

# Models for (spiral) galaxies

- Spectra
- Brightness Profiles
- Colors
- Spectral Indices

**Stellar  
Populations  
Indicators:  
Synthesis  
Models**

Averaged  
along the  
evolutionary  
history  
Properties

**Constraints  
Chemical  
Evolution  
Models**

- **HII regions, emission lines Abundances**
- **H $\alpha$  fluxes : (recent) Star formation rate**
- **Atomic and molecular gas densities**

Present time

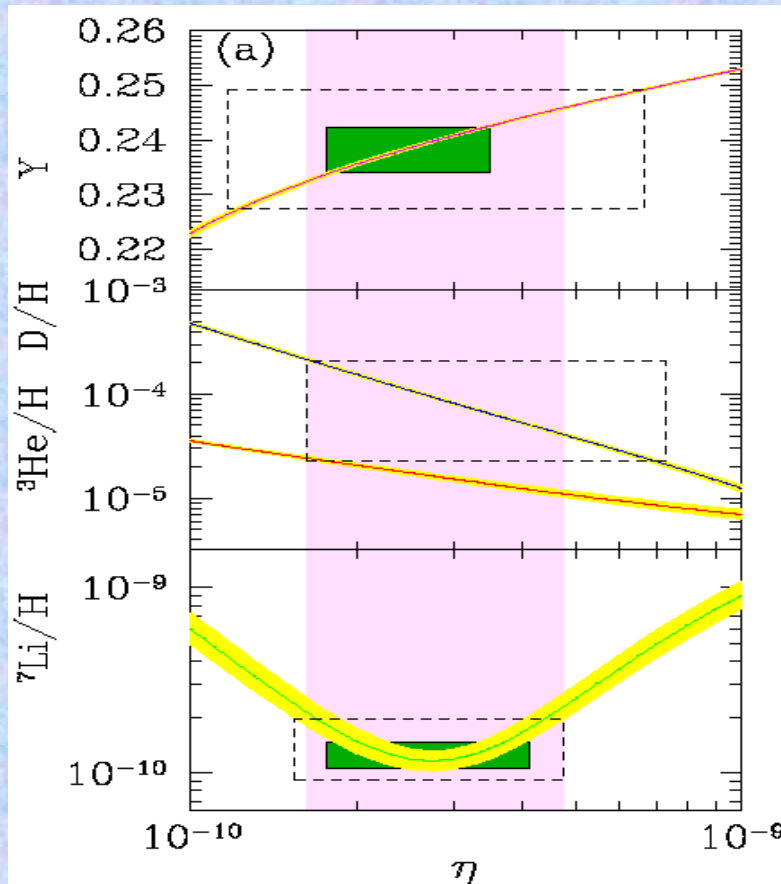
GH14-IFS techniques and analysis

# CHEMICAL EVOLUTION MODELS FOR SPIRAL AND IRREGULAR GALAXIES

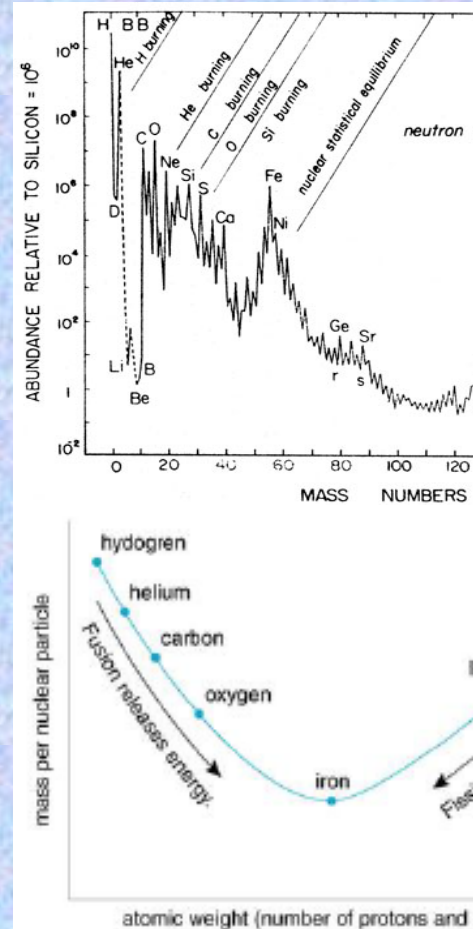
**Mercedes Mollá**  
**CIEMAT, Madrid (Spain)**

GH14-IFS techniques and analysis

# Primordial & Solar abundances



Before the creation of stars. There are H, He and traces of Li or Be from Big Bang



<b>H</b>	<b>0.735</b>
<b>He</b>	<b>0.248</b>
<b>D</b>	<b>0.48e-4</b>
<b>He3</b>	<b>0.29e-4</b>
<b>C</b>	<b>0.292e-2</b>
<b>O</b>	<b>0.795e-2</b>
<b>N</b>	<b>0.856e-3</b>
<b>Ne</b>	<b>0.177e-2</b>
<b>Mg</b>	<b>0.671e-3</b>
<b>Si</b>	<b>0.730e-3</b>
<b>S</b>	<b>0.503e-3</b>
<b>Ca</b>	<b>0.674e-4</b>
<b>Fe</b>	<b>0.130e-2</b>

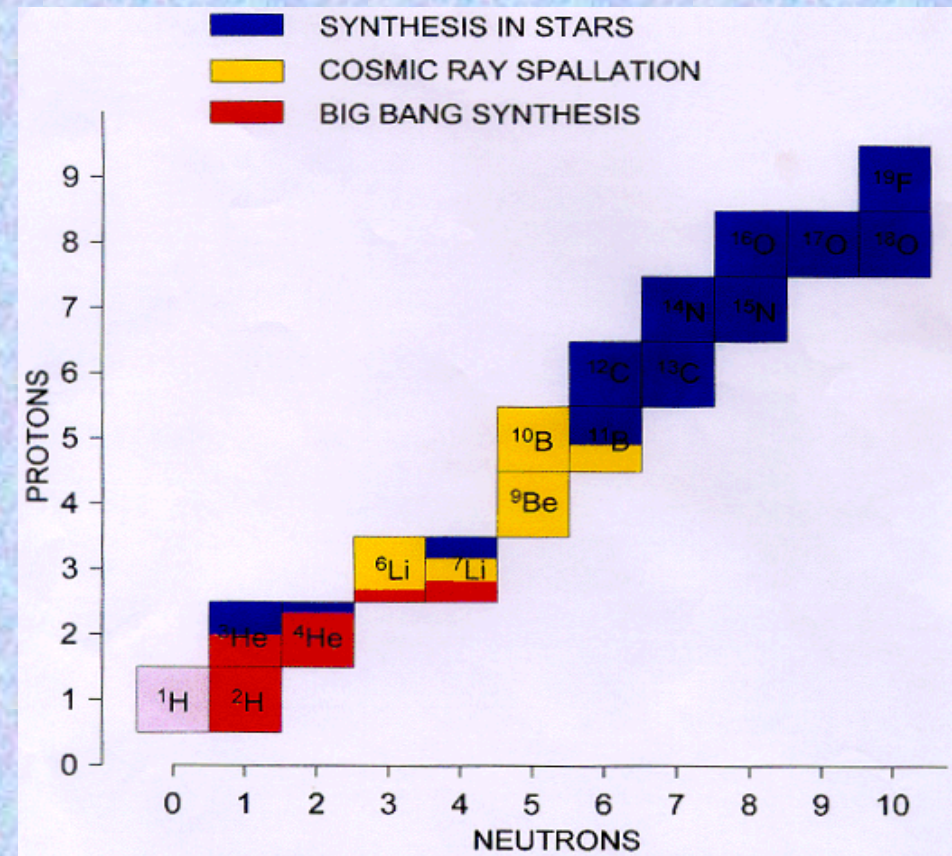
• Associated with magic numbers

• Separation among pics: slow or rapid addition of n

GH14-IFS techniques and analysis



- ❖ Chemical elements appear in the Universe as a consequence of three processes of elements production:
  - Big Bang Nucleosynthesis
  - Fragmentation processes (Cosmic Rays)
  - **Stellar Nucleosynthesis**
- ❖ H will disappear at the same time that metals (elements heavier than He) increase their abundances.
- ❖ The gas composition is defined by:  $X+Y+Z=1$ ,  $X=H$ ,  $Y=He$ ,  $Z=metals$
- ❖ Primordial abundances:  $X=0.76$ ,  $Y=0.24$ ,  $Z=0$ ,
- ❖ Solar abundances:  $X=0.70$ ,  $Y=0.28$ ,  $Z=0.02$ .





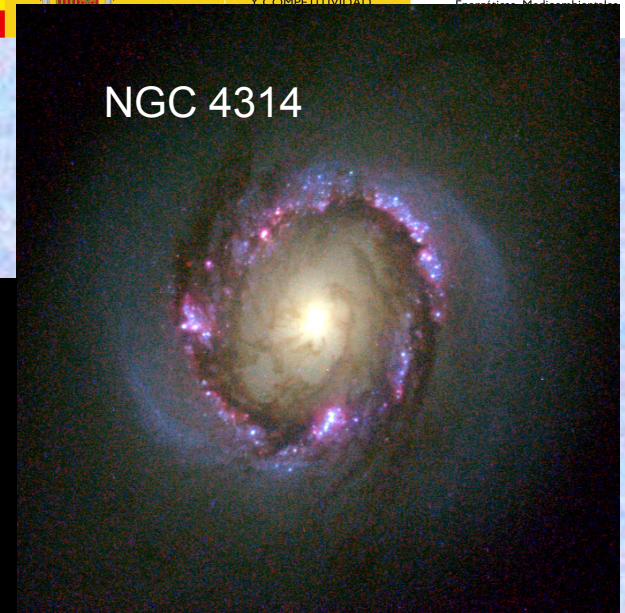
Burbidge, Burbidge & Hoyle 1957

## Overview of nucleosynthesis mechanisms

- H-burning
- He-burning
- C-burning
- O-burning
- Ne-burning
- Si-burning
- NSE
- s-process
- r-process
- p-process
- $\gamma$ -process
- $\nu$ -process
- spallation reactions

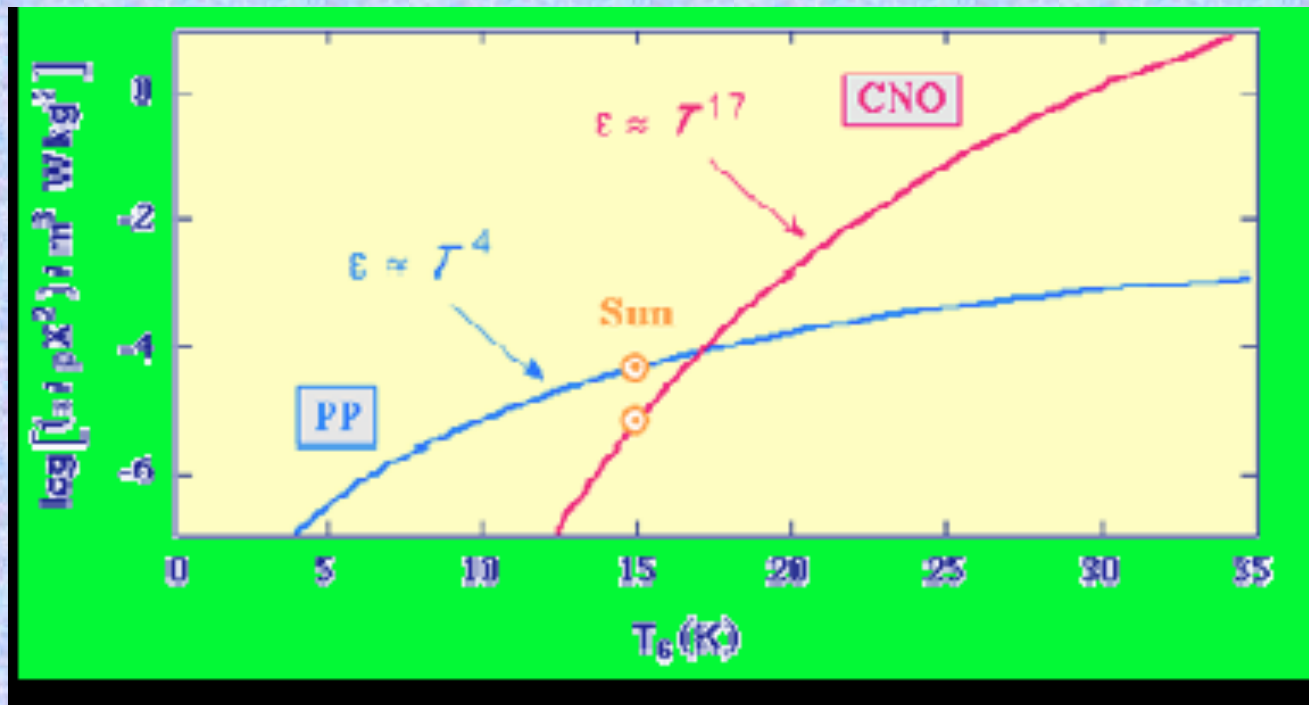
**Some of these mechanisms can work  
in hydrostatic or hydrodynamic regimes**

NGC 4314



**New stars forming: HII  
regions**

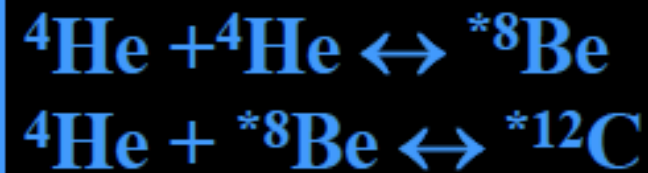
# Production of nuclei in stars: Stellar yields



