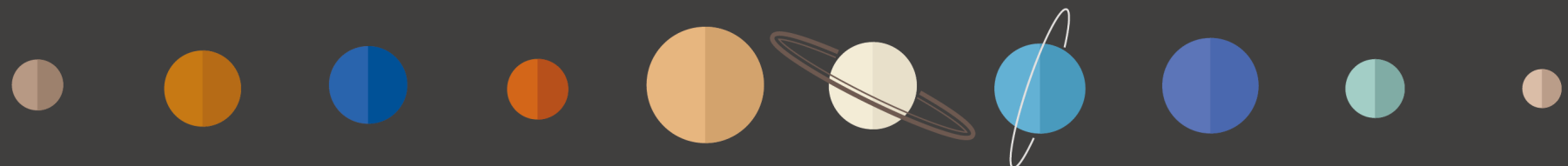
*G. Haro School on Molecular Astrophysics, 11-20 October 2016*

## OUTLINE:

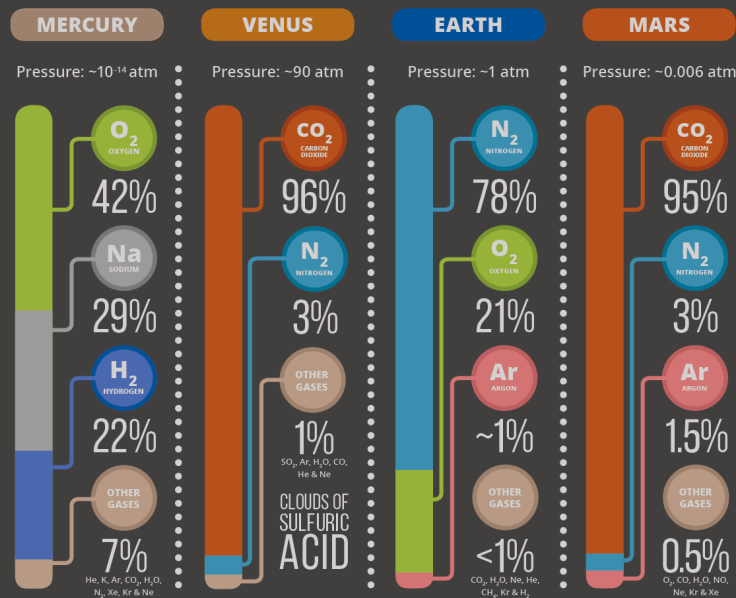
- *The Earth's atmosphere: absorption and scattering of EM radiation*
- *The millimeter wavelength range*
- *Curves of atmospheric transmission*
- *Observational strategies*
- *Calibration (atmospheric): single-dish observations*
- *ATM: atmospheric transmission model*
- *Radiometers*
- *Calibration (atmospheric): interferometry*

## - Solar system atmospheres:

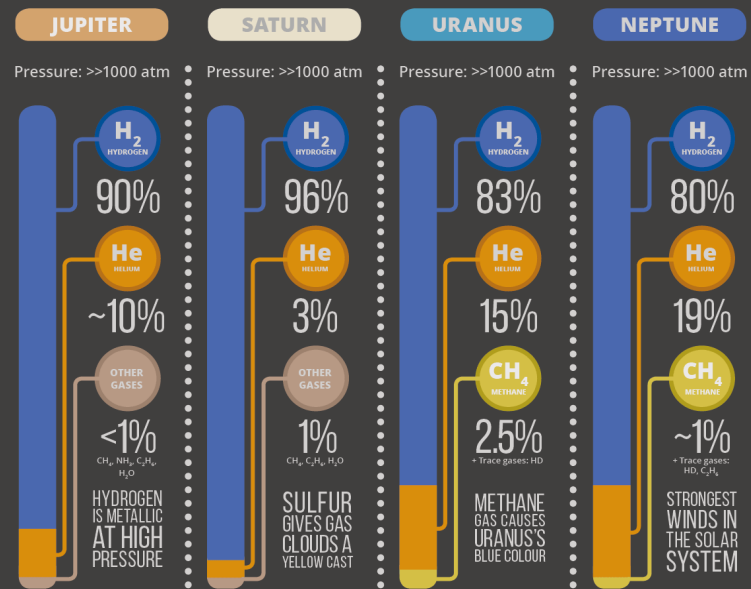
# THE ATMOSPHERES OF THE SOLAR SYSTEM



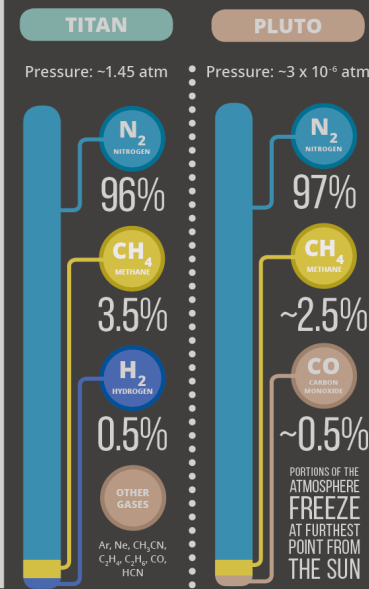
### The Terrestrial Planets



### The Gas Giants



### Other Bodies



Note: Planet sizes not to scale. Pressures for terrestrial planets are surface pressures. Mercury's atmosphere is not an atmosphere in the strict sense of the word, being a trillion times thinner than Earth's.

# Earth's atmosphere: composition

## Composition of the Atmosphere Near Earth's Surface

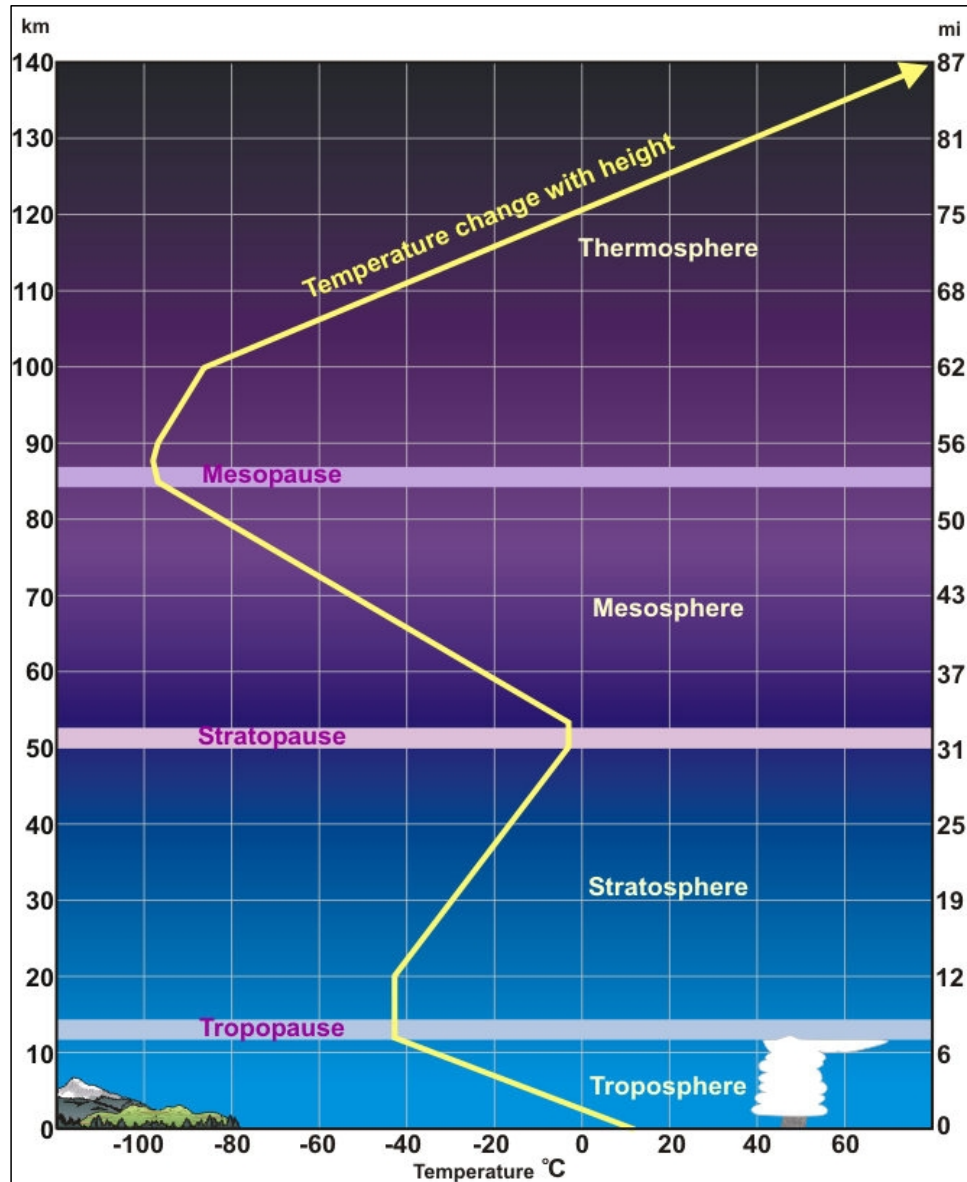
Permanent Gases			Variable Gases	
Gas	Symbol	Percent (by Volume) Dry Air	Gas (and Particles)	Symbol
Nitrogen	N <sub>2</sub>	78.08	Water vapor	H <sub>2</sub> O
Oxygen	O <sub>2</sub>	20.95	Carbon dioxide	CO <sub>2</sub>
Argon	Ar	0.93	Methane	CH <sub>4</sub>
Neon	Ne	0.0018	Nitrous oxide	N <sub>2</sub> O
Helium	He	0.0005	Ozone	O <sub>3</sub>
Hydrogen	H <sub>2</sub>	0.0006	Particles (dust, soot, etc.)	
Xenon	X <sub>2</sub>	0.000009	Chlorofluorocarbons	

*- Water vapor content will determine the feasibility of observations in the mm and submm range*



# Earth's atmosphere: structure

## - Layers of the atmosphere:

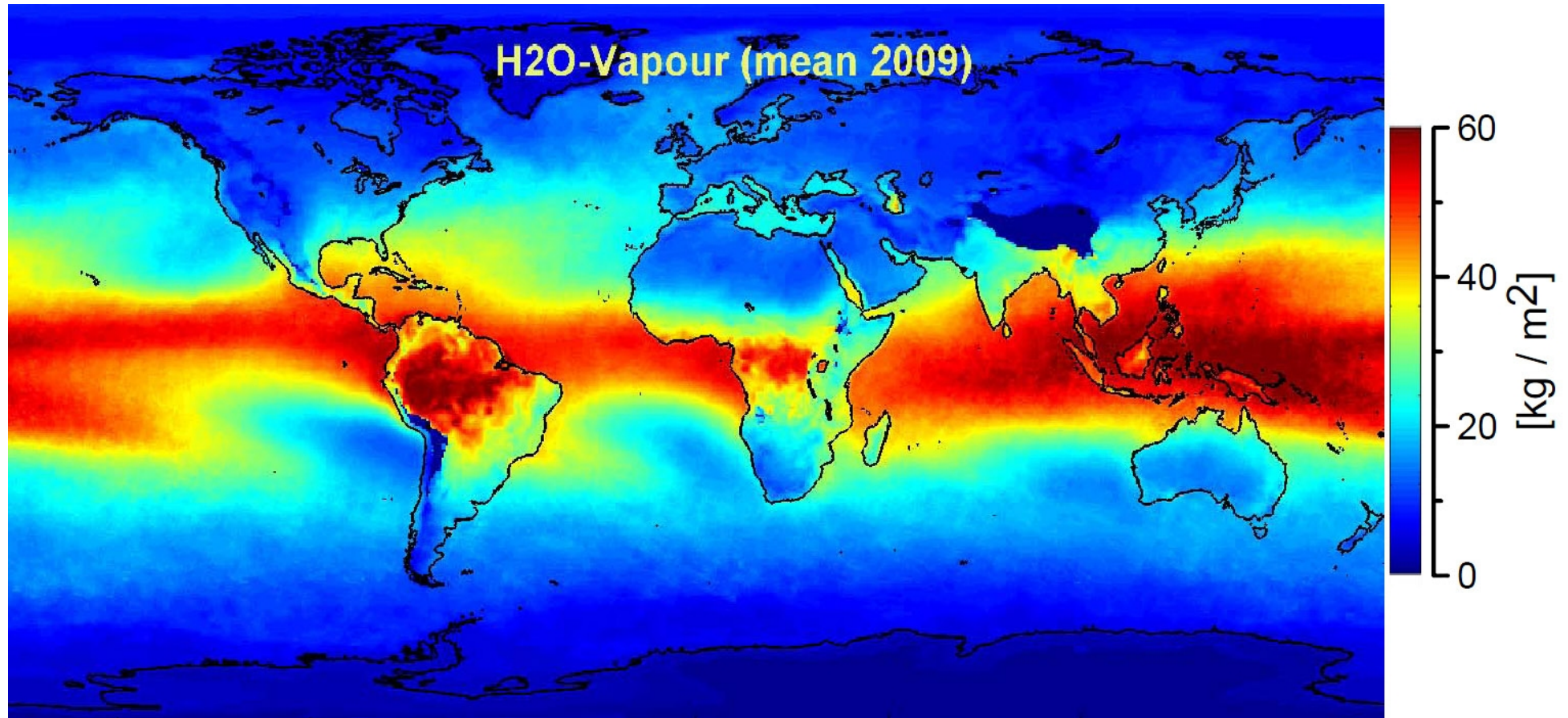


- 70-80% of the total mass of the atmosphere is contained in the troposphere

- Troposphere contains almost all atmospheric water vapor

# *Earth's atmosphere: water vapor*

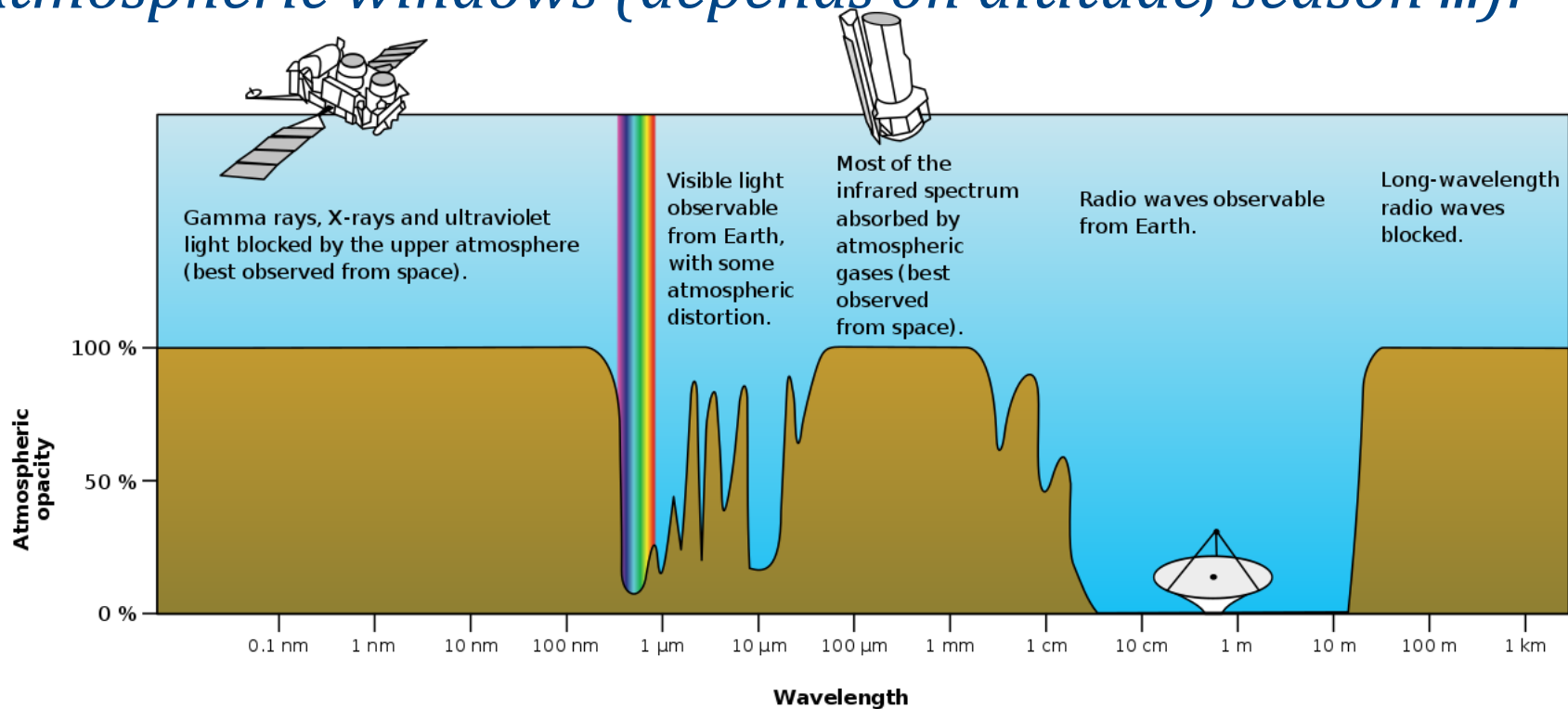
*- Water vapor:*



*Water vapor content is variable (~1-5% by volume)*

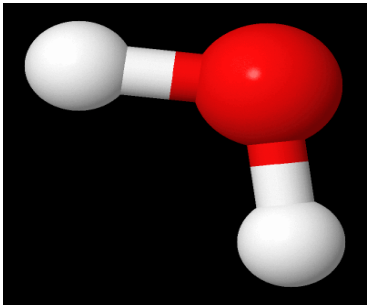
# Earth's atmosphere: physical processes

- The atmosphere absorbs and transmits different wavelengths of EM radiation
- The main physical processes involved are absorption and scattering
- Atmospheric windows (depends on altitude, season ...):

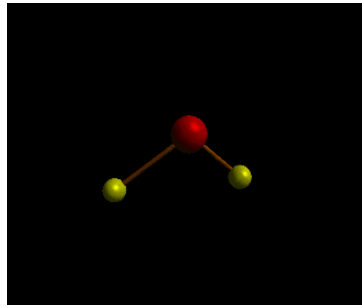


# Earth's atmosphere: absorption process

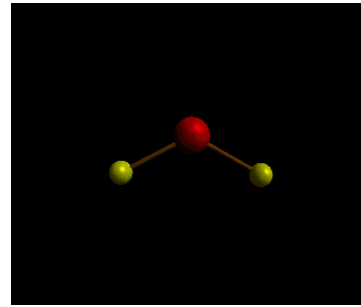
- Molecules in the atmosphere absorb photons at certain wavelengths (electronic, rotational, vibrational, and ro-vibrational transitions + ionisation + dissociation)



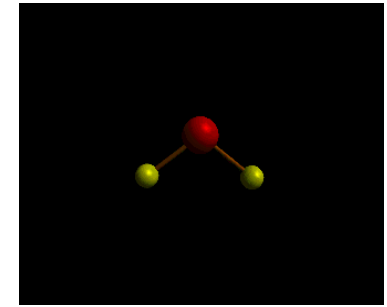
Rotation



Antisymmetric stretching



Bending



Symmetric stretching

And also overtones, combinations of modes ...



Rotation+vibration

## Most important absorbers:

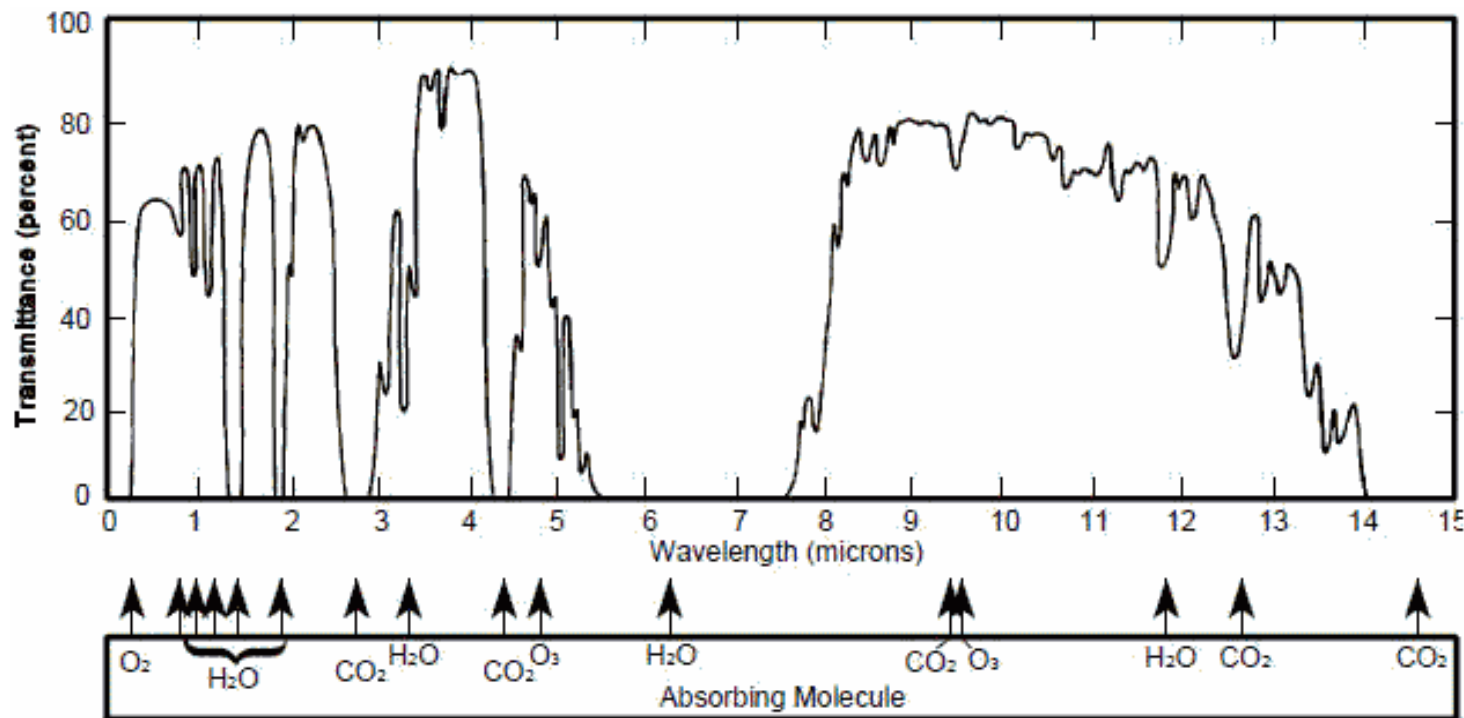
Water vapor: low abundance but it has electric dipolar transitions