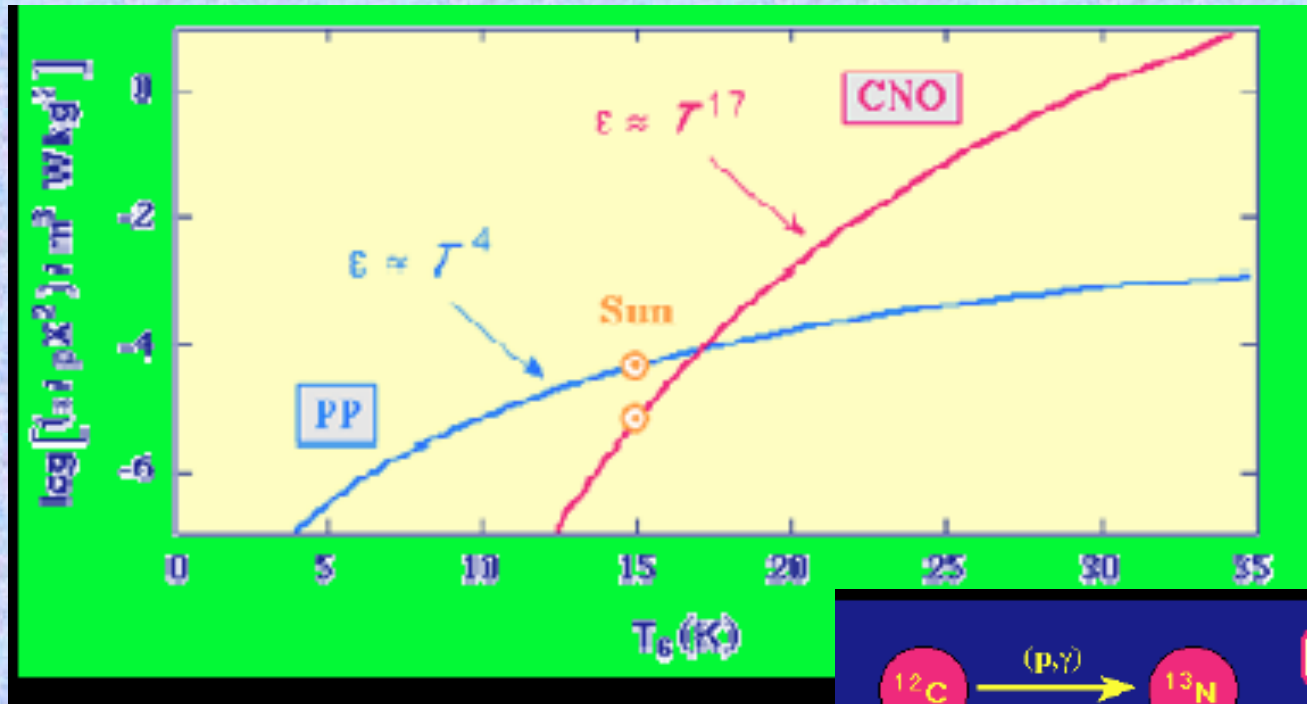
Low mass stars:  $m < 4M_{\text{sun}}$

Burning of H

Burning of  $4\text{He}$



# Production of nuclei in stars: Stellar yields



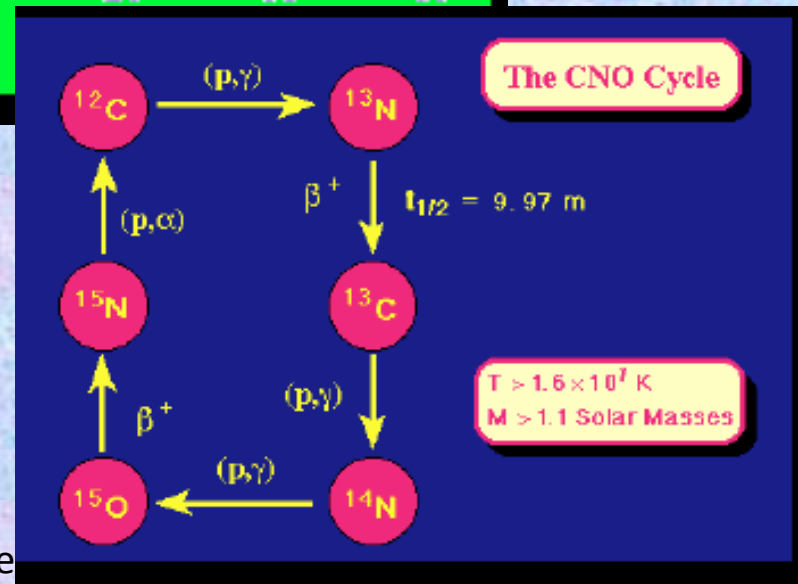
Intermediate mass stars:

$4 M_{\text{sun}} < m < 8 M_{\text{sun}}$

Burning of  $^{12}\text{C}$

CNO cycle

Production of N (primary) GH14-IFS technique

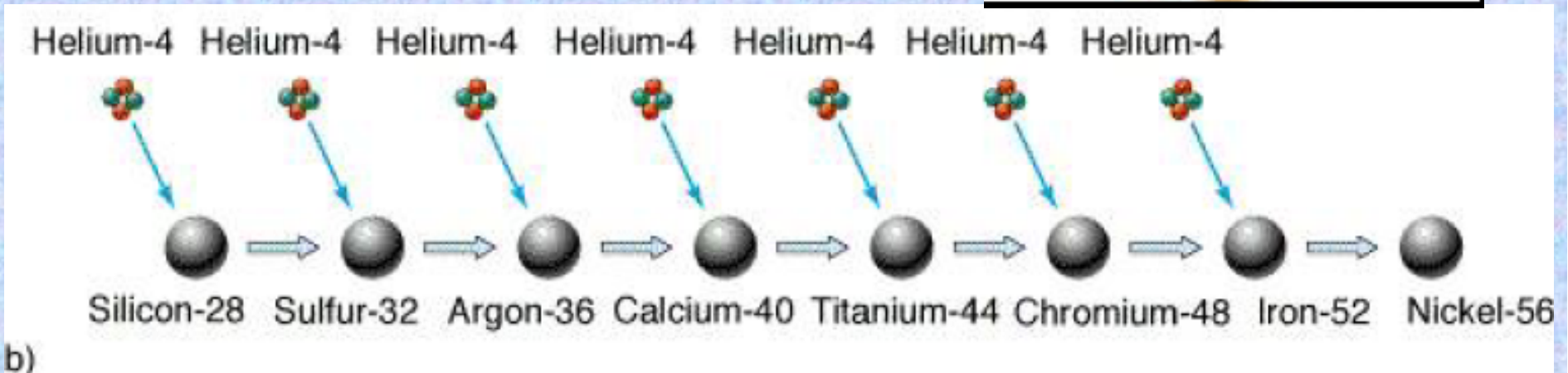
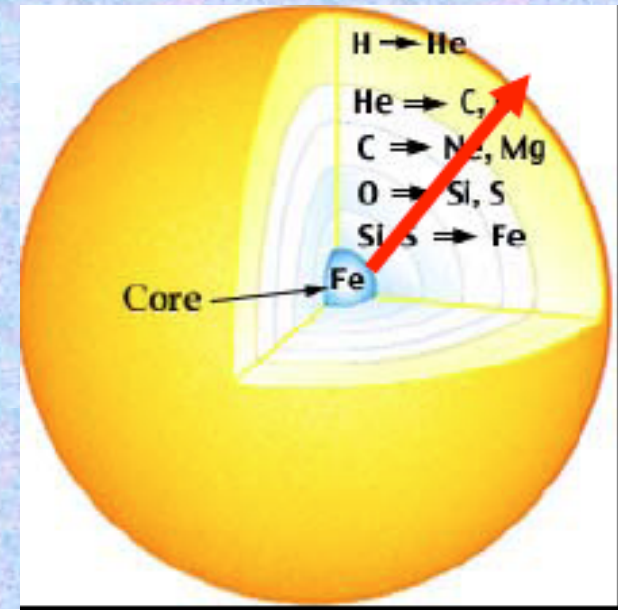
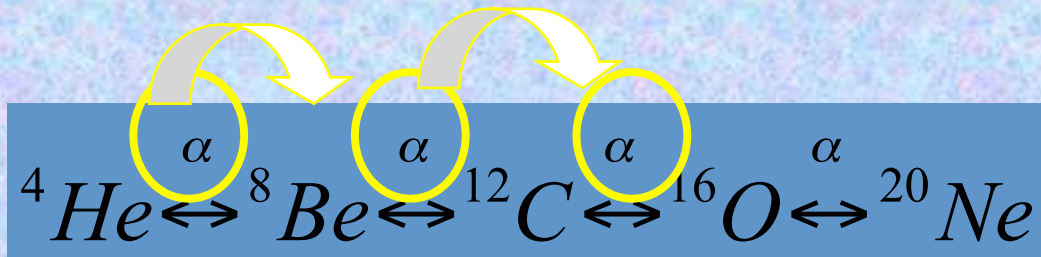




# Production of nuclei in stars: Stellar yields

Massive stars:  $m > 8M_{\text{sun}}$

Production of elements by  $\alpha$ -process

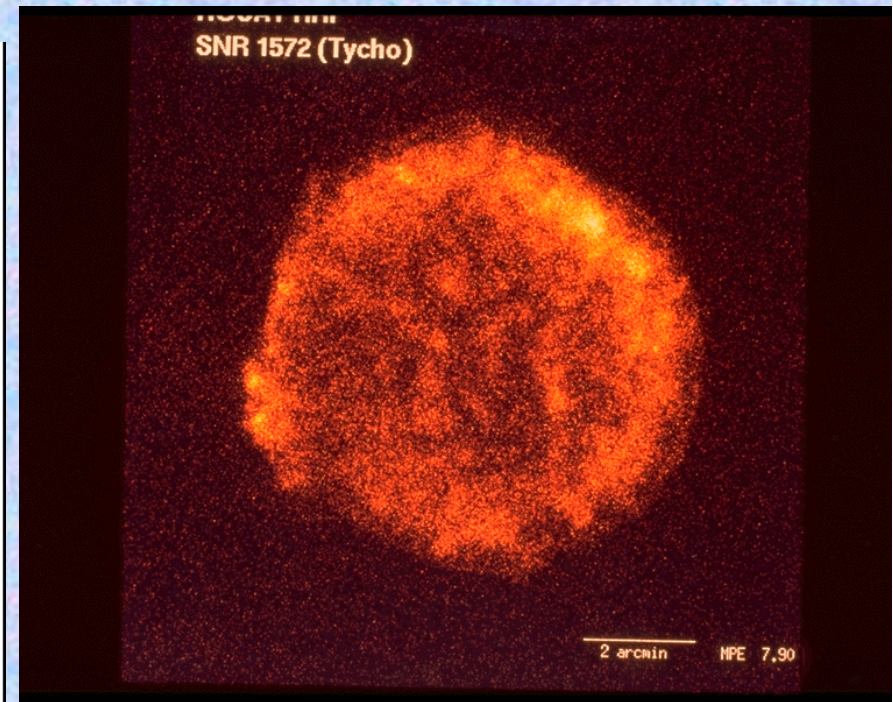
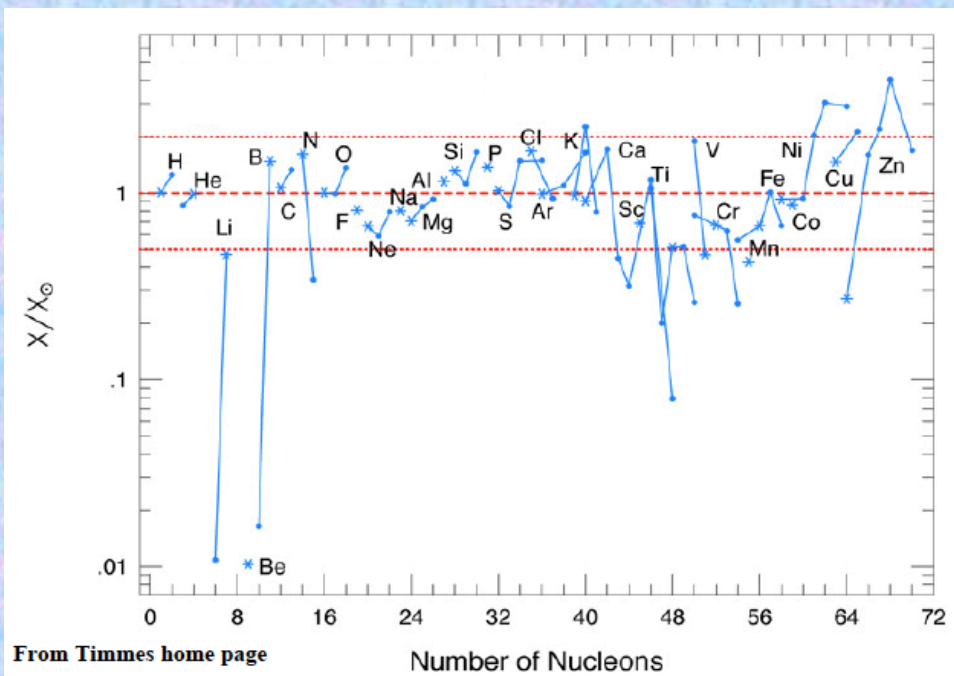


Several elements until Fe form in a onion-skin structure with the Fe in the center  
GH14-IFS techniques and analysis

# Nucleosynthesis in gravitational SN

It is determined by:

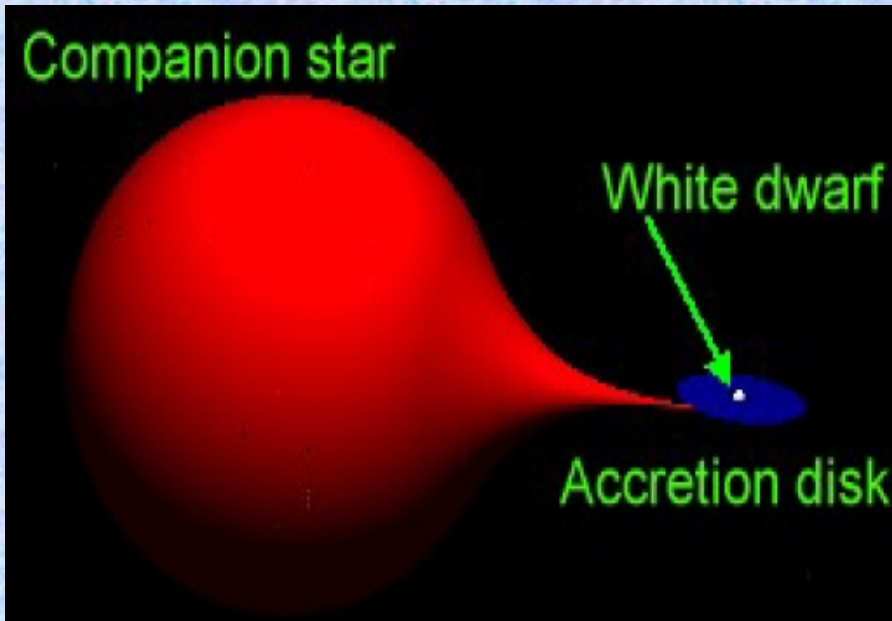
- Nucleosynthesis during the presupernova evolution
- Explosive burning induced by the shock wave