Oxygen: high abundance but it has magnetic dipolar transitions

$(EDT/MDT)_{strength} \sim [100-1000]$

# Earth's atmosphere: absorption visible and IR

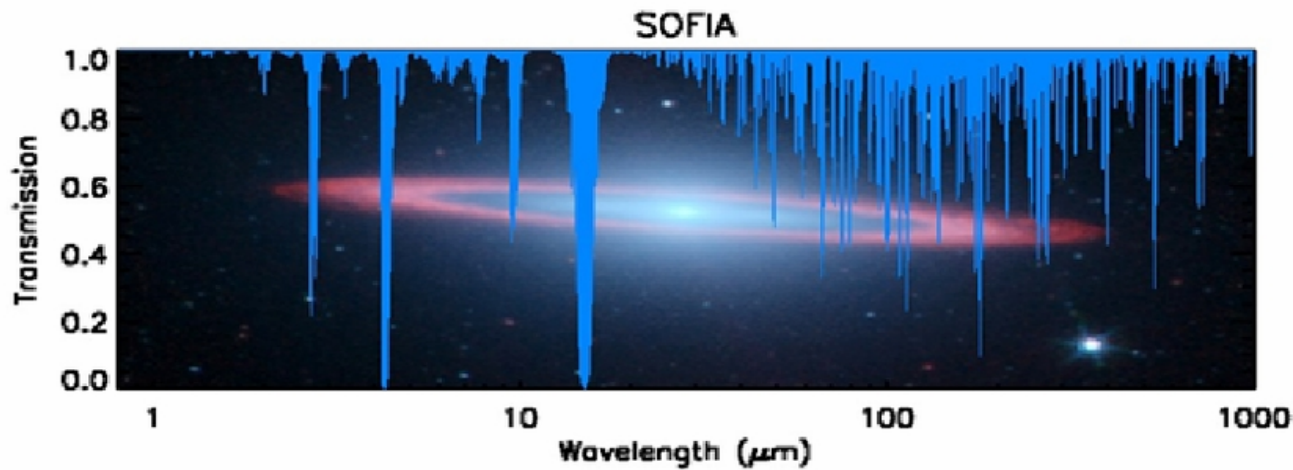
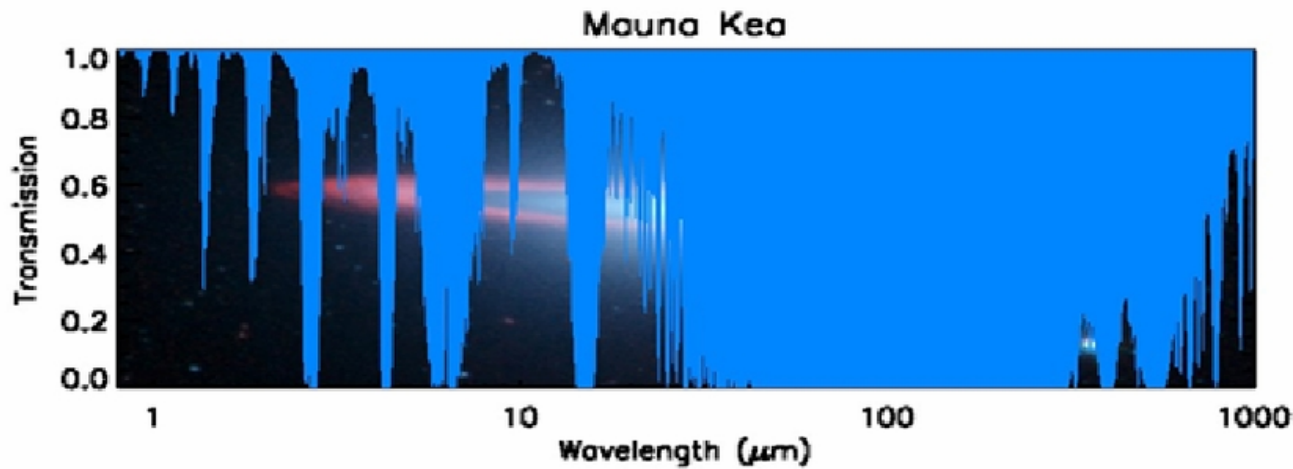
- Absorption in the visible and IR is caused by gases in the atmosphere, mainly: Water vapor ( $H_2O$ ), carbon dioxide ( $CO_2$ ), and ozone ( $O_3$ )





# Earth's atmosphere: infrared altitude transmission

- Increasing altitude improves transmission



*Aprox. 4500 m.*



*Aprox. 13000 m.*



# *Earth's atmosphere: scattering*

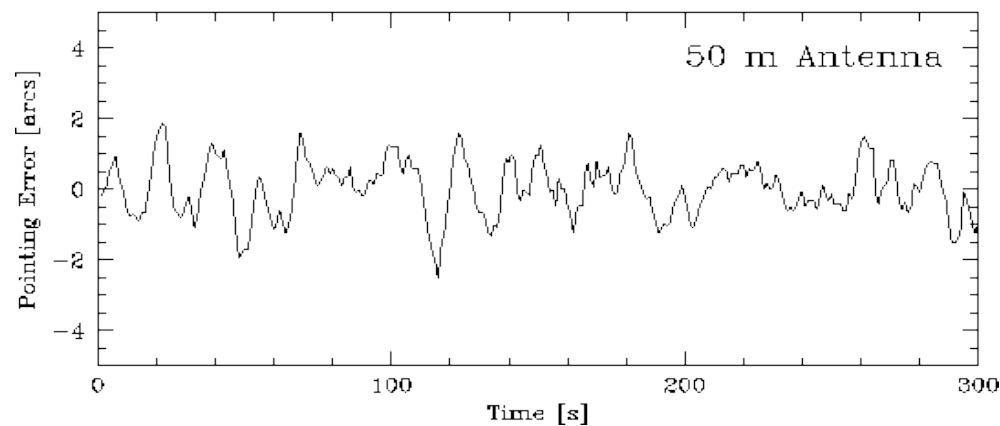
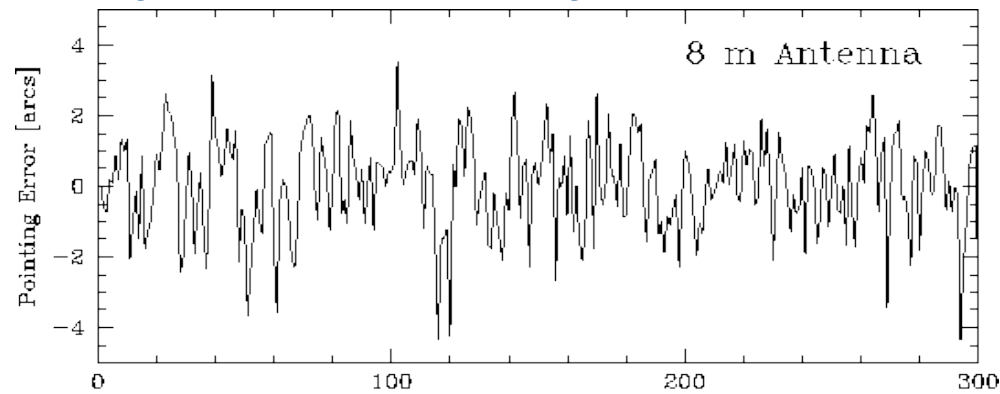
- *Relevant types of scattering: Rayleigh and Mie*
- *Rayleigh scattering:  $x=2\pi r/\lambda \ll 1$  (e.g. VIS molecules)*
  - *Wavelength dependency:  $\lambda^{-4}$*
- *Mie scattering:  $x \sim 1$  (e.g. VIS dust, water droplets, hydrometeors)*
  - *Not so wavelength dependent*





# Earth's atmosphere: anomalous refraction or “radio-seeing”

- Atmospheric turbulence causes pointing errors ( $\sim 1''$ ) and results are worst with poor weather conditions
- This is particularly worse for interferometric observations (different columns of water vapor for each antenna): phase errors



*CORRECTION  
WITH  
RADIOMETERS  
FOR  
INTERFEROMETERS*

## *Earth's atmosphere: long wavelengths*

*- Ionosphere: UV radiation from the Sun photodissociates molecules (Lyman- $\alpha$ , NO, O<sub>2</sub>, ...) producing ions and free electrons that interact with EM waves*

*- Transmission cut-off (plasma frequency):*

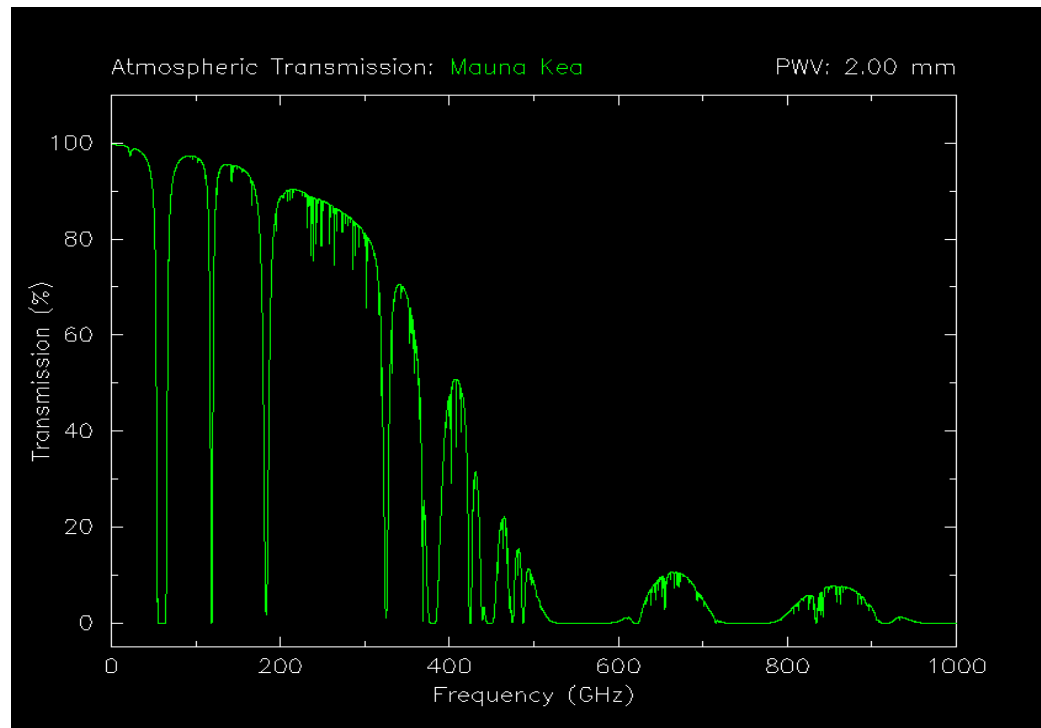
$$\frac{\nu_p}{\text{kHz}} = 8.97 \sqrt{\frac{N_e}{\text{cm}^{-3}}}$$

*- Electron density varies between  $1.5 \times 10^6 \text{ cm}^{-3}$  (daytime) down to  $2.5 \times 10^5 \text{ cm}^{-3}$  (at night)*

*- Observatories in radio-quiet locations (human interference)*

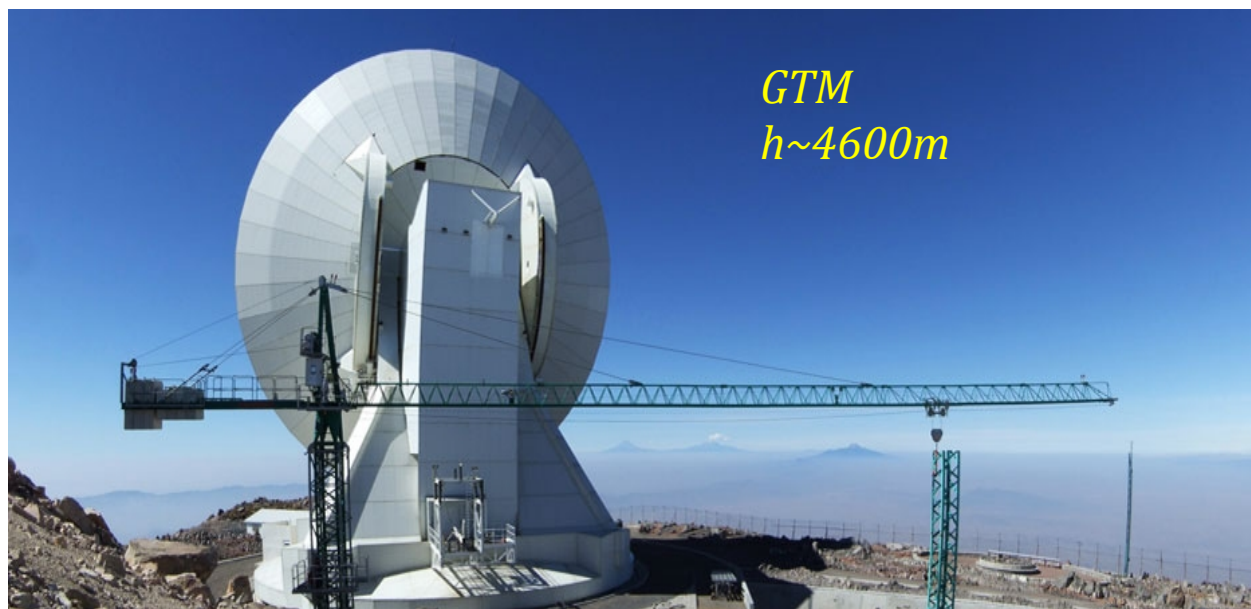
# The mm and submm wavelength range

- Atmospheric opacity mainly due to:
  - Water vapor ( $H_2O$ ) bands: 1.63, 0.92mm ...
  - Oxygen ( $O_2$ ) bands: 2.52, 5mm ...
- . And other molecules like  $N_2$  or  $CO_2$  for  $\nu > 300\text{GHz}$