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# Supernovae type Ia: binary systems



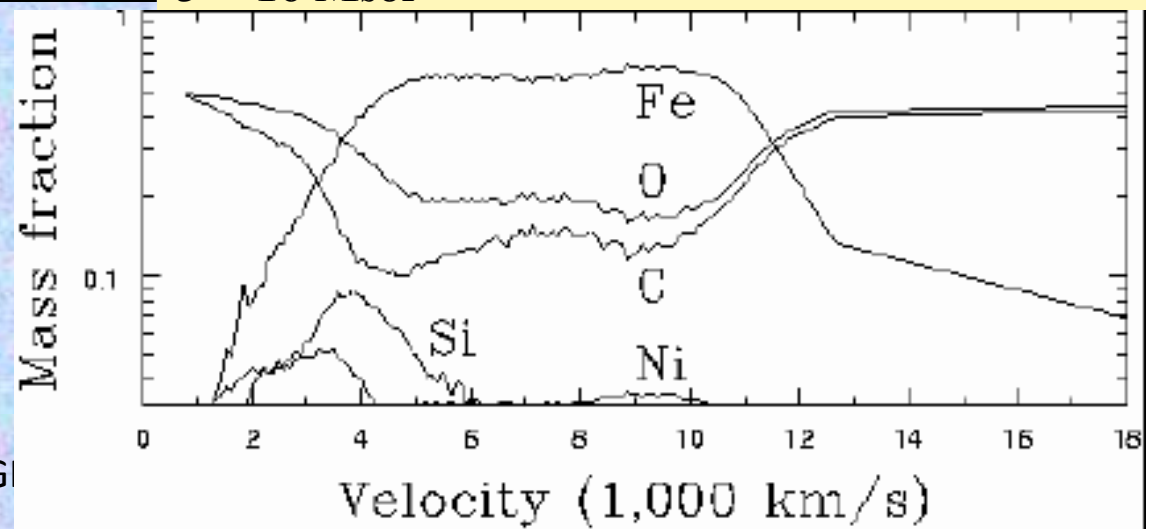
- The SNIa form in a binary system in which the evolved component is a CO-WD accreting the companion star mass. This way a nuclear deflagration is produced.

- The deflagration front propagates by electrons moving at subsonic velocities. The wave preceding the wave front ejects the star without any rest

- The masses of the binary system are between 3 -- 16 Msol

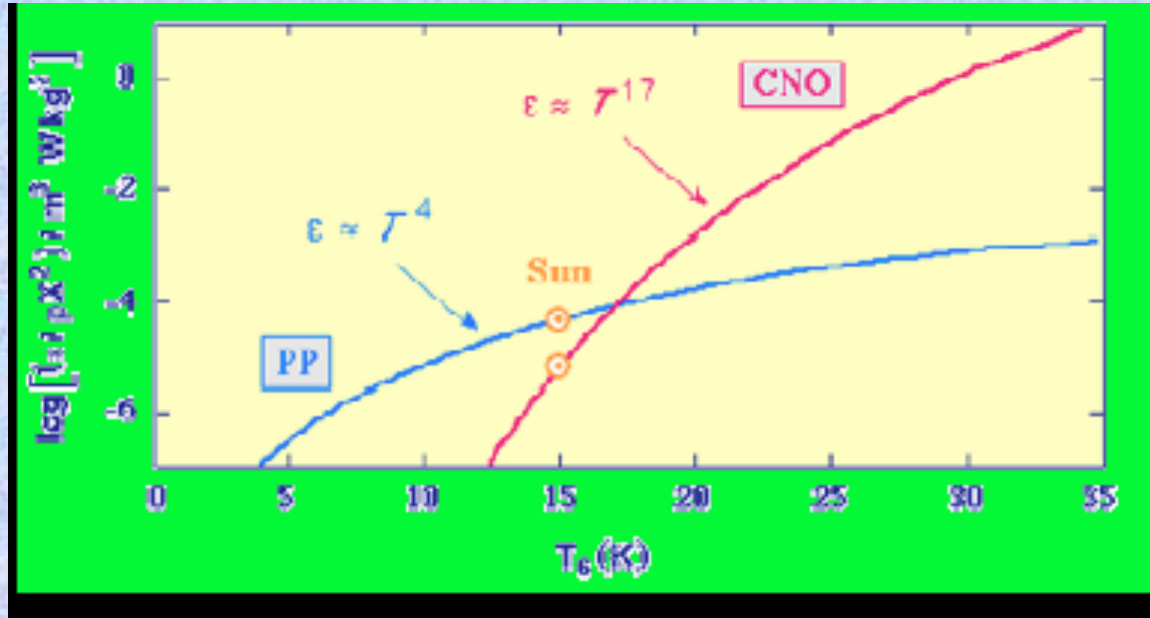
- Merging of two CO WD
- He star accreting WD
- H (Red giant) accreting WD

■ The most important of these SNIa is the large quantity of Fe produced, they eject 0.6 Mo





# Production of nuclei in stars: Stellar yields



- Cycle pp: low mass stars  $m < 4M_{\odot}$
- Cycle pp+CNO: intermediate mass stars  $4M_{\odot} < m < 8M_{\odot}$
- Cycle CNO+ capture  $\alpha$ : massive stars  $m > 8M_{\odot}$

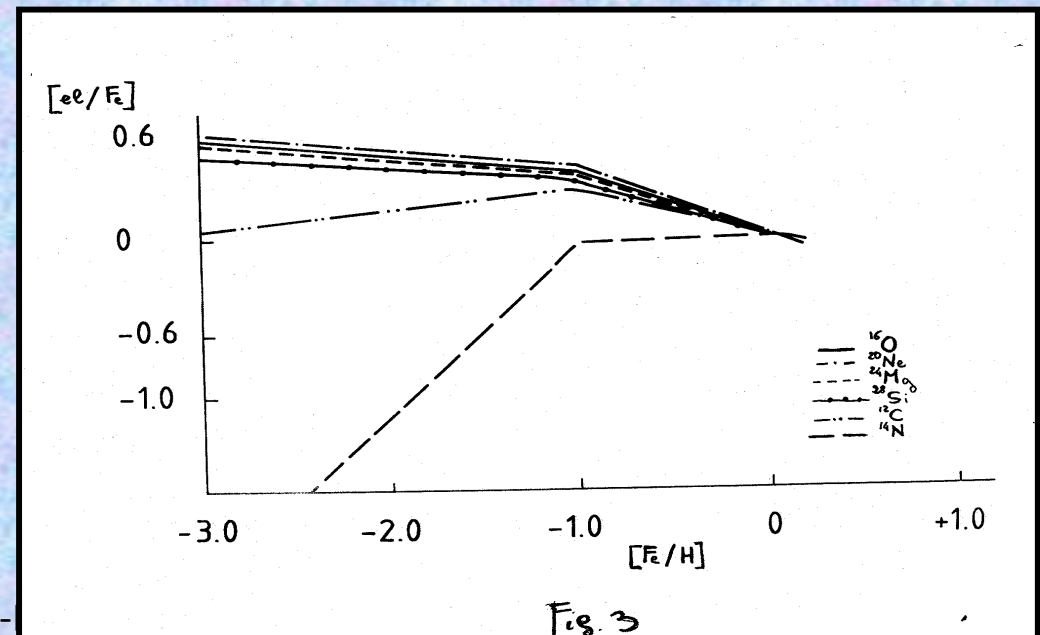
- Low mass stars produce He and C12
- Intermediate mass stars produce C,N and O
- Massive stars produce O,Ne,Mg,S.,N, and Fe
- Binary Systems, SNIa Fe

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Cycle pp: low mass stars  $m < 4M_{\odot}$   
 Cycle pp+CNO: intermediate mass stars  $4M_{\odot} < m < 8M_{\odot}$   
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- Low mass stars produce He and C12
- Intermediate mass stars produce C,N and O
- Massive stars produce O,Ne,Mg,S...,N, and Fe
- Binary Systems, SNIa Fe

The meanlifetimes of  
different stars explain the  
relative abundances of  
elements



GH14-

Fig. 3

Cycle pp: low mass stars  $m < 4M_{\odot}$

Cycle pp+CNO: intermediate mass stars  $4M_{\odot} < m < 8M_{\odot}$

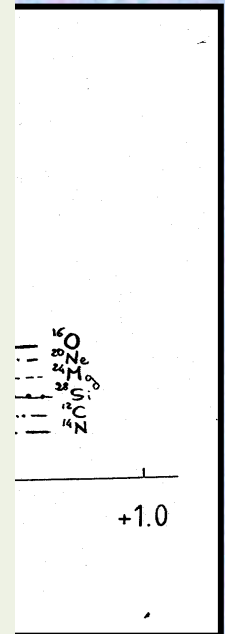
Cycle

**EACH ELEMENT APPEARS AT  
A DIFFERENT TIME FOLLOWING  
THE MASS OF THE STAR WHICH  
PRODUCES IT**

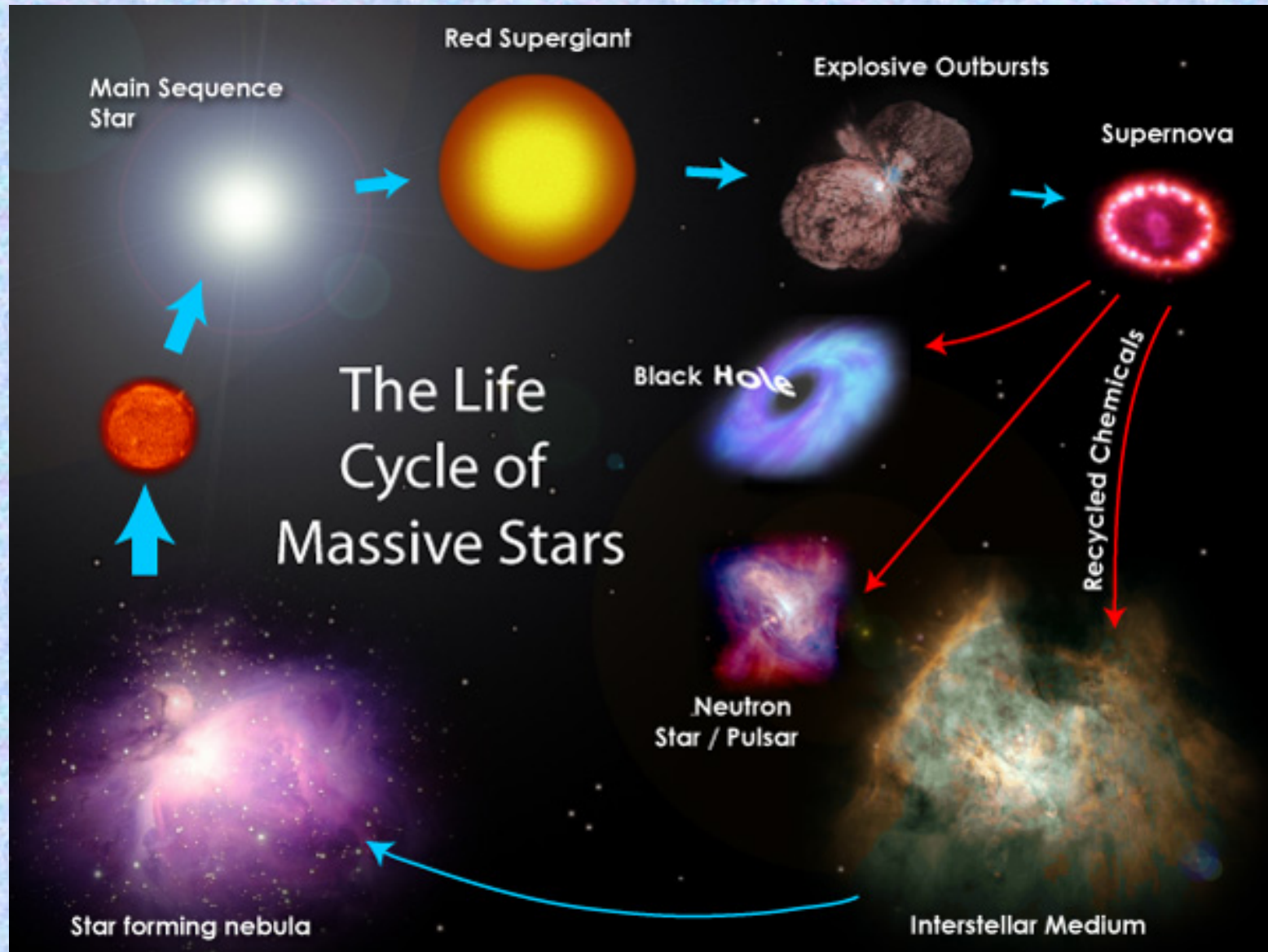
- Low
- Inte
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**RELATIVE ABUNDANCES GIVE  
INFORMATION ABOUT DIFFERENT  
STELLAR MASS RANGE CREATING  
ELEMENTS**







# Galaxies Chemical Evolution Aim

Chemical elements are created and then:

- Ejected and diluted in the interstellar medium
- Incorporated to the successive generations of stars

**Elemental abundances give clues about star formation: when, how, with which rate stars form**

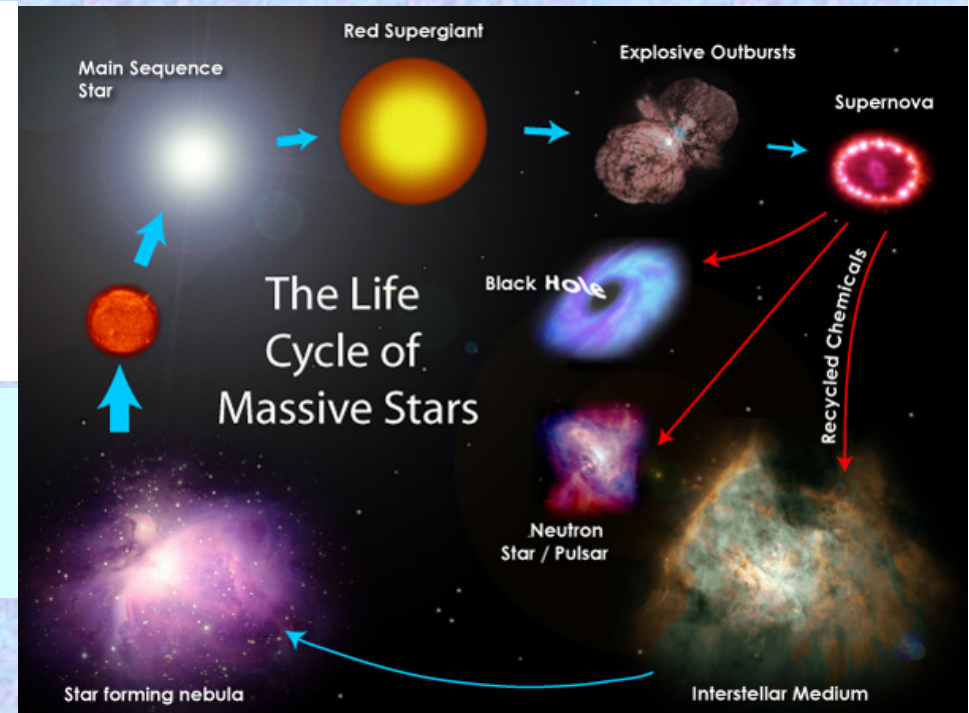
•Phases:

- to understand processes,
- to predict elemental abundances,
- to compare with data

**GCE tries to explain how and when the elements appear**

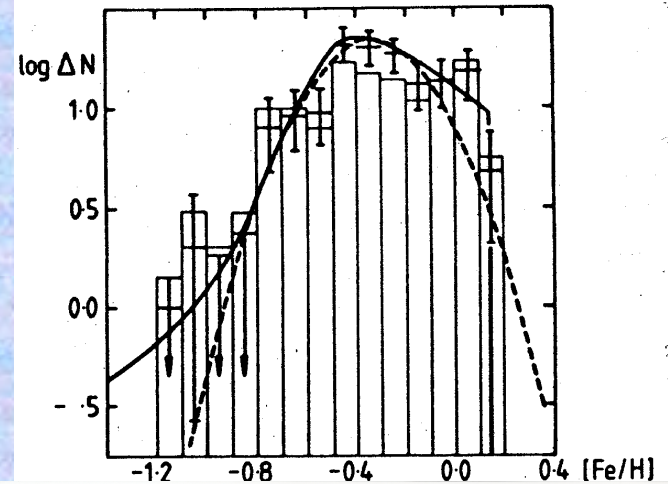
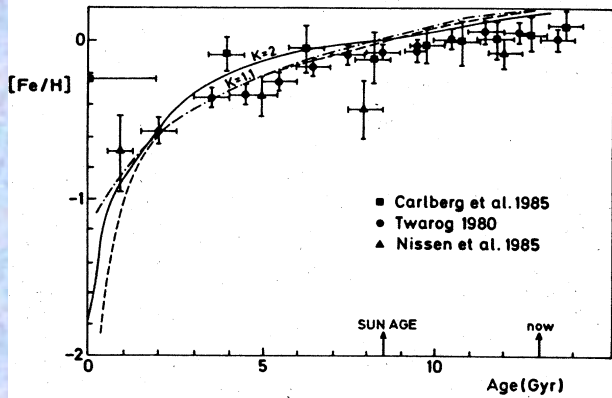
From elemental abundances we may deduce the evolutionary histories of galaxies

GH14-IFS techniques and analysis

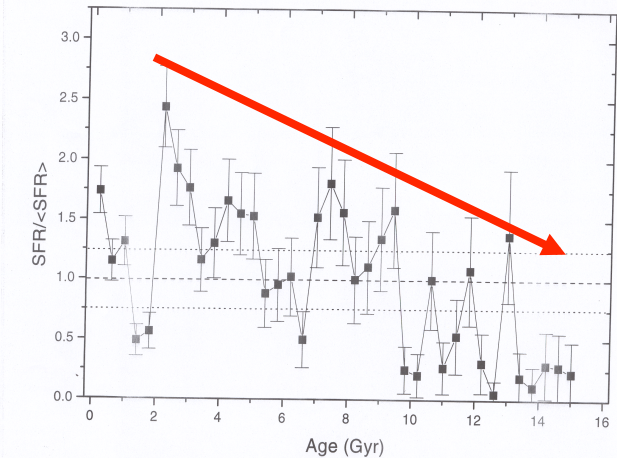
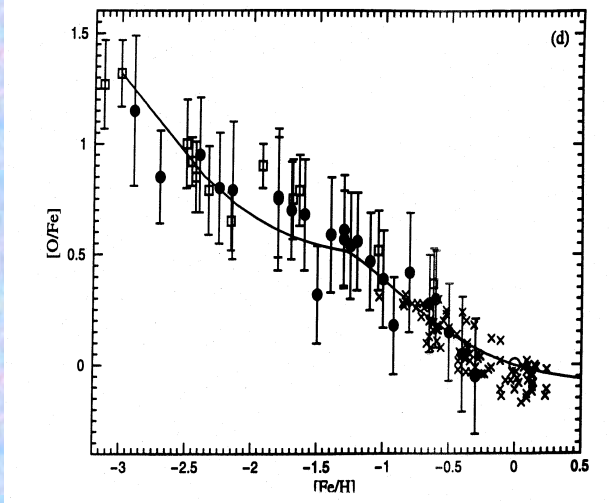




# Some MWG early observational data



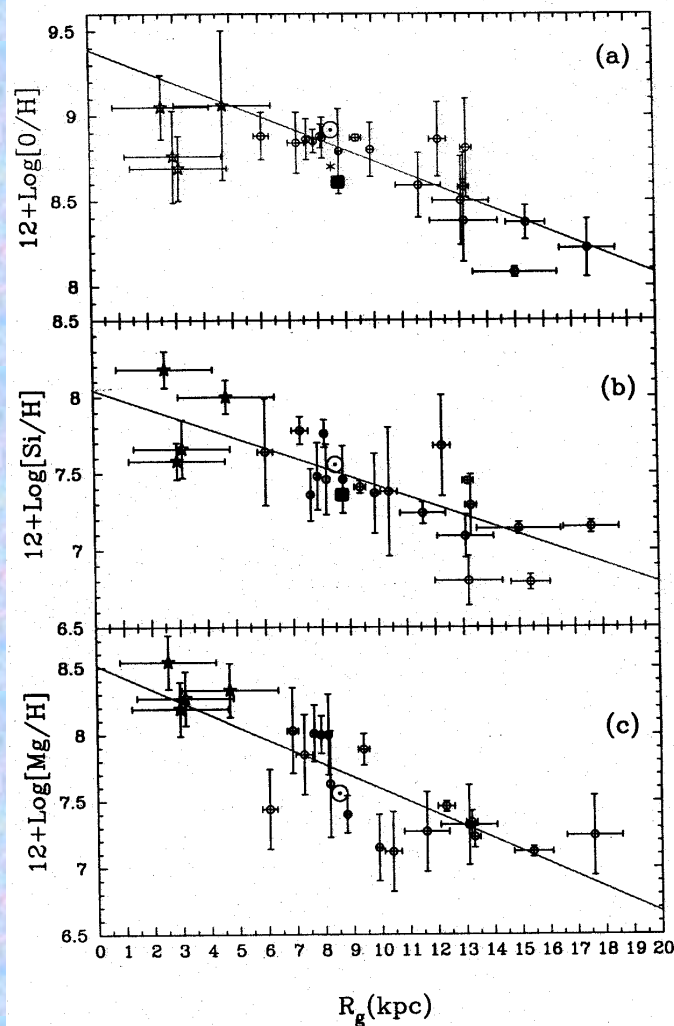
- The age-metallicity relation
- The G-dwarf metallicity distribution
- The star formation history in the SN
- The relative abundance of elements



GH14-IFS techniques and an

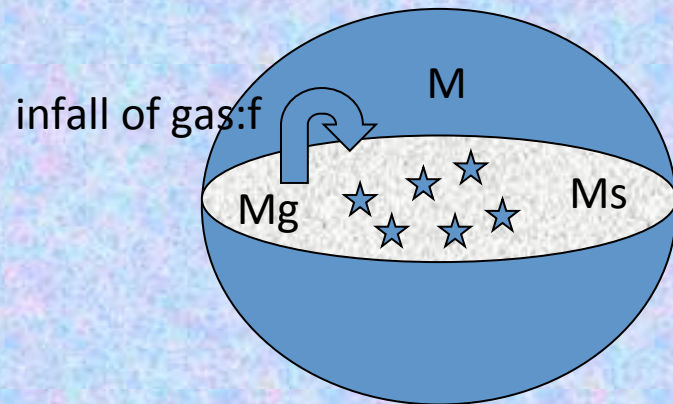


# CHEMICAL EVOLUTION MODELS: OBJETIVES



- **Chemical evolution models try to explain the chemical elements abundances and distributions within galaxies:**
  - Radial Variations of abundances
  - Metallicity Distributions
  - Relative abundances of elements
- **Ingredients which governs the chemical evolution**
  - Star Formation
  - Nucleosynthesis in the interior of stars
  - Initial Mass Function (IMF)
  - Mass loss of stars during their evolution
  - Exchange of matter or gas with external regions

## The basic system of CEM



- $f$  = flux of inflow gas (it may be 0 )
- $M$  = total mass of the system
- $\Psi$  = SFR (star formation rate)
- $E$  = mass ejection rate by the stars
- $M_s$  = stellar mass
- $M_g$  = gas mass

Each star loss mass after its stellar lifetime  $\tau_m$ , after this there is a remnant  $\omega_m$ , and therefore the total ejection by all stars created in a region is:

$$E(t) = \int_{m_i}^{\infty} (m - \omega_m) \Psi(t - \tau_m) \Phi(m) dm$$

Ejected mass by a star of mass  $m$

Initial mass function or number of stars in the range  $dm$

Mass of stars created in the time  $(t - \tau_m)$  which are now dying and ejecting mass after a time  $\tau_m$

## The basic equations of a CEM

$$\frac{dM}{dt} = f$$

$$\frac{dM_s}{dt} = \Psi - E$$

$$\frac{dM_g}{dt} = -\Psi + E + f$$

$$M = M_s + M_g$$

- $f$ = flux of inflow gas (it may be 0 )
- $M$ = total mass of the system
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- $E$ = mass ejection rate by the stars
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Mass of stars created in the time  $(t - \tau_m)$  which are now dying and ejecting mass after a time  $\tau_m$

Ejected mass by a star of mass  $m$



**The total yield of a stellar generation**

$$y = \frac{1}{1-R} \int_m^{\infty} m p_{z,m} \Phi(m) dm$$

$p_{z,m}$  is the metal fraction ejected by a star of mass  $m$

The abundance of metals may be obtained from this equation, which implies:

$$\frac{d(ZMg)}{dt} = -Z\Psi + Z_f f + -Z_w w + E_z$$

- 1)  $Z\Psi$ , metals which disappear from the gas when stars form
- 2)  $Z_f f$  mass of metals which going in to the region when the gas infall
- 3)  $Z_w w$  is the mass of metals which disappears with the outflow of gas
- 4)  $E_z$  quantity of metals ejected by stars

$$E_Z = \int_{m_t}^{\infty} m p_{z,m} \Psi(t - \tau_m) \Phi(m) dm +$$

$$\int_{m_t}^{\infty} (m - \omega_m - m p_{z,m}) Z(t - \tau_m) \Psi(t - \tau_m) \Phi(m) dm$$

The first part is the yield or metals newly created

The second one correspond to the metals which were before, in the original gas with which the star form

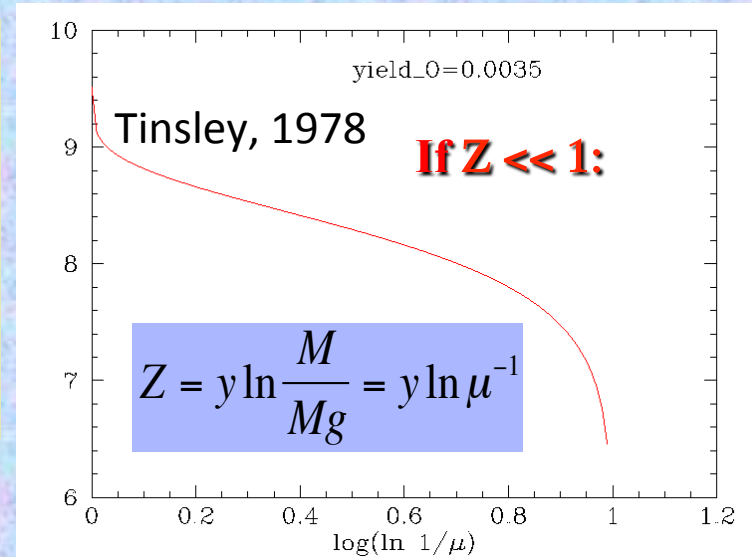
## THE SIMPLE MODEL: THE CLOSED BOX MODEL

1) The system will have 2 types of stars

- those with mass  $m > m_1$  with  $t = 0$
- those with  $m < m_1$  and  $t = \infty$

2) The system is closed  $f=0$

3) Metals are instantaneously mixed with the ISM



### Model predictions:

1. Abundance proportional to the total yield of one stellar generation  $y$
2. This relation abundance-yield is independent of the star formation history

### Problems:

1. The G-dwarf metallicity distribution is not reproduced
2. The relation not sufficient to obtain the observed radial gradient of abundances
3. The delay due to the mean-lifetimes of stars is necessary to each element appears in a different time

## Chemical Evolution Models

- These models calculate the chemical evolution of a galaxy: stars form, die and eject the elements created by stellar nucleosynthesis.
- They are the tool to interpret the elemental abundances in terms of star formation rate and/or of the gas dilution/enrichment processes in each region
- The evolutionary history gives the final state of the gas and stars, and the intermediate steps, too. The successive stellar generations are well defined in terms of age, metallicity (abundances) and stars and gas masses.
- The classical numerical chemical evolution models do not require as long computation time as cosmological simulations, they are better to test new assumptions or new inputs