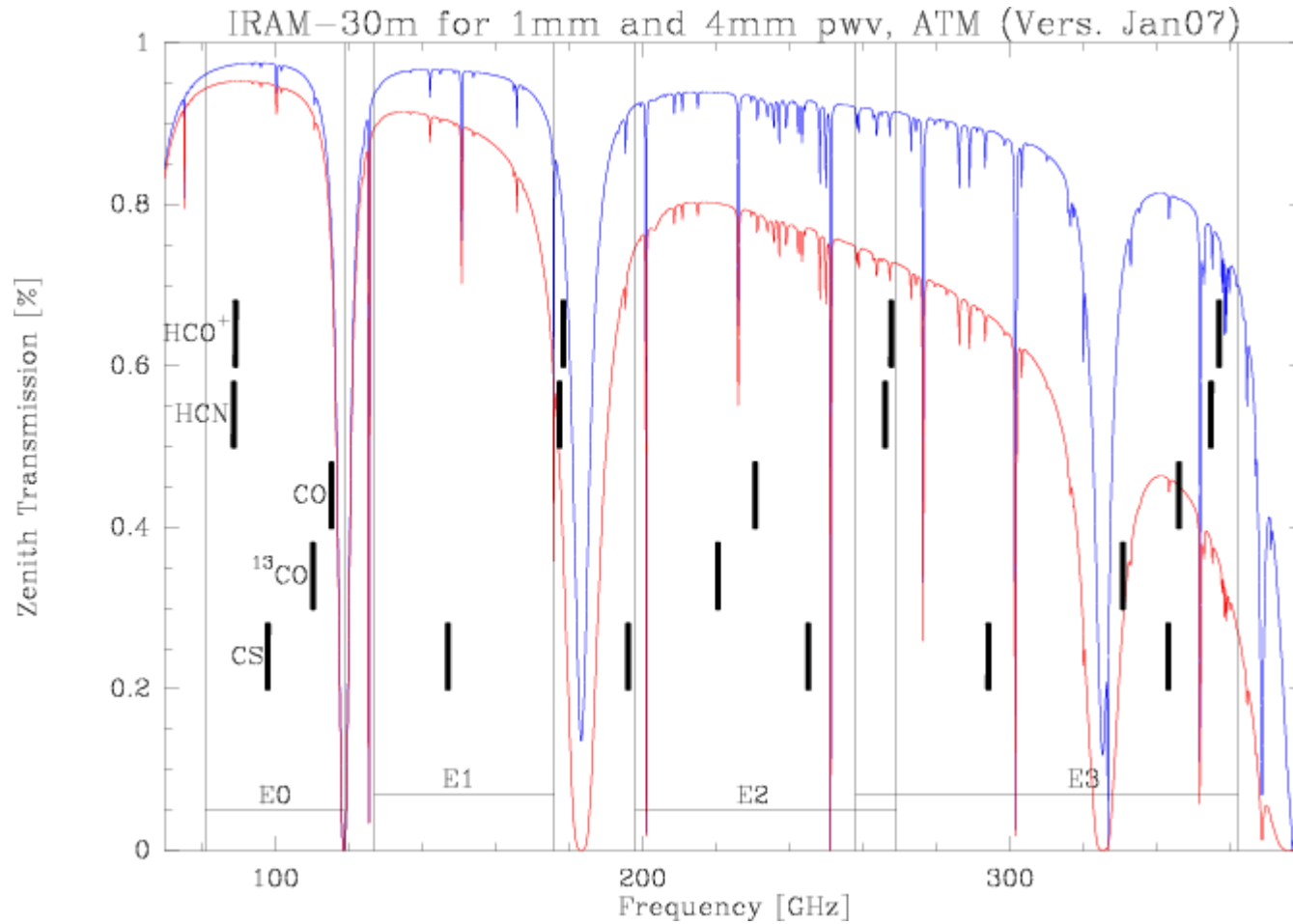
# The mm and submm wavelength range: altitude

- *Observatories at high altitude and dry atmospheric conditions*



# Curves of atmospheric transmission

- IRAM-30m ( $h \sim 2850\text{m}$ ):





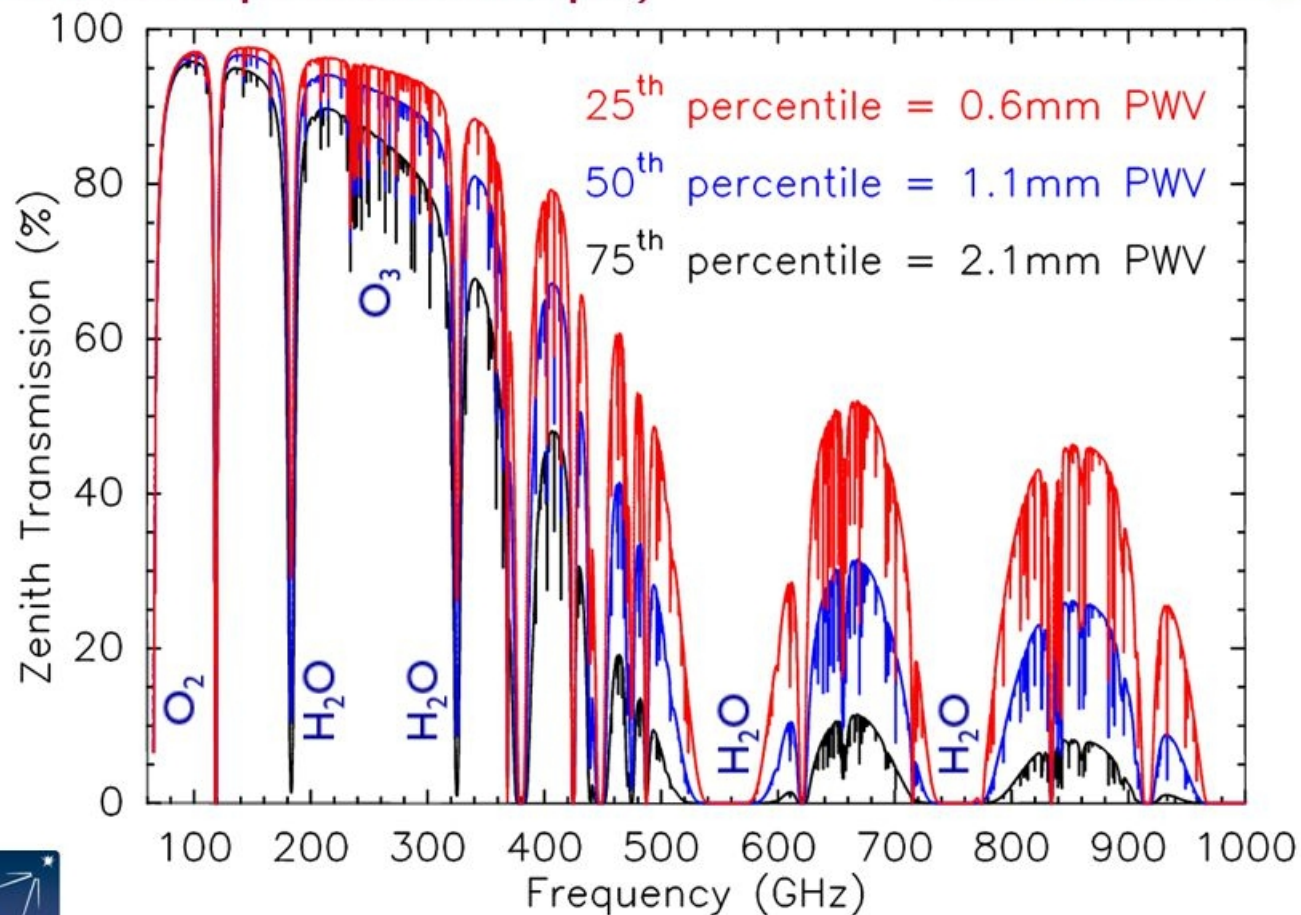
# Curves of atmospheric transmission

- ALMA ( $h \sim 5000\text{m}$ ):

## Atmospheric Opacity

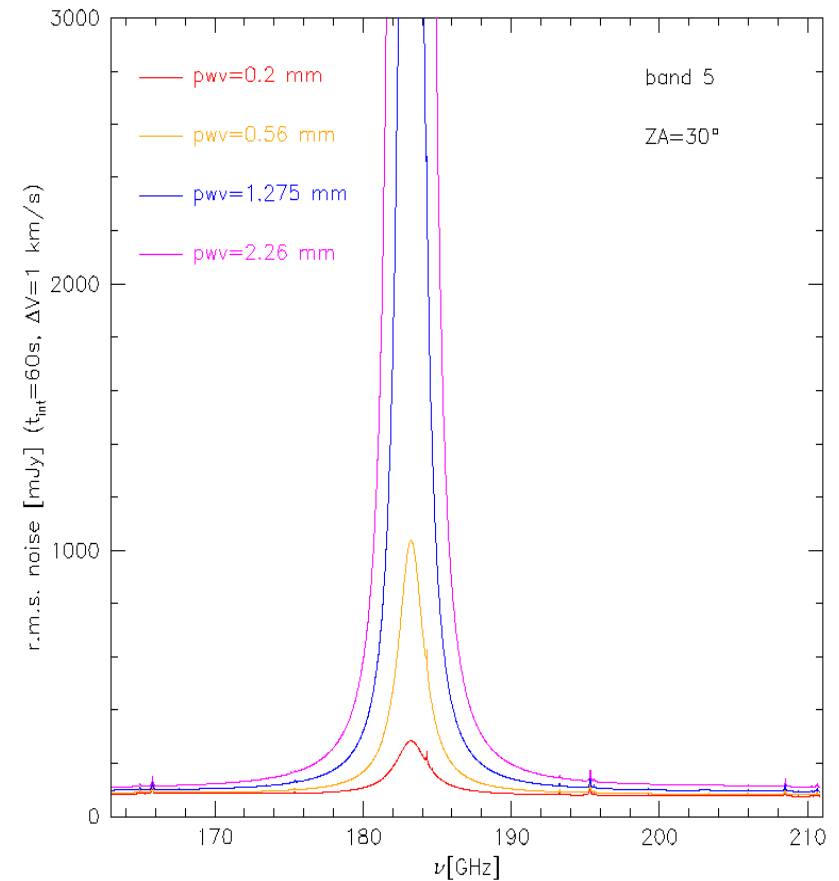
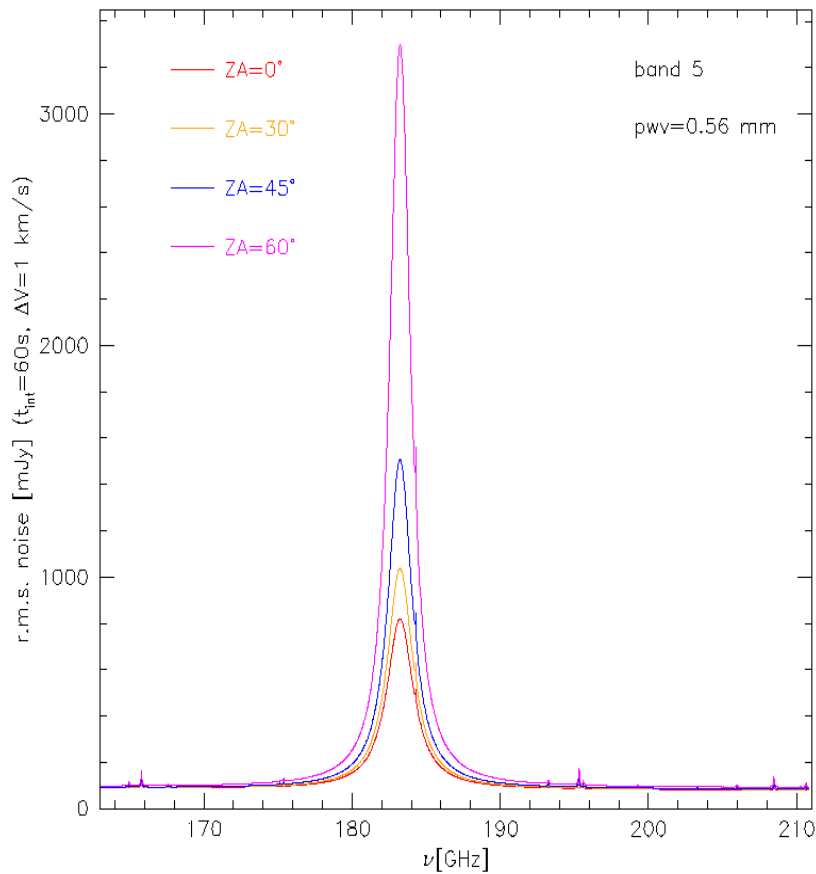
(PWV = Precipitable Water Vapor)