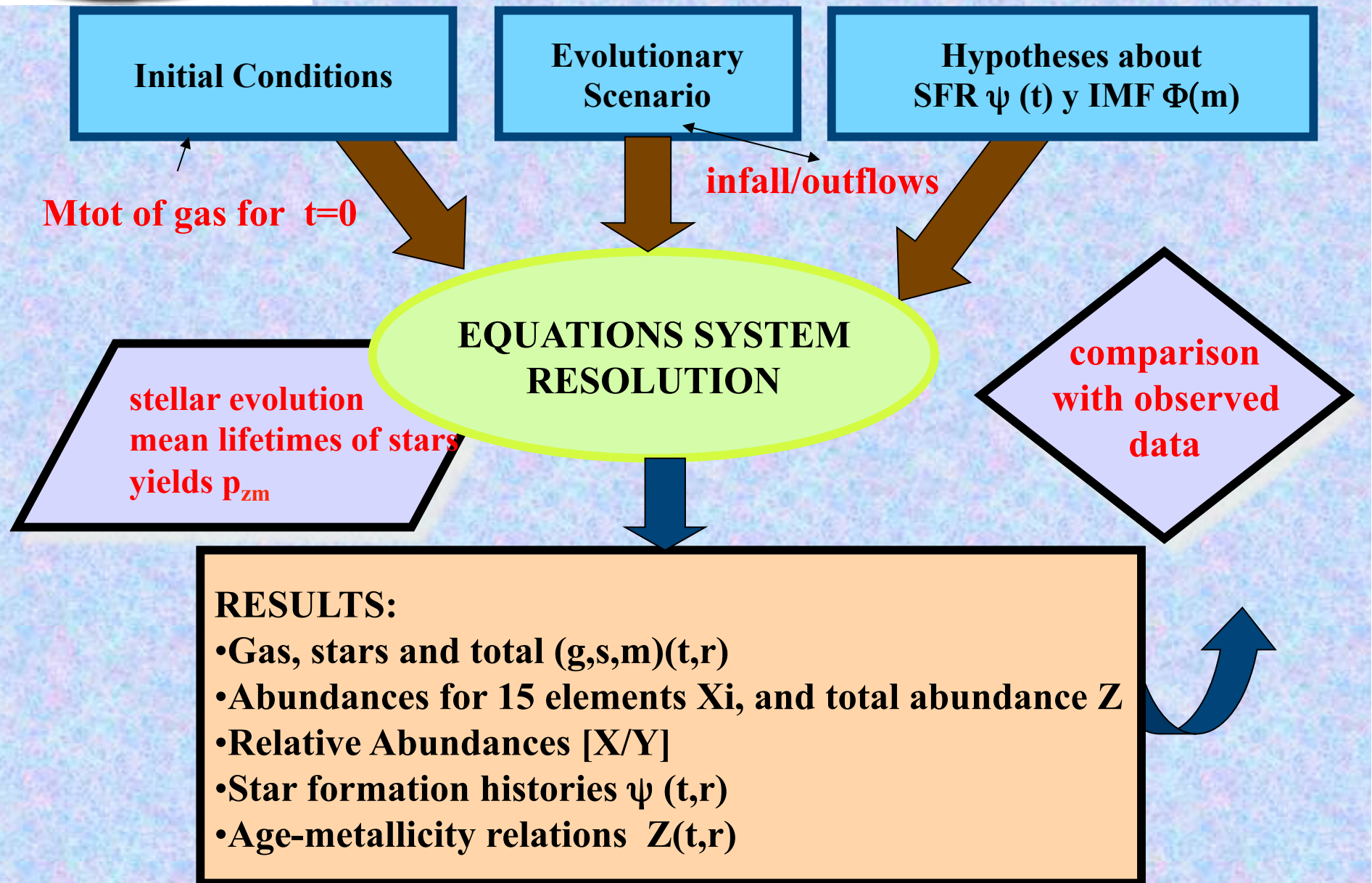
# A chemical evolution model



GOBIERNO  
DE ESPAÑA

MINISTERIO  
DE ECONOMÍA  
Y COMPETITIVIDAD

**Ciemat**  
Centro de Investigaciones  
Energéticas, Medioambientales  
y Tecnológicas



GH14-IFS techniques and analysis

Initial Conditions

Evolutionary  
Scenario

Hypotheses about  
SFR  $\psi(t)$  y IMF  $\Phi(m)$

infall/outflows

$M_{tot}$

❖ Initial Conditions:

- total mass
- Gas mass
- Primordials abundances

❖ Initial mass function (IMF):

- Variations with time
- Variations in the space

❖ Star formation laws: different possibilities

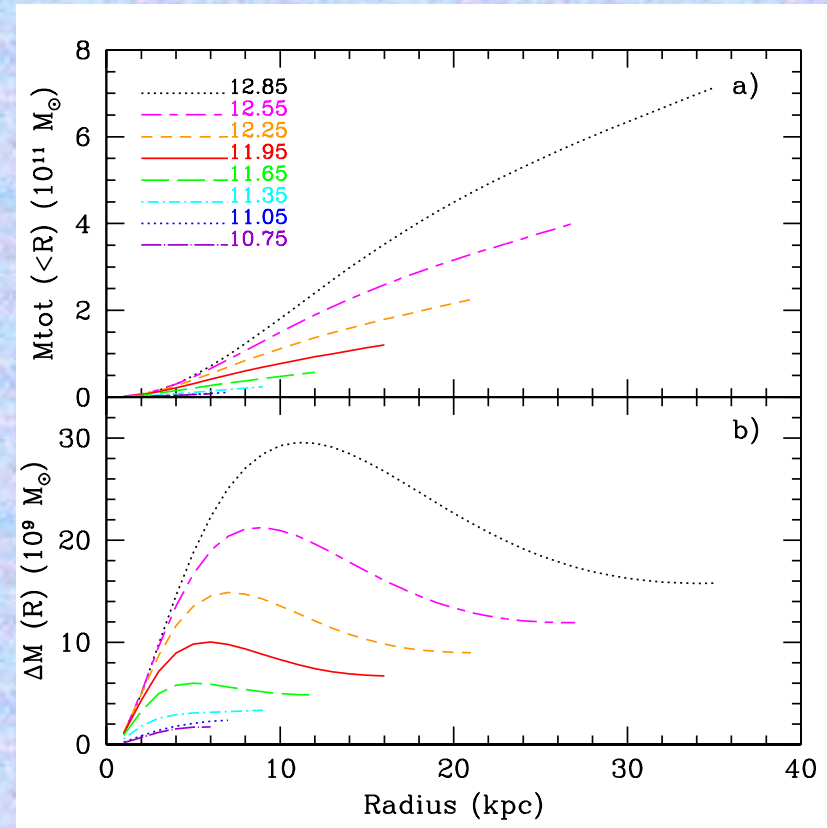
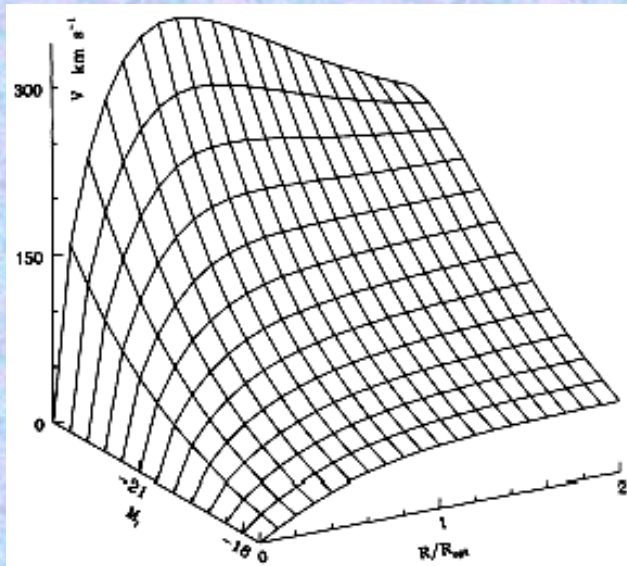
❖ The metallicity dependent yields

❖ The existence of possible inflows or outflows of gas

❖ The galactic scenario: the formation and evolution of the galaxy

• Age-metallicity relations  $Z(t,r)$

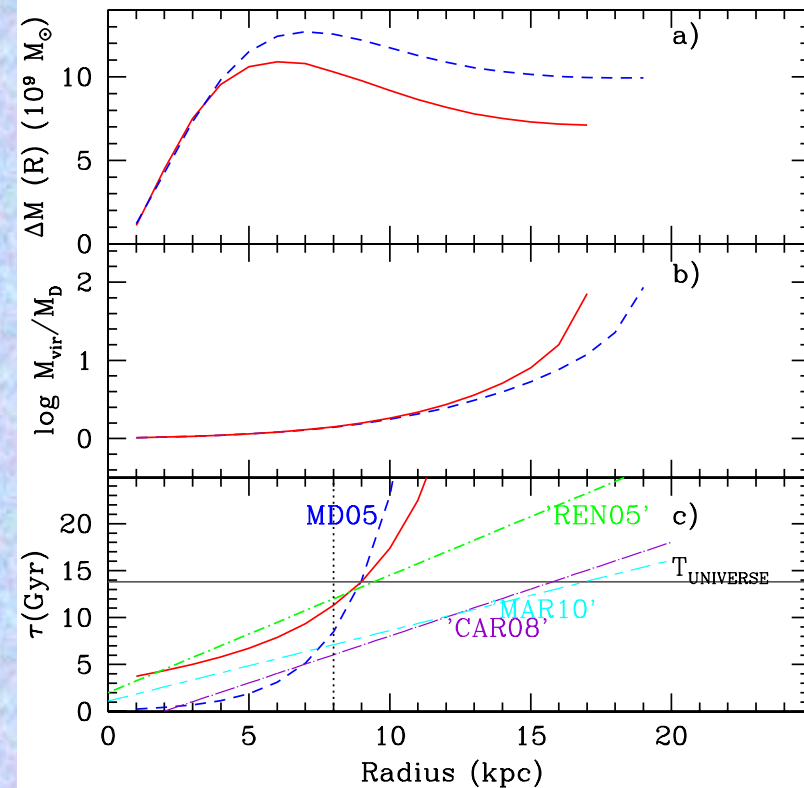
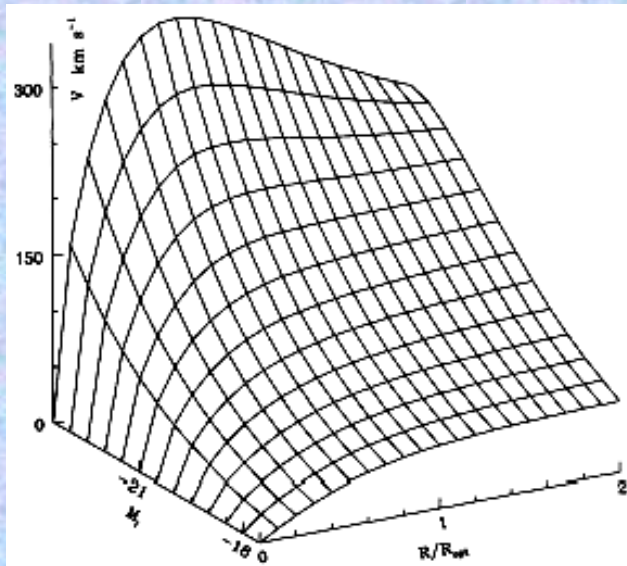
## Ingredients of the multiphase chemical evolution model: the scenario



The total mass  $M$  of each modeled galaxy and its radial distribution  $M(R)$  have been computed from the universal rotation curve  $V(R)$  from [Salucci \(2007\)](#)

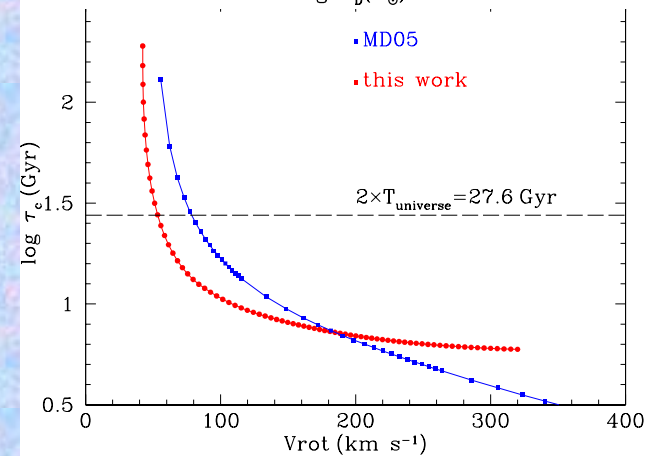
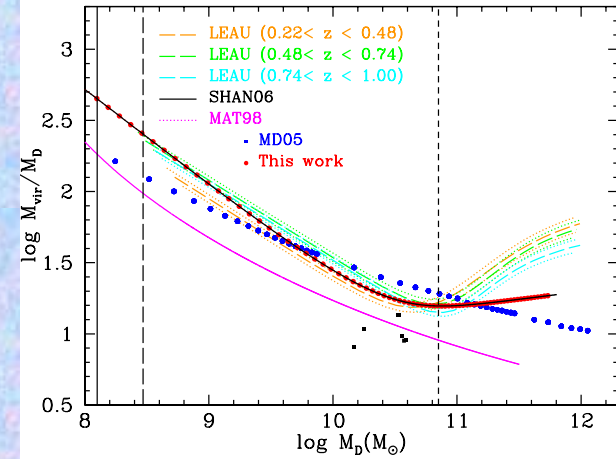
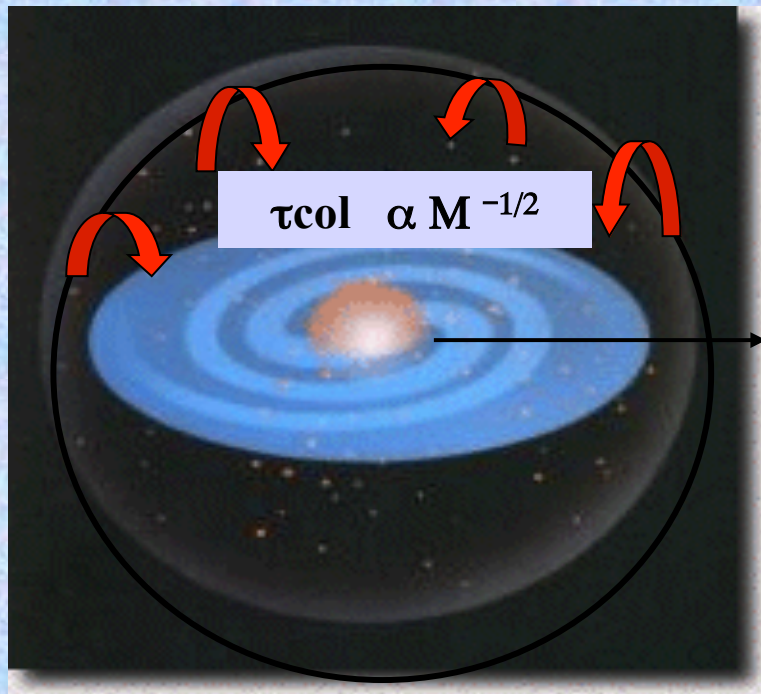