ALMA 



# Curves of atmospheric transmission: zenith + pwv variation

- ALMA ( $h \sim 5000\text{m}$ ):



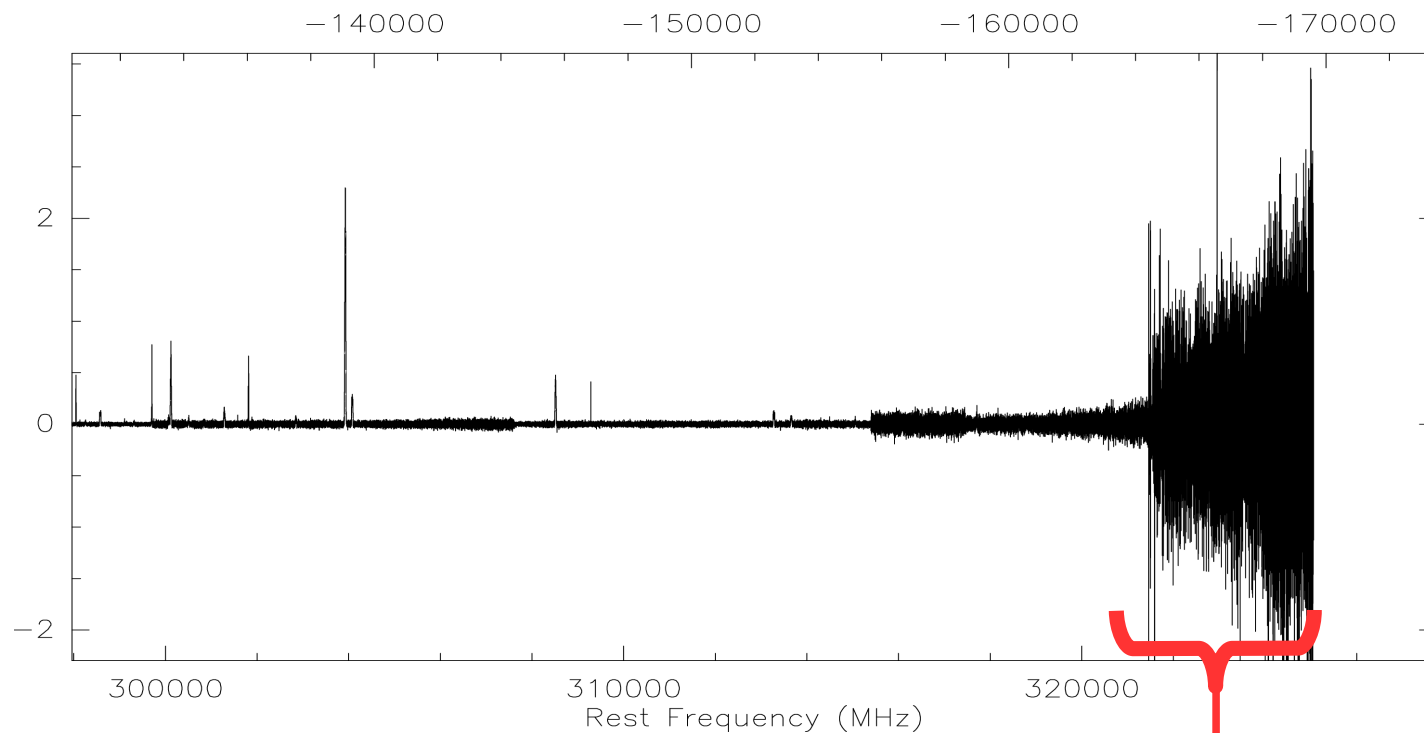
*Increase ZA = Increase air mass*

*Increase pwv*



## The effect of water vapor in our observations:

2;1 IKTAU SRVFINAL FTS 0:20-NOV-2013 R:12-OCT-2015  
RA: 03:53:28.84 DEC: 11:24:22.6 Eq 2000.0 Offs: +0.0 +0.0  
Unknown tau: 0.134 Tsys: 272. Time: 4.10E+03min El: 0.0  
N: 788636 IO: 28037.8 VO: 33.80 Dv: -0.2821 LSR  
FO: 207590.000 Df: 0.1954 Fi: 220095.538



*H<sub>2</sub>O (325.1 GHz)*

# Observational strategies

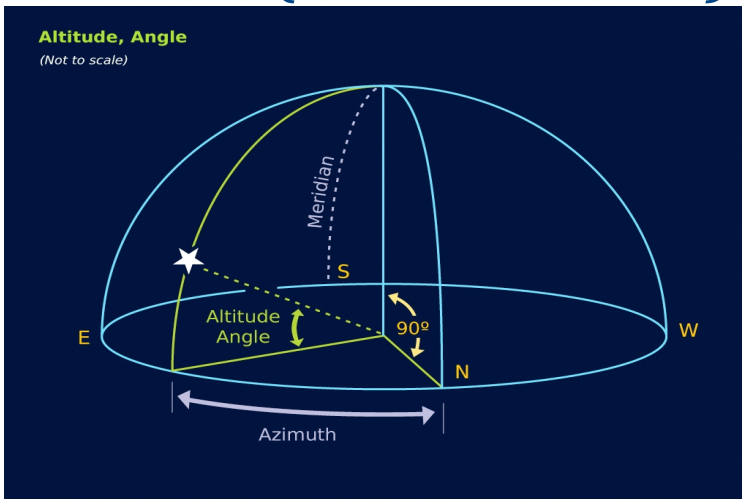
*Winter or summer?*



*Daytime or night?*



*Altitude (astronomical)?*



*Altitude (geographical)?*



## *Pause to summarise*

- The atmosphere causes absorption of incoming astronomical radiation*
- High contents of water vapor in the atmosphere are bad for mm and submm observations*
- High altitude and dry conditions improve the detection of astronomical signals*

*What else can we do?*

- Review of concepts that we will use:

Nyquist theorem:  $P = \Delta\nu kT$



Antenna  
temperature

Planck's law:  $B_\nu(T) = \frac{h\nu^3}{c^2} \frac{1}{e^{h\nu/kT} - 1}$

Radiation temperature:  $J(T) = \frac{c^2}{2k\nu^2} I = \frac{h\nu}{k} \frac{1}{e^{h\nu/kT} - 1}$

Radiative transfer:  $I_\nu(s) = I_\nu(0) e^{-\tau_\nu(0)} + \int_0^{\tau_\nu(0)} B_\nu(T(\tau)) e^{-\tau} d\tau$

Optical depth:  $\tau_\nu(s) = \int_{s_0}^s \kappa_\nu(s) ds$

## Calibration – single-dish: signal from empty sky

- **Goal:** obtain the net astronomical signal
- What are we really measuring? (Empty sky):

$$T_A(z) = T_{rx} + T_{atm} \eta_1 (1 - e^{-\tau_0 X(z)}) + T_{amb} (1 - \eta_1)$$

$T_A(z)$ : Antenna temperature at an elevation  $z$

$T_{rx}$ : receiver temperature

$T_{atm}$ : effective temperature of the atmosphere

$\eta_L$ : feed/forward efficiency ( $\sim 0.9$ )

$\tau_o$ : zenith optical depth

$X(z)$ : air mass at zenith distance  $z$

$T_{amb}$ : ambient temperature

# Calibration – single-dish: chopper wheel method ( $T_{rx}$ )

- **Goal:** obtain a Kelvin per Volt conversion factor

$$P_{out} \propto V_{out} = g(T_{input} + T_{rx}) \longleftrightarrow y = mx + b$$

$P_{out}$ ,  $V_{out}$ : power detector

$g$ : gain factor (slope)

$T_{input}$ : calibrated loads

- $T_{cold}$ :  $\sim 77K$  (He, N<sub>2</sub>)
- $T_{hot}$ : room temp.



$T_{rx}$ : receiver temperature  $\rightarrow T_{rx} = \frac{T_{hot} - YT_{cold}}{Y - 1}$

$$Y = \frac{V_{rx} + V_{hot}}{V_{rx} + V_{cold}}$$

$$g[V/K] = \frac{(V_{rx} + V_{hot}) - (V_{rx} + V_{cold})}{T_{hot} + T_{cold}}$$



## Calibration – single-dish: skydip

$\eta_L$ : forward efficiency (aka  $F_{\text{eff}} \sim 0.9$ ) is measured with a skydip

1) Obtain different pairs of  $(T_A, z)$  measures:



Observe at different zenith distances with almost equal weather conditions (same noise from other sources)

2) Least squares fitting of:  $T_A(z) = T_{\text{rx}} + T_{\text{atm}} \eta_l (1 - e^{-\tau_0 X(z)}) + T_{\text{amb}} (1 - \eta_l)$

*This is usually done by the observatory staff*



## *Calibration – single-dish: atmospheric effects*

*The atmosphere is a complex system, how do we simplify it?*



*SIMPLE MODEL:*

*Static, 1-D plane parallel, LTE, ideal gas*

# Calibration – single-dish: simple model of the atmosphere

Equation of state:  $P = \frac{\rho}{M} RT$

Scale height:  $H = \frac{RT}{\mu g} \approx 7998 \text{ m.}$

Hydrostatic equilibrium:  $\frac{dP}{dz} = -\rho g \longrightarrow P(z) = P_o e^{-z/H}$

Temperature gradient:  $\frac{dT}{dz} = -6.5 [K/km], (z < 11 \text{ km})$

LTE:  $\left\{ \begin{array}{l} 220 < T < 320 \text{ K} \\ 1020 < P < 0.0015 \text{ mb} \end{array} \right\} \longrightarrow \frac{N_u}{N_l} = \frac{g_u}{g_l} \exp(-\Delta E/kT)$   
Boltzmann's distribution

# Calibration – single-dish: Atmospheric Transmission Model

*Atmospheric transmission model (Cernicharo, 1985, IRAM report):*

*- Radiative transport in a plane parallel atmosphere:*

$$I_{\nu}(s) = I_{\nu}(0) e^{-\tau(0,s)} + \int_0^s S_{\nu}(s') e^{-\tau(s',s)} \kappa_{\nu}(s') ds' \quad (\kappa_{\nu})_{lu} = \frac{8\pi^3 N_{\nu}}{3hcQ} \left( e^{-E_l/kT} - e^{-E_u/kT} \right) \cdot |\langle u | \mu | l \rangle|^2 f(\nu, \nu_{l \rightarrow u})$$

*- Estimate the integrated opacity along the line of sight:*

*- Abundance distribution of all the species:  $N_i(s)$*

*- Spectroscopic parameters: transition probabilities...*

*- Species:  $H_2^{16}O$ ,  $H_2^{18}O$ ,  $H_2^{17}O$ , HDO,  $^{16}O_2$ ,  $^{16}O^{18}O$ ,  $^{16}O^{17}O$ ,  $^{16}O_3$ ,*

*$^{16}O^{16}O^{18}O$ ,  $^{16}O^{18}O^{16}O$ ,  $^{16}O^{16}O^{17}O$ ,  $^{16}O^{17}O^{16}O$ ,  $N_2O$ , CO,  $SO_2$ ,  $H_2S$ ,  $NO_2$*

*- Integrate for all the spectrum (all frequencies)*

## Line profile:

Natural broadening: negligible ( $\sim 10^{-6}$  Hz)

Pressure broadening: dominates at  $h < 50$  km. ( $\sim 2.5$  MHz/mbar)

Van Vleck-Weisskopf profile:

Collisional broadening

Approximation:  $t_{col} \ll 1/A_{ul}$

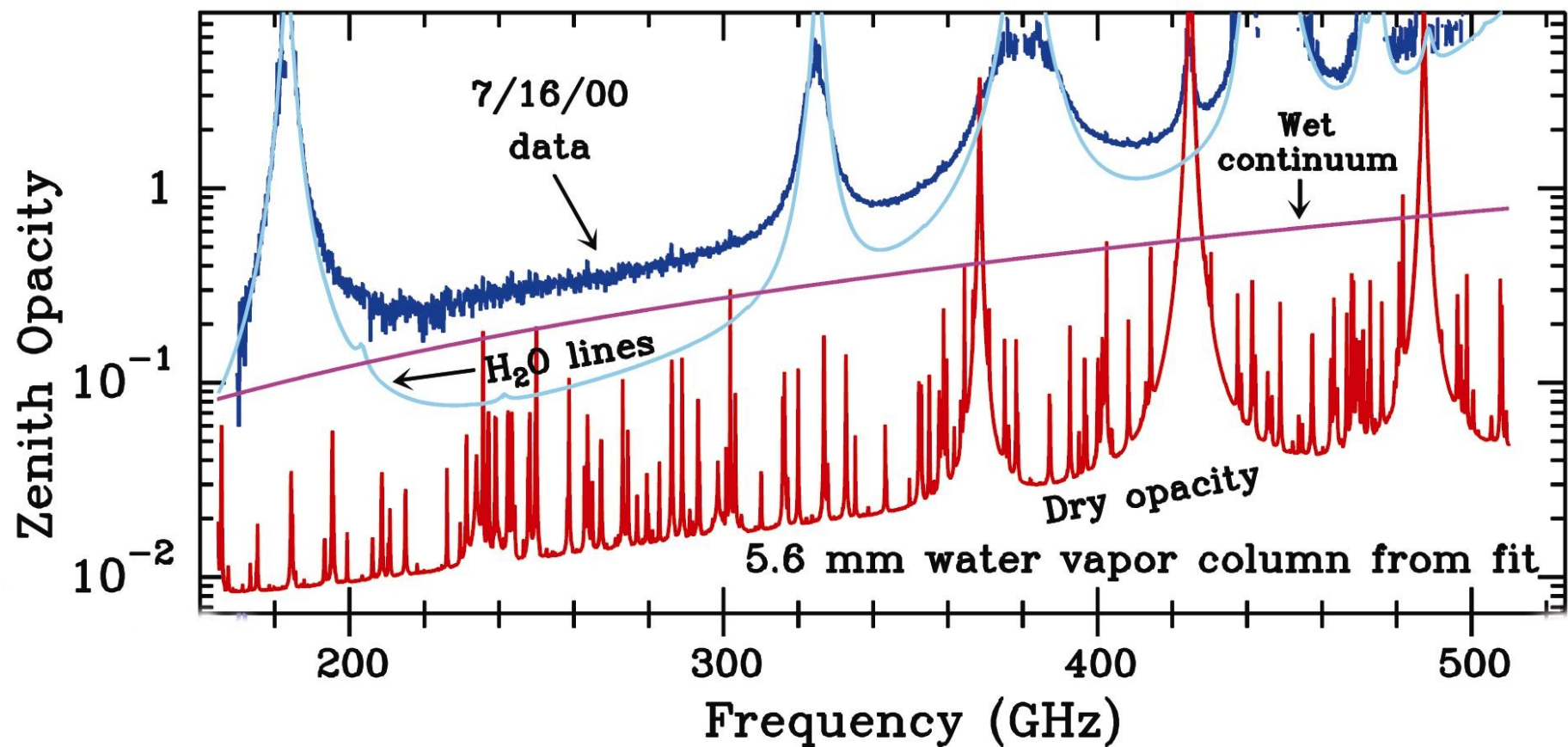
$$f_{VW}(\nu, \nu_{l \rightarrow u}) = \frac{\nu \Delta\nu}{\pi \nu_{l \rightarrow u}} \left( \frac{1}{(\Delta\nu)^2 + (\nu - \nu_{l \rightarrow u})^2} + \frac{1}{(\Delta\nu)^2 + (\nu + \nu_{l \rightarrow u})^2} \right),$$

Doppler broadening: low pressure (density)

Gaussian profile:

$$f_D(\nu, \nu_{l \rightarrow u}) = \frac{1}{\Delta\nu_D} \left( \frac{\ln 2}{\pi} \right)^{\frac{1}{2}} \exp \left[ - \left( \frac{\nu - \nu_{l \rightarrow u}}{\Delta\nu_D} \right)^2 \ln 2 \right]$$

## Continuum-like absorption:



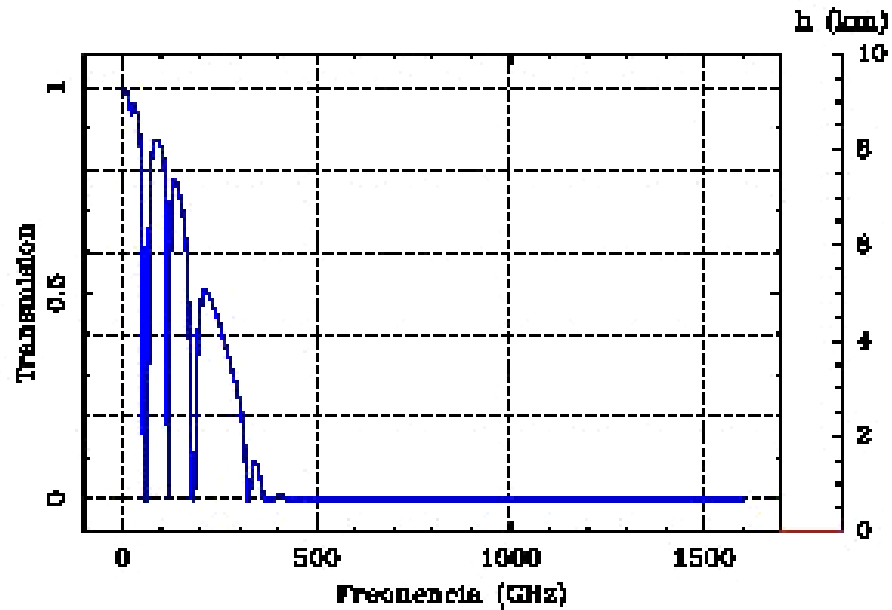
*Empirical law proportional to:*

1) *(water vapor partial pressure)<sup>2</sup>*

2) *product of water vapor and foreign-gas partial pressure*

# Calibration – single-dish: ATM results

## Example: Variation with altitude

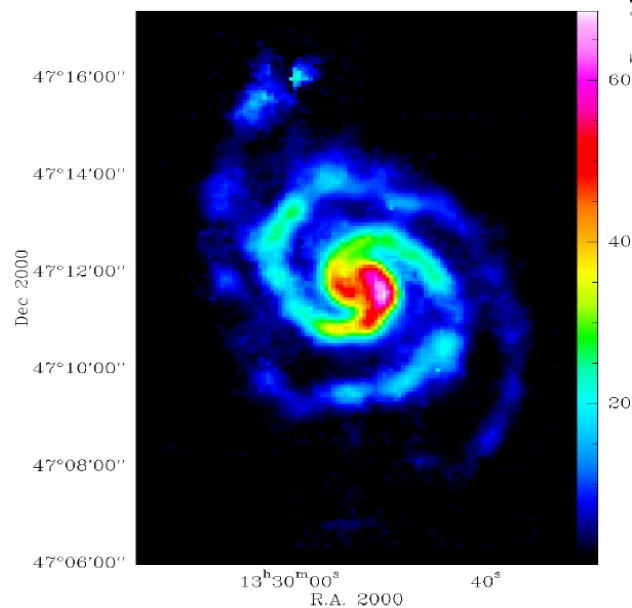
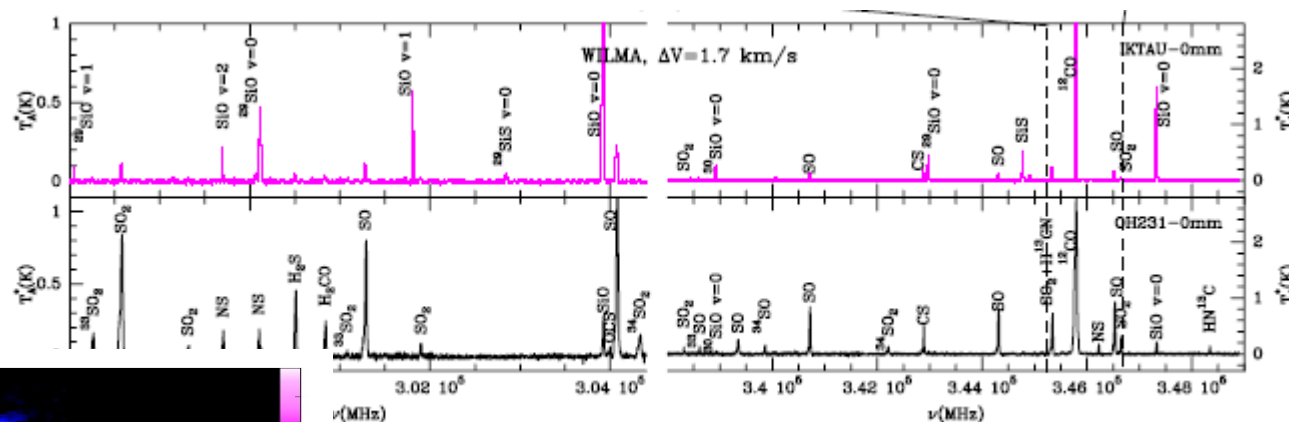




# Calibration – single-dish: results

- Atmospheric calibration procedure is done automatically (chopper wheel method to obtain counts for: SKY-HOT LOAD-COLD LOAD) you only need to include this procedure in your observing run

- Result:



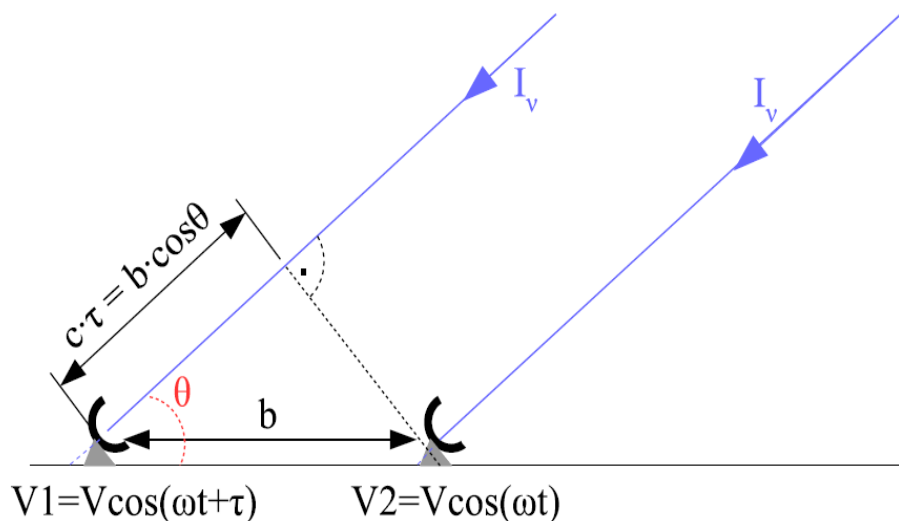
*Astronomical data  
ready for the  
analysis*