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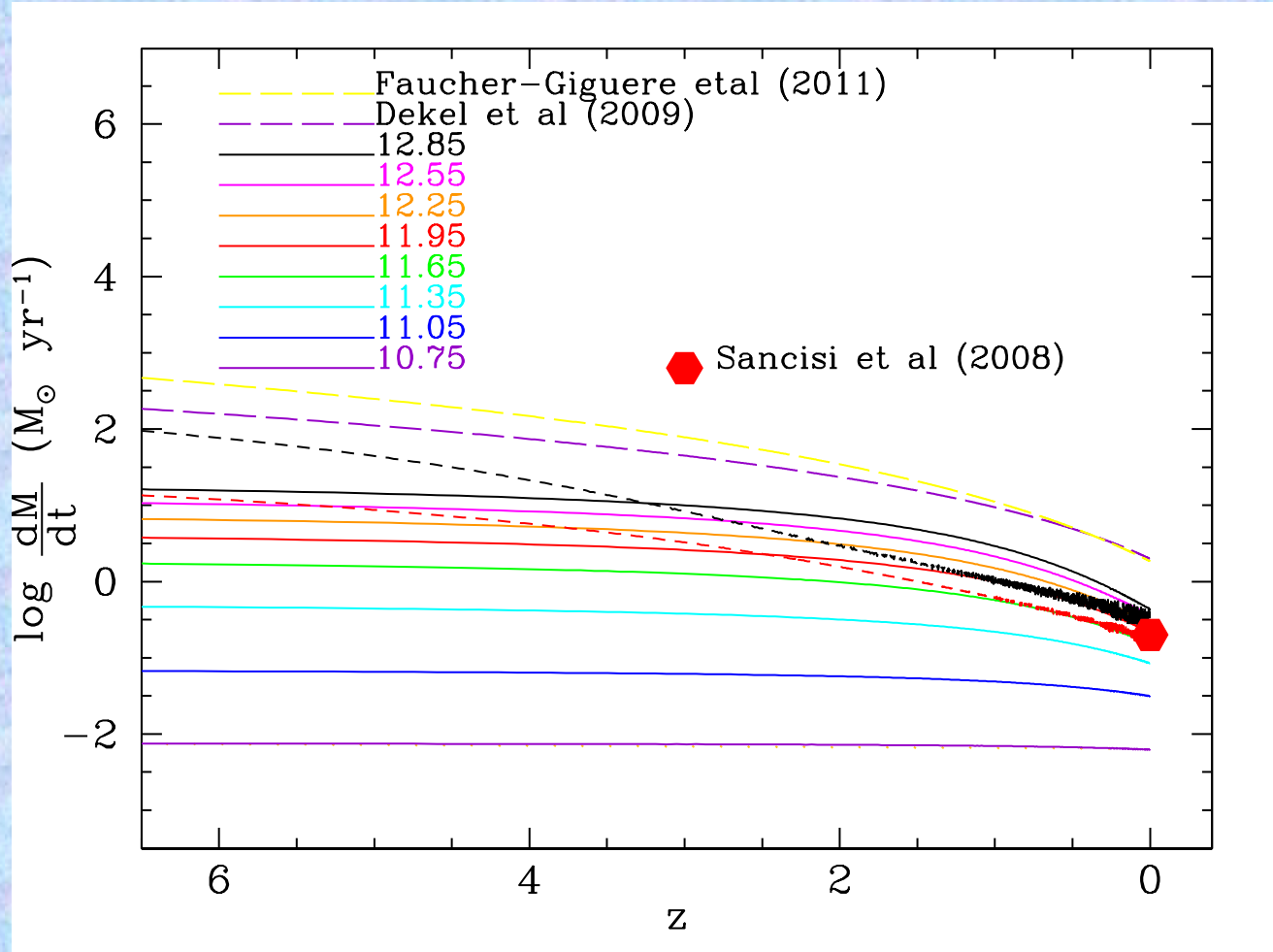


The total mass  $M$  of each modeled galaxy and its radial distribution  $M(R)$  have been computed from the universal rotation curve  $V(R)$  from **Salucci (2007)**

## Ingredients : The infall rate



- The gas collapses onto the equatorial plane and forms out the disc
- Infall rate  $\propto 1/\tau_{col}$
- $\tau_{col} = f(M_{gal})$  ...calibration with the MWG
- Since  $\sigma_{mass} = f(R)$ ,  $\tau = \tau(R)$ , following Shankar et al.



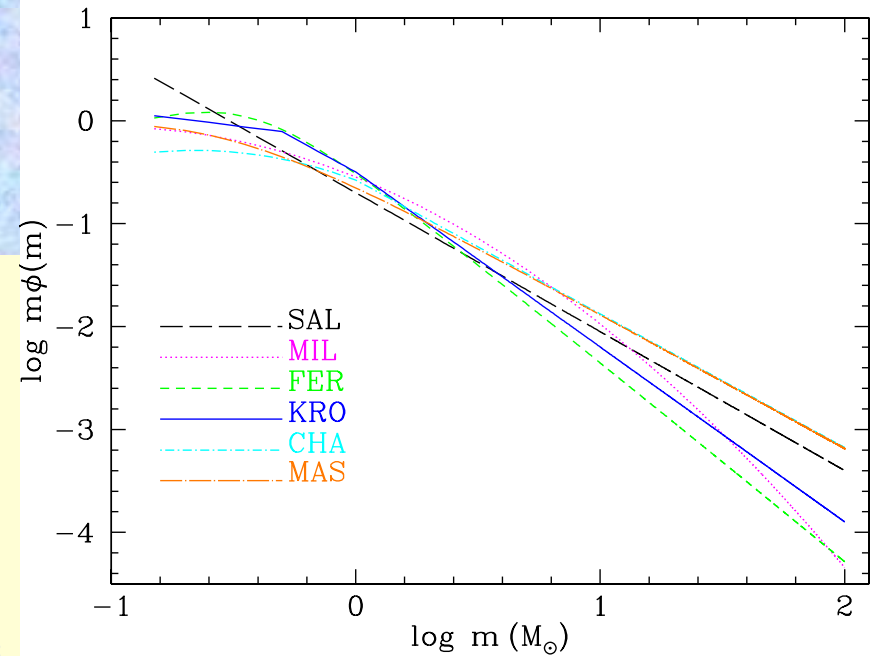
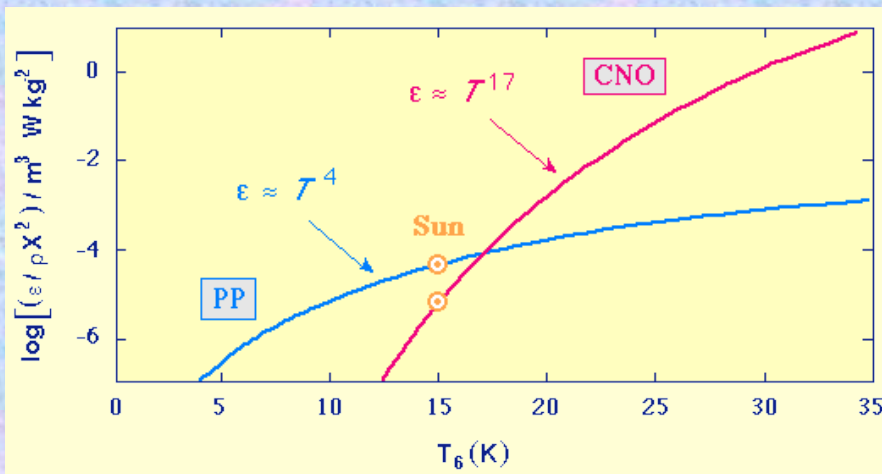
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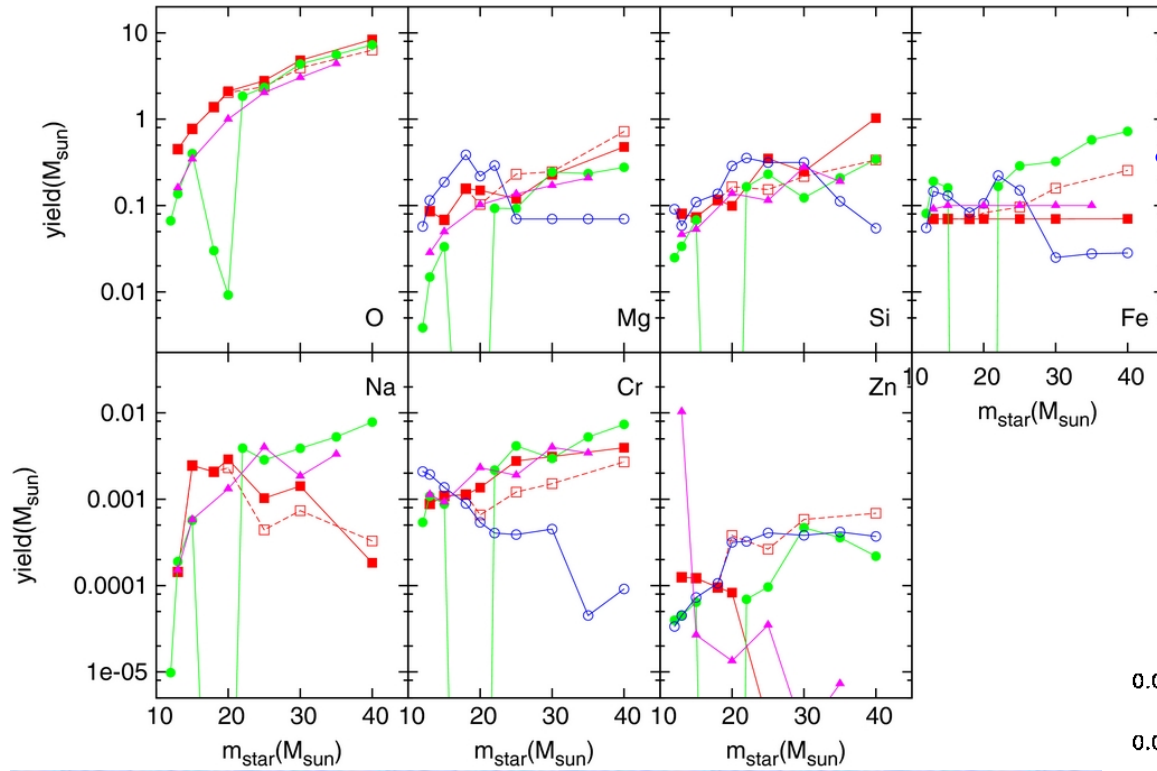
# IMF + stellar yields

- ❖ Absolute abundances depend on **the yield of a generation of stars** (single stellar population):  $p_z + \text{IMF}$

$$y = \frac{1}{1-R} \int_m^{\infty} m p_{z,m} \Phi(m) dm$$



- **Cycle pp:** low mass stars  $m < 4M_{\odot}$
- **Cycle pp+CNO:** intermediate mass stars  $4M_{\odot} < m < 8M_{\odot}$
- **Cycle CNO+ capture  $\alpha$ :** massive stars  $m > 8M_{\odot}$



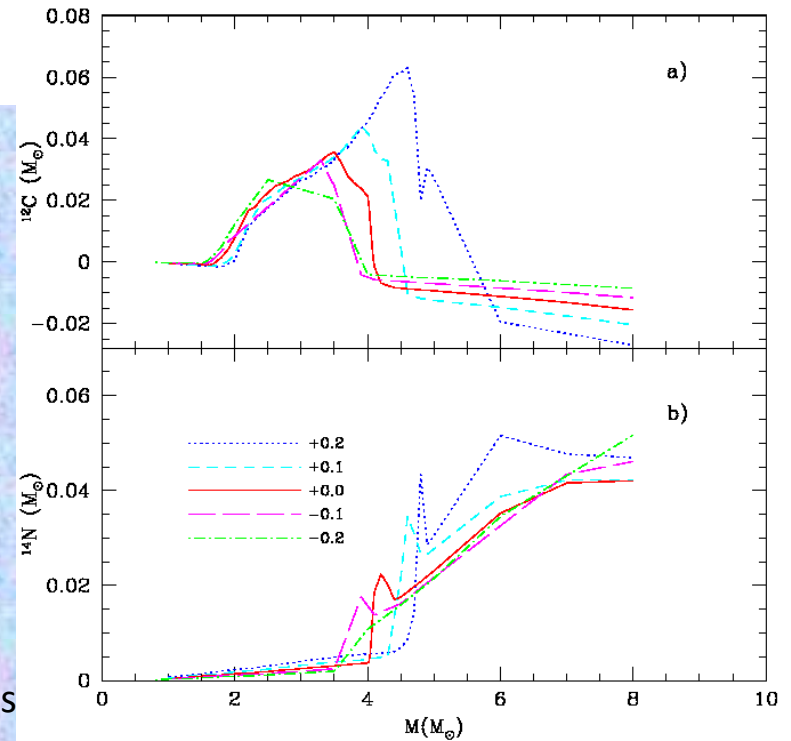
## Massive star yields

- Woosley & Weaver (1995)
- Frohlich et al. (2008)
- Chieffi & Limongi (2004)
- Kobayashi et al.
- Maeder & Meynet (1992)
- Maeder, Meynet & Hischi (2005)
- Portinari et al. (1998)

- LIM yields

- Renzini & Voli (1991)
- Van der Hoek & Groenewegen (1997)
- Marigo (2001)
- Gavián et al. (2005)
- Ventura et al. (2002)
- Dray et al (2003)
- Karakas & Lattanzio (2010)

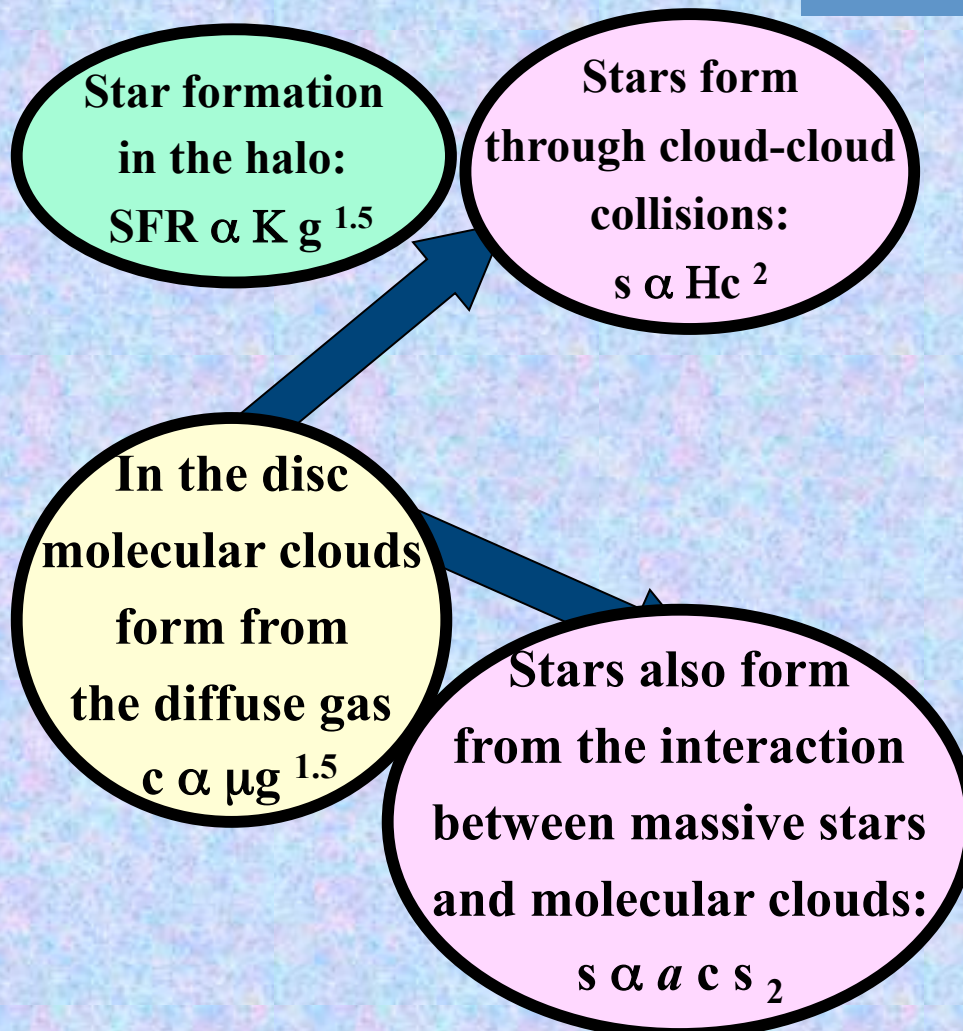
GH14-IFS techniques



# Inputs of the multiphase chemical evolution model:

## The star formation law

$$\Psi_D(t) = (H_1 + H_2)c_D^2(t) + (a_1 + a_2)S_{2,D}(t)c_D(t)$$



- ❖ Every parameter changes along the galactocentric radius:
  - $K = \epsilon_K (G/V)^{1/2}$
  - $\mu = \epsilon_\mu (G/Vd)^{1/2}$
  - $H = \epsilon_H cte / Vd$
  - $a = \epsilon_a (G \rho_c)^{1/2} / \langle m_{s2} \rangle$
- ❖ The efficiency  $\epsilon_a$  is a local parameter
- ❖ The efficiency  $\epsilon_K$  is assumed as constant for all halos
- ❖ Efficiencies  $\epsilon_\mu$  y  $\epsilon_H$  are variable for each galaxy



❖ **Every parameter changes along the galactocentric radius:**

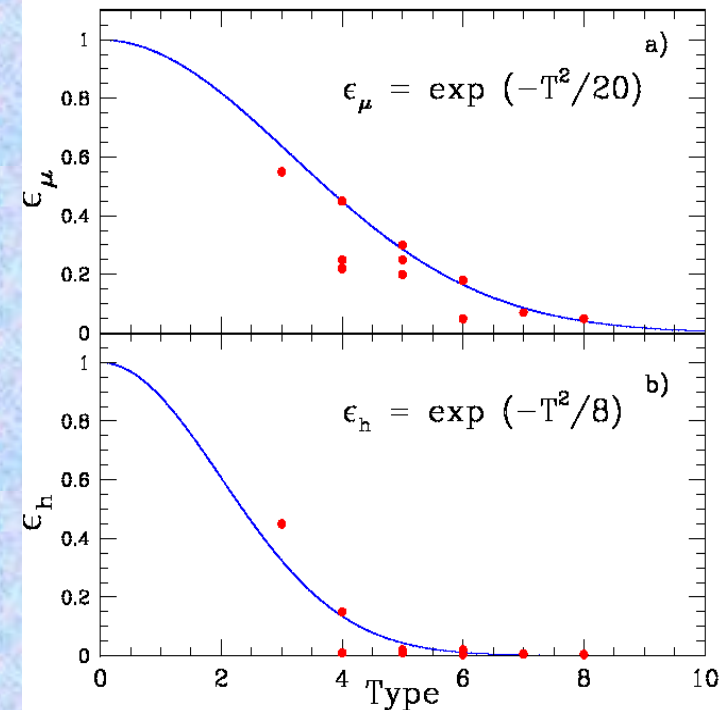
- $K = \epsilon_K (G/V)^{1/2}$
- $\mu = \epsilon_\mu (G/Vd)^{1/2}$
- $H = \epsilon_H \text{cte} / Vd$
- $a = \epsilon_a (G \rho_c)^{1/2} / \langle m_{s2} \rangle$
- $\tau_{\text{col}} = \tau_{\text{col},0} \exp(R/\lambda)$

❖ **The efficiency  $\epsilon_a$  does not change with R since it is a local process**

❖ **The efficiency  $\epsilon_K$  is assumed as constant for all halos**

❖ **Efficiencies  $\epsilon_\mu$  y  $\epsilon_H$  are variable for each galaxy**

❖ **The collapse time scale depends on the total mass of the galaxy**



**From data of molecular and diffuse gas masses in galaxies (Young et al. 1996), we found that efficiencies to form molecular clouds and stars depend on morphological type of galaxies.**

**We vary only 2 “parameters”, total mass and T**

		1	2	3	4	5	6	7	8	9	10		
	Vrot	0.95	0.8	0.75									
1	30	<div style="border: 2px solid green; padding: 10px; display: inline-block;"> <p style="text-align: center;"><u>BCD &amp; HII Gal.</u></p> <p style="text-align: center;"><u>Low mass galaxies</u></p> </div>											
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28	200					MWG							
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39	291			M31									
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43													
44	387												

BCD & HII Gal.

Low mass galaxies

Normal spirals

Starbursts

Low surface brightness Galaxies

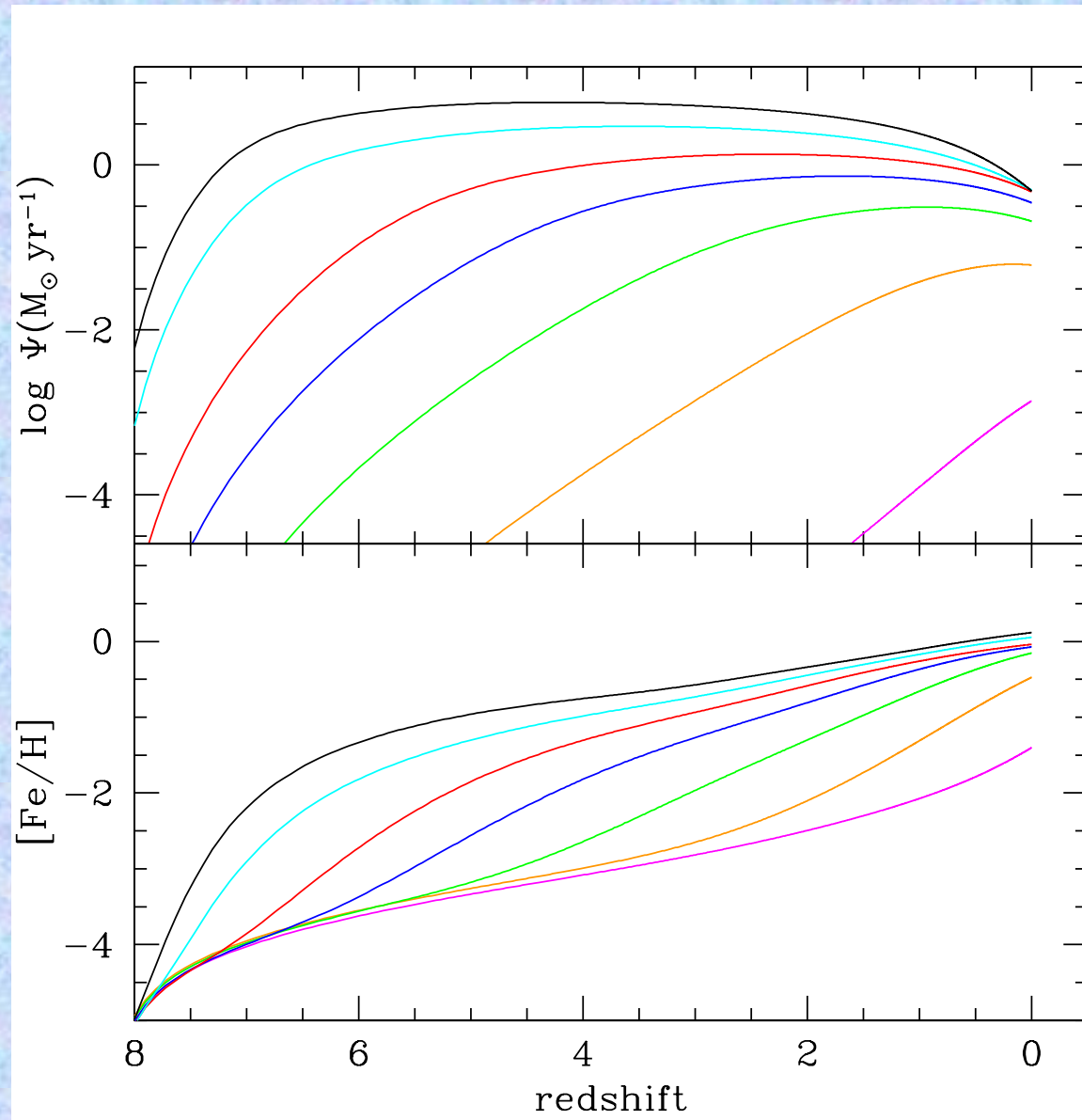
		1	2	3	4	5	6	7	8	9	10																																																																			
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1	30	<div style="border: 2px solid green; padding: 10px;"> <p style="text-align: center; font-size: 2em; color: blue;">BCD &amp;</p> <p style="text-align: center; font-weight: bold;">Table 1. Theoretical galaxy models selected to represent a simulated Hubble sequence</p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <thead> <tr> <th>dis</th> <th><math>V_{max}</math> km s<sup>-1</sup></th> <th><math>M_{gal}</math> 10<sup>11</sup> M<sub>⊙</sub></th> <th><math>R_{opt}</math> kpc</th> <th><math>\tau_c</math> Gyr</th> <th><math>nt</math></th> <th><math>\epsilon_\gamma</math></th> <th><math>\epsilon_\delta</math></th> </tr> </thead> <tbody> <tr> <td>3</td> <td>48</td> <td>0.3</td> <td>2.3</td> <td>31.6</td> <td>8</td> <td>0.037</td> <td>2.6 10<sup>-4</sup></td> </tr> <tr> <td>10</td> <td>78</td> <td>1.3</td> <td>4.1</td> <td>15.5</td> <td>7</td> <td>0.075</td> <td>1.5 10<sup>-3</sup></td> </tr> <tr> <td>21</td> <td>122</td> <td>4.3</td> <td>7.1</td> <td>8.1</td> <td>6</td> <td>0.15</td> <td>1.0 10<sup>-2</sup></td> </tr> <tr> <td>24</td> <td>163</td> <td>9.8</td> <td>10.1</td> <td>5.4</td> <td>5</td> <td>0.30</td> <td>5.0 10<sup>-2</sup></td> </tr> <tr> <td>28</td> <td>200</td> <td>17.9</td> <td>13.0</td> <td>4.0</td> <td>4</td> <td>0.45</td> <td>1.4 10<sup>-1</sup></td> </tr> <tr> <td>35</td> <td>250</td> <td>33.5</td> <td>16.9</td> <td>2.9</td> <td>3</td> <td>0.65</td> <td>3.4 10<sup>-1</sup></td> </tr> <tr> <td>39</td> <td>290</td> <td>52.7</td> <td>20.6</td> <td>2.3</td> <td>1</td> <td>0.95</td> <td>8.8 10<sup>-1</sup></td> </tr> </tbody> </table> </div>											dis	$V_{max}$ km s <sup>-1</sup>	$M_{gal}$ 10 <sup>11</sup> M <sub>⊙</sub>	$R_{opt}$ kpc	$\tau_c$ Gyr	$nt$	$\epsilon_\gamma$	$\epsilon_\delta$	3	48	0.3	2.3	31.6	8	0.037	2.6 10 <sup>-4</sup>	10	78	1.3	4.1	15.5	7	0.075	1.5 10 <sup>-3</sup>	21	122	4.3	7.1	8.1	6	0.15	1.0 10 <sup>-2</sup>	24	163	9.8	10.1	5.4	5	0.30	5.0 10 <sup>-2</sup>	28	200	17.9	13.0	4.0	4	0.45	1.4 10 <sup>-1</sup>	35	250	33.5	16.9	2.9	3	0.65	3.4 10 <sup>-1</sup>	39	290	52.7	20.6	2.3	1	0.95	8.8 10 <sup>-1</sup>		
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Low surface  
brightness Galaxies