# Calibration – interferometry: phase delay

- We have seen that fluctuating atmosphere causes anomalous refraction or “radio-seeing” → 

- Refractive effects cause phase delays when using long baseline interferometry: tropospheric variability of  $H_2O$



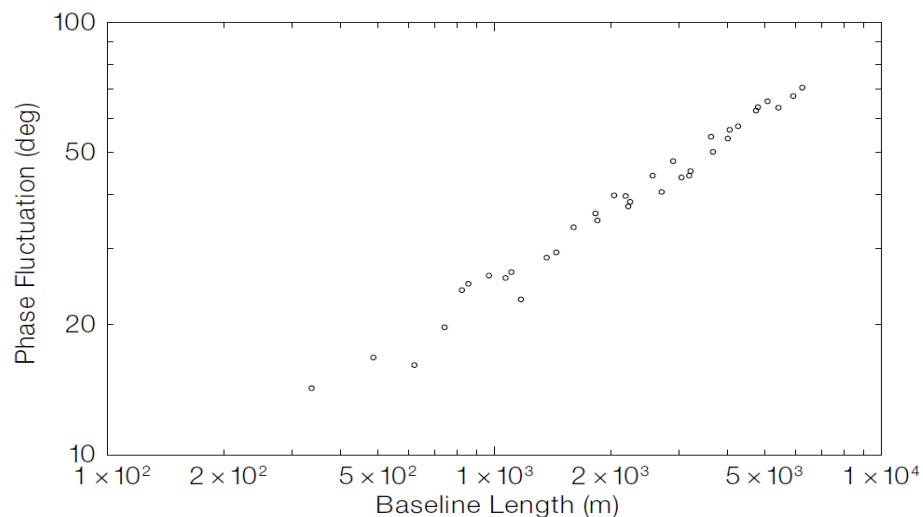
Alma goal:  $\sim 0.001''$  angular resolution

Alma baselines: up to  $\sim 10$  km.

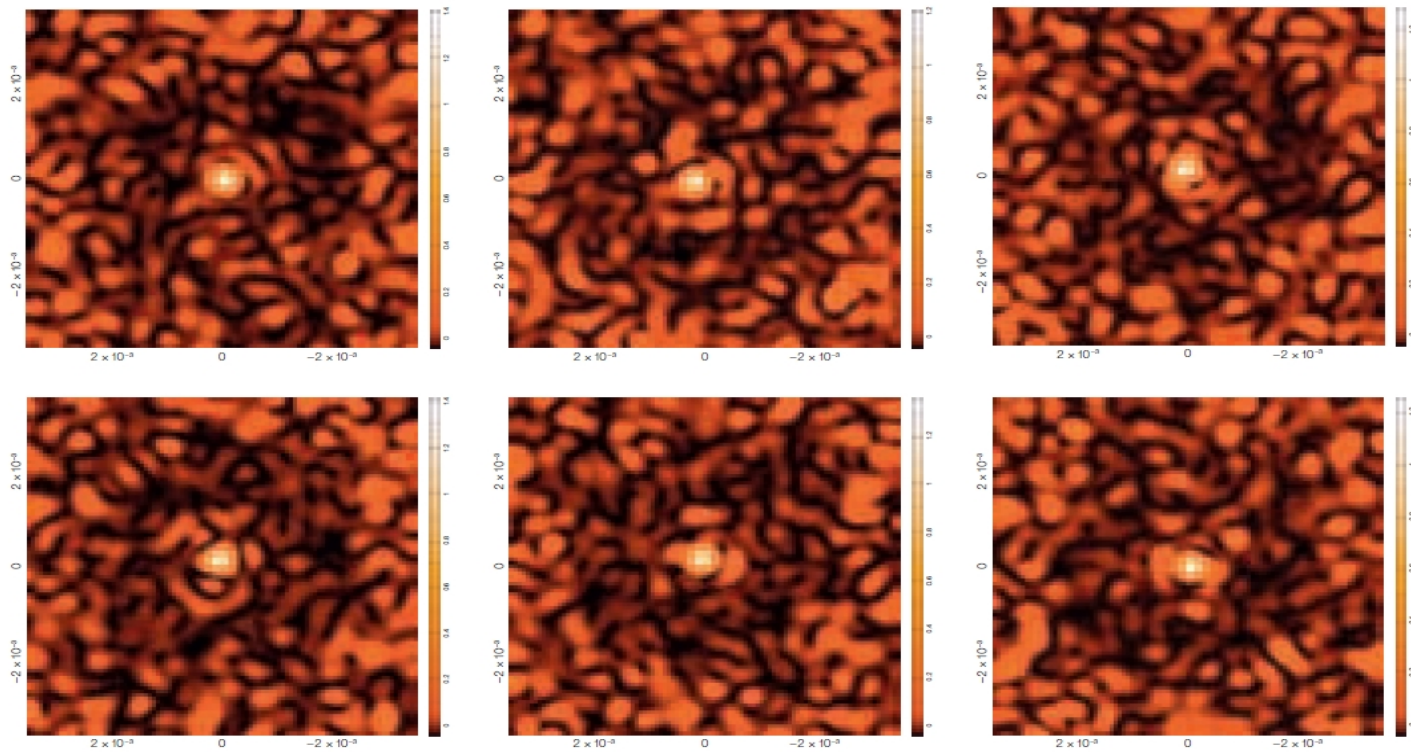
1mm of pwv is equivalent to  
7mm pathlength delay

ALMA shortest wavelength is  
 $\sim 0.3$ mm (delay  $\sim 20\lambda$ )

# Calibration – interferometry: phase delay effects



*Phase fluctuations measured with the Very Large Array at 22 GHz as a function of the baseline*



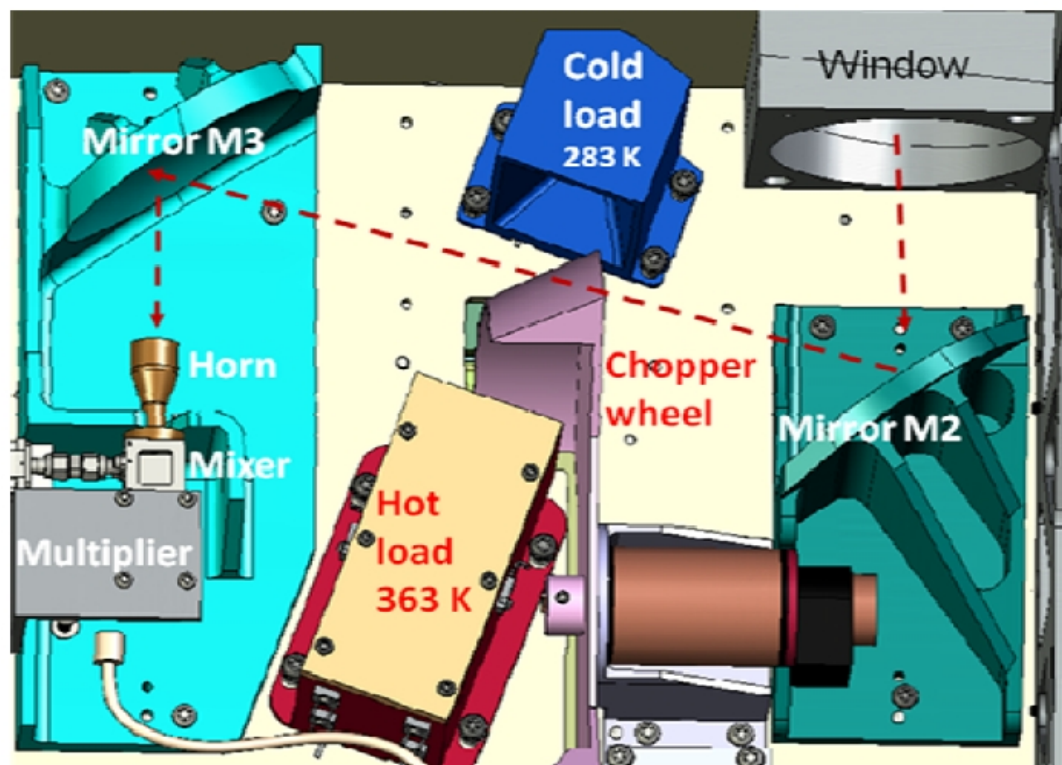
*Simulated images of a 2 Jy point-source observed with ALMA with the presence of uncorrected phase fluctuations*

## - Solution:

1) *Fast switching: observe well-known source*

2) *Radiometers: predict pathlength variations due to*

*H<sub>2</sub>O vapor using radiometers+ATM and correct the delay*



*Scheme of an ALMA Radiometer operating at 183 GHz (p-H<sub>2</sub>O 3,1,3 - 2,2,0 line)*

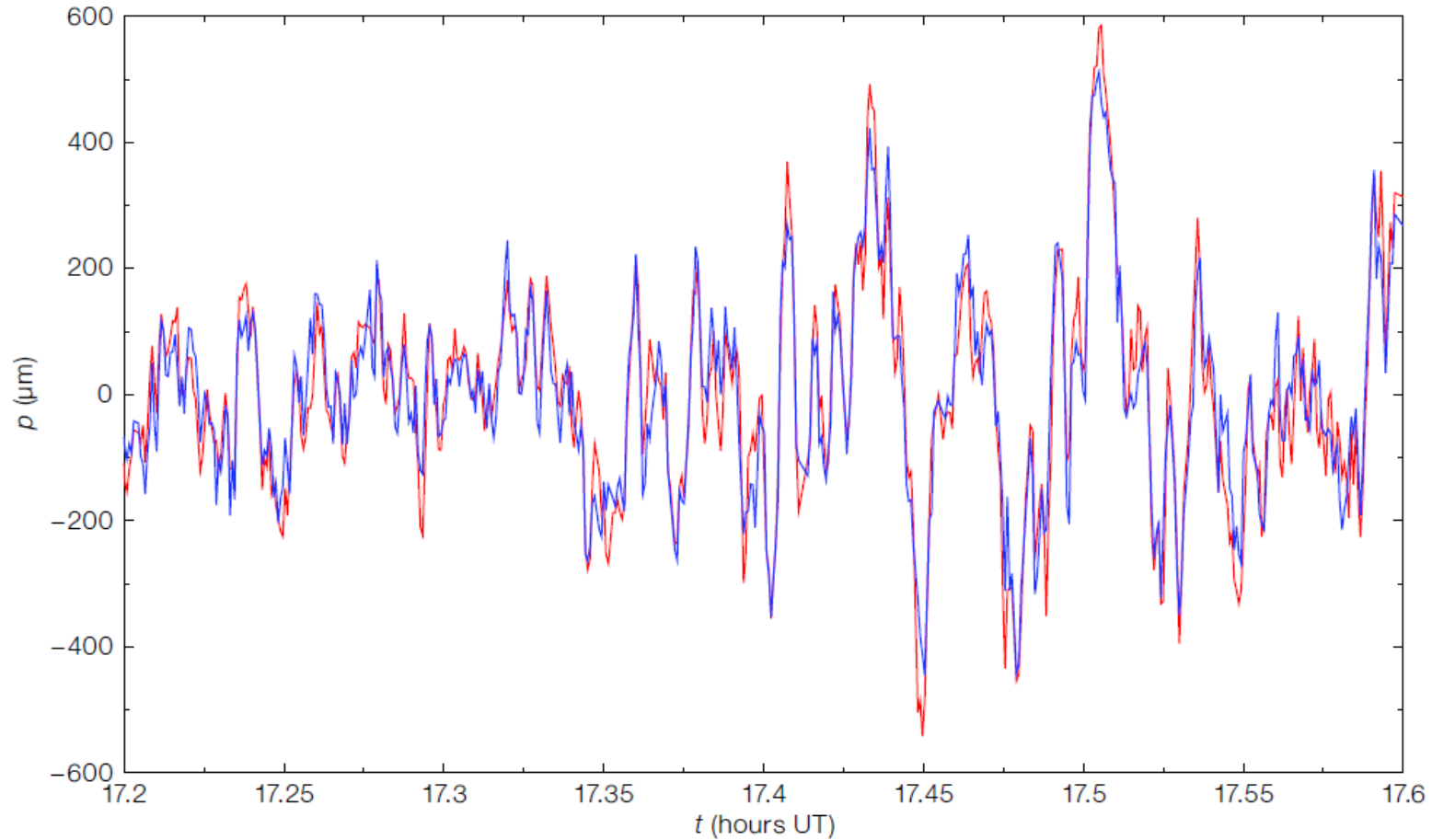
*The beam enters through the window, and goes to the horn after successive reflections in M2 and M3.*