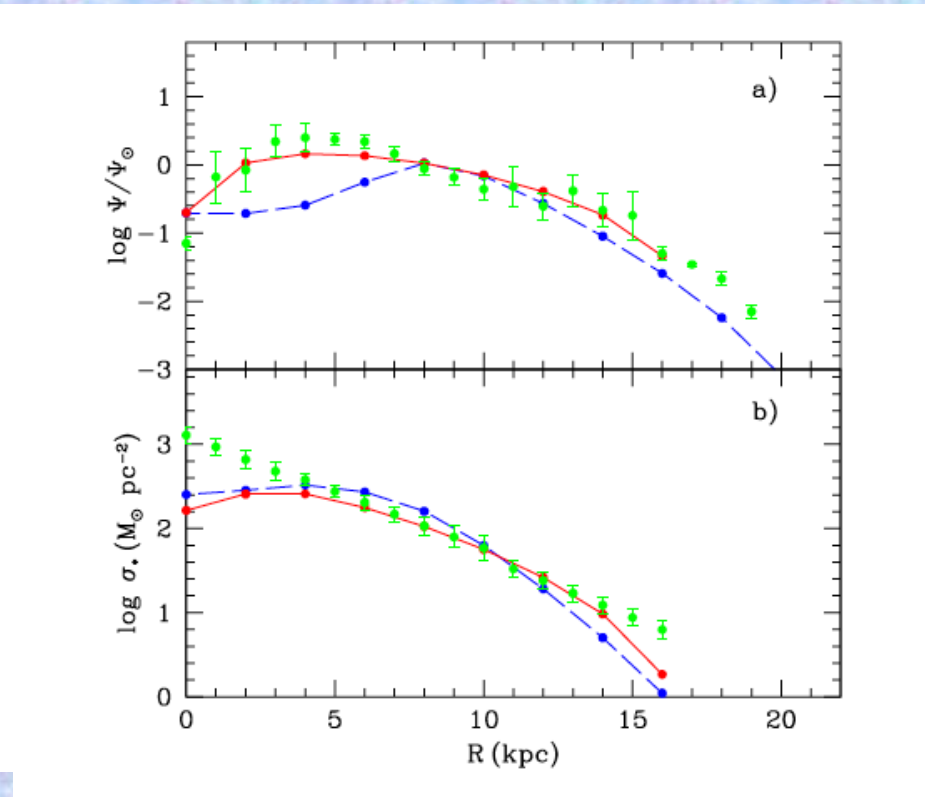
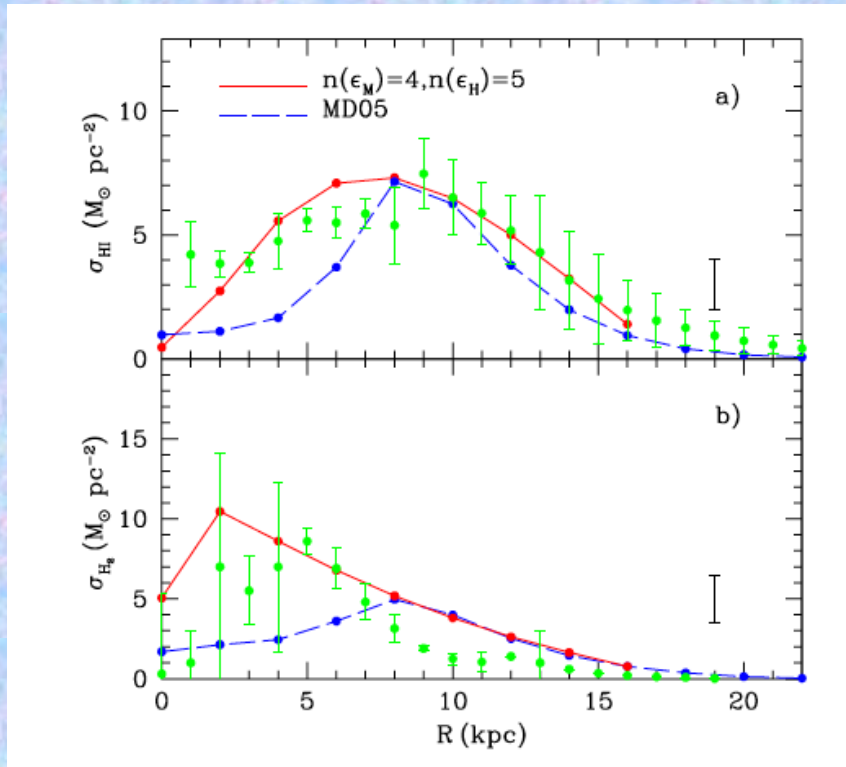


## **New grid of models: updating the inputs and assumptions**

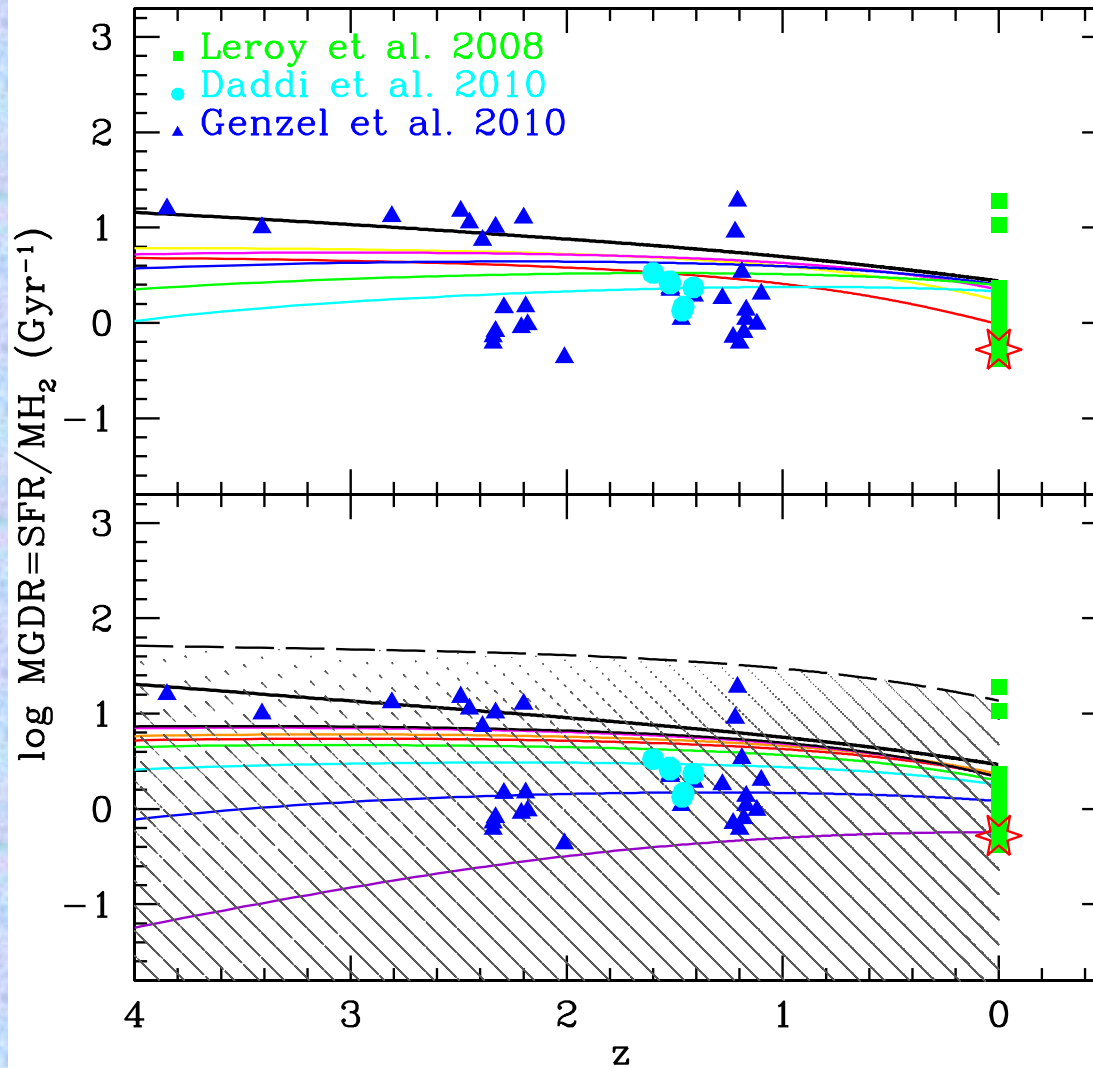
- Radial distributions computed following equations from Salucci et al. (2007) defined in terms of  $M_{\text{vir}}$  and arriving to longer distances along the galactocentric radius
- Collapse time-scale  $\tau$  modified to follow the prescriptions from Shankar et al. (2006) about the observed ratio  $M_{\text{disk}}/M_{\text{halo}}$
- New grid of models: 75 radial mass distributions,
  - $M_{\text{vir}} \in [5 \cdot 10^{10} - 10^{13}] M_{\text{sun}}$
  - $M_{\text{disk}} \in [1.25 \cdot 10^8 - 5.3 \cdot 10^{11}] M_{\text{sun}}$
  - $V_{\text{rot}} \in [42 - 320] \text{ km/s}$
- Radial dependence  $\tau(R)$  smoother than the old one
- Efficiencies  $\varepsilon_{\text{M}}$  and  $\varepsilon_{\text{H}}$  selected independently: 10 values in the range [0--1]
- Revision of new set of stellar yields and different IMFs



## Calibration of the MWG disk: radial distributions of surface density of gas, stellar mass and SFR

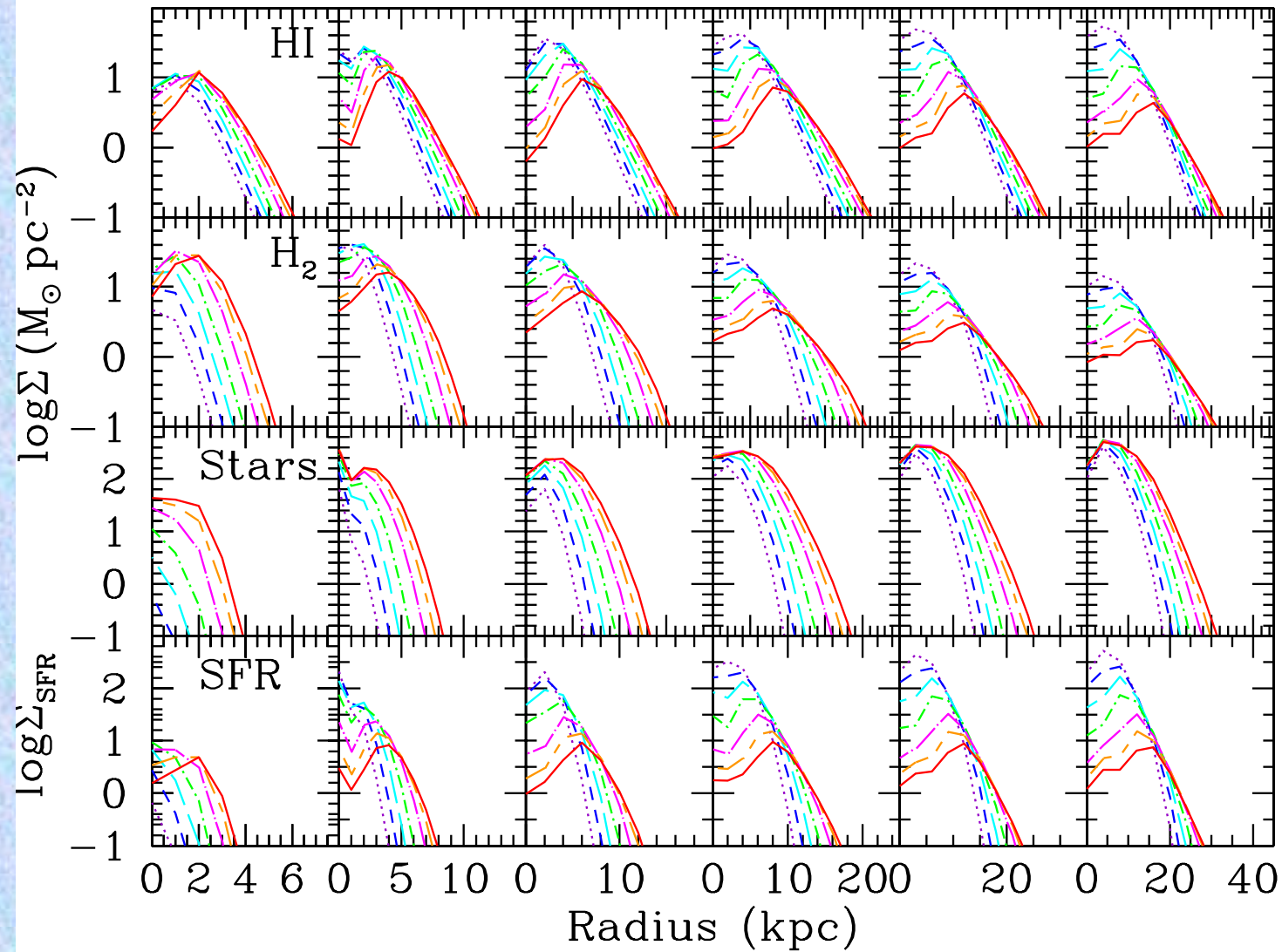




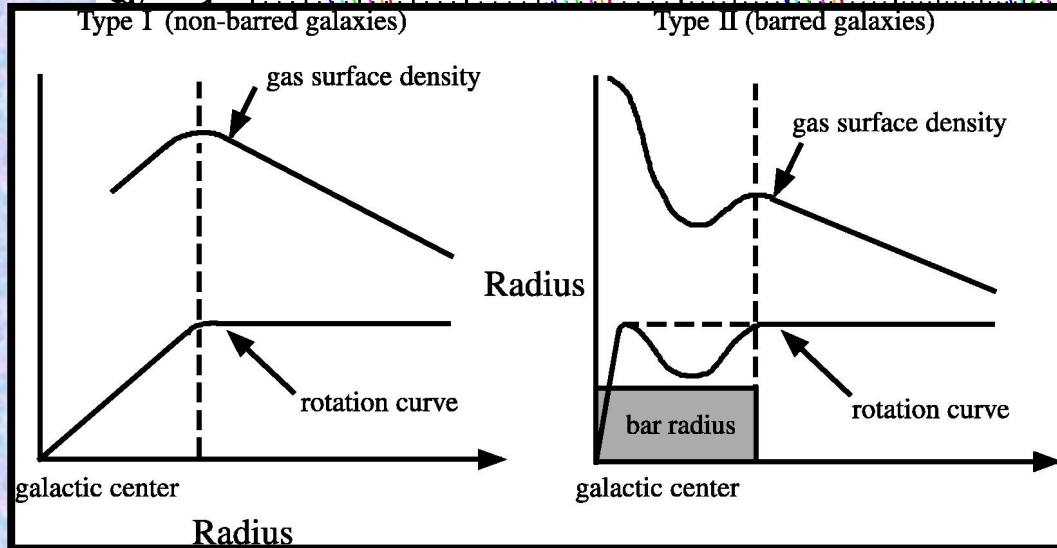