*The chopper wheel deflects the beam following the sequence:  
Sky-Cold-Sky-Hot*



# Calibration – interferometry: radiometers

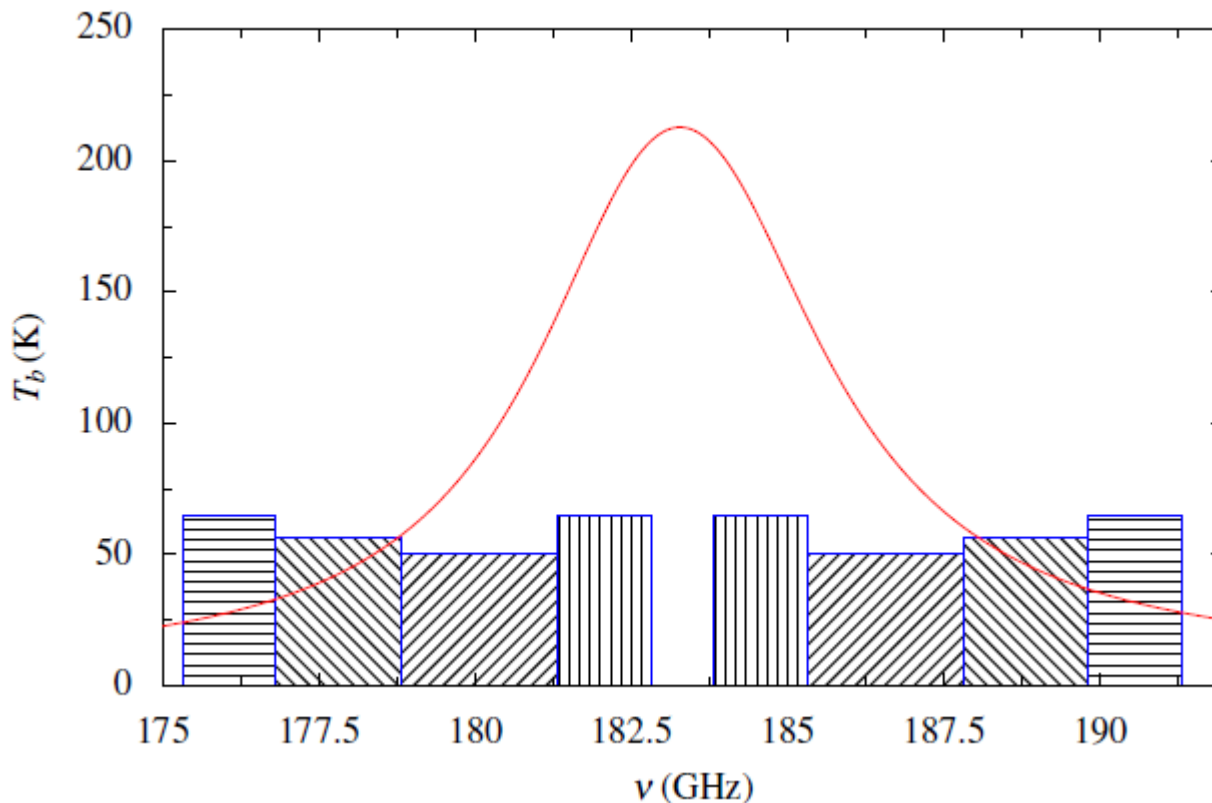
- *Performance of an ALMA radiometer tested at the SMA:*



**Red curve:** *fluctuating atmospheric path measured by the interferometer*  
**Blue curve:** *estimated by the radiometer*

## Calibration – interferometry: ALMA radiometers

- Each 12 m antenna has its own radiometer which measures the  $T_b$  of the sky on timescales  $\sim 1$  s.
- On timescales longer than 3 min.: phase calibrators
- These data are stored for phase-correction (Nikolic et al. 2013)



**Red curve:** brightness temperature model of the 183 GHz line of water with 1 mm of pwv.

The eight channels of the radiometer are shown

# BASIC BIBLIOGRAPHY

- *“Tools of Radio Astronomy” T.L. Wilson, K. Rohlfs, S. Hüttemesiter. A&A Library, Springer 5th Ed. 2009*
- *Carter, M., Lazareff, B., Maier, D., et al. 2012, A&A, 538, A89*
- *Nikolic, B., Bolton, R.C., Graves, et al. 2013, A&A, 552, A104*
- *Pardo, J.R., Cernicharo, J., & Serabyn, E. 2001, IEEE Transactions on Antennas and Propagation, 49, 1683*
- *Ulich, B.L. & Haas, R.W. 1976, ApJ, 30, 247*
- *Check EMIR for astronomers Wiki (internal reports):*
  - <http://www.iram.es/IRAMES/mainWiki/EmirforAstronomers>*
  - <http://www.iram.es/IRAMES/mainWiki/CalibrationPapers>*
- *Play with it:*
  - <https://almascience.eso.org/about-alma/atmosphere-model>*
  - <https://www.mrao.cam.ac.uk/~bn204/alma/atmomodel.html>*



# Additional slide: Calibration method equations

- Loads are considered black bodies and their physical temperatures are equivalent to their

Rayleigh-Jeans radiation temperature ( $h\nu \ll kT$ ):  $T_B = 77\text{ K} \longrightarrow J_\nu(T_B, 345\text{ GHz}) = 70\text{ K}$

This is equivalent to a 10% higher  $T_{rx}$   $\longrightarrow$  acceptable approximation

- How to convert counts into antenna temperature (when measuring the sky):

$$\frac{T_{hot} - T_A^{sky}}{C_{hot} - C_{atm}} = \frac{T_{hot} - T_{cold}}{C_{hot} - C_{cold}}$$

with

$$T_A^{sky} = \eta_l T_{sky} + (1 - \eta_l) T_{cab}$$

$$T_{cab} = 0.8 T_{hot} + 0.2 T_{amb} \quad (\text{IRAM-30m})$$

- $T_{sky}$  and  $\tau$  are calculated by fitting the emission of both receiver sidebands with ATM (pwv)

- Spectral line calibration: difference of counts between the source and the blank sky (off

position) is related to the difference of counts between the hot load and the blank sky:

$$T_A^* = T_{cal} \frac{C_{source} - C_{atm}}{C_{hot} - C_{atm}} = \frac{1 + G_i}{\eta_l \exp(-\tau_{sig} A)} (T_{hot} - T_A^{sky})$$

$A$ : airmass =  $1/\sin(\text{elev.})$   
 $G_i$ : gain ratio of the two sidebands =  $G_{ima}/G_{sig}$

## Additional slide: Calibration method equations

- Counts for the hot load:

$$C_{hot} = g [G_{sig} J(\nu_{sig}, T_{hot}) + G_{ima} J(\nu_{sig}, T_{hot}) + T_{rx}]$$

- Counts for the blank sky:

$$C_{atm} = g (G_{sig} [\eta_l J(\nu_{sig}, T_{sky}) + (1 - \eta_l) J(\nu_{sig}, T_{cab})] + G_{ima} [\eta_l J(\nu_{ima}, T_{sky}) + (1 - \eta_l) J(\nu_{ima}, T_{cab})] T_{rx})$$

- For each sideband:

$$J(\nu, T_{sky}) = J(\nu, T_{atm}) (1 - \exp(-\tau A)) + J(\nu, T_{bg}) \exp(-\tau A)$$

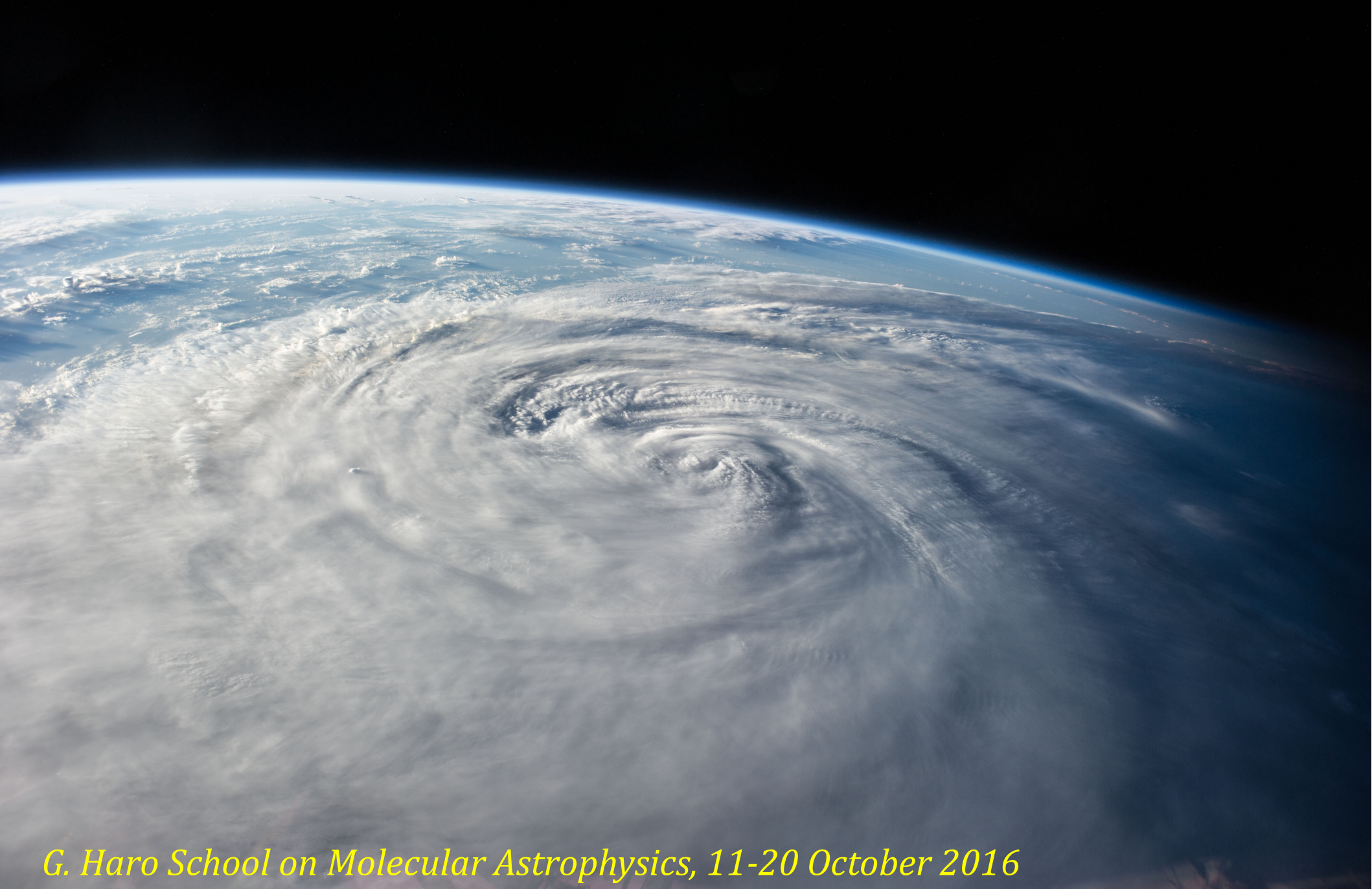
where we assumed:

$$J(\nu_{sig}, T) = J(\nu_{ima}, T) = J(T)$$

- Difference of counts between source and blank sky:

$$C_{source} - C_{atm} = g G_{sig} \eta_l \exp(-\tau_{sig} A) T_A^*$$

**See “Calibration of spectral line data at the IRAM-30m radio telescope” C. Kramer, 1997 (Bibliography: Calibration Papers).**



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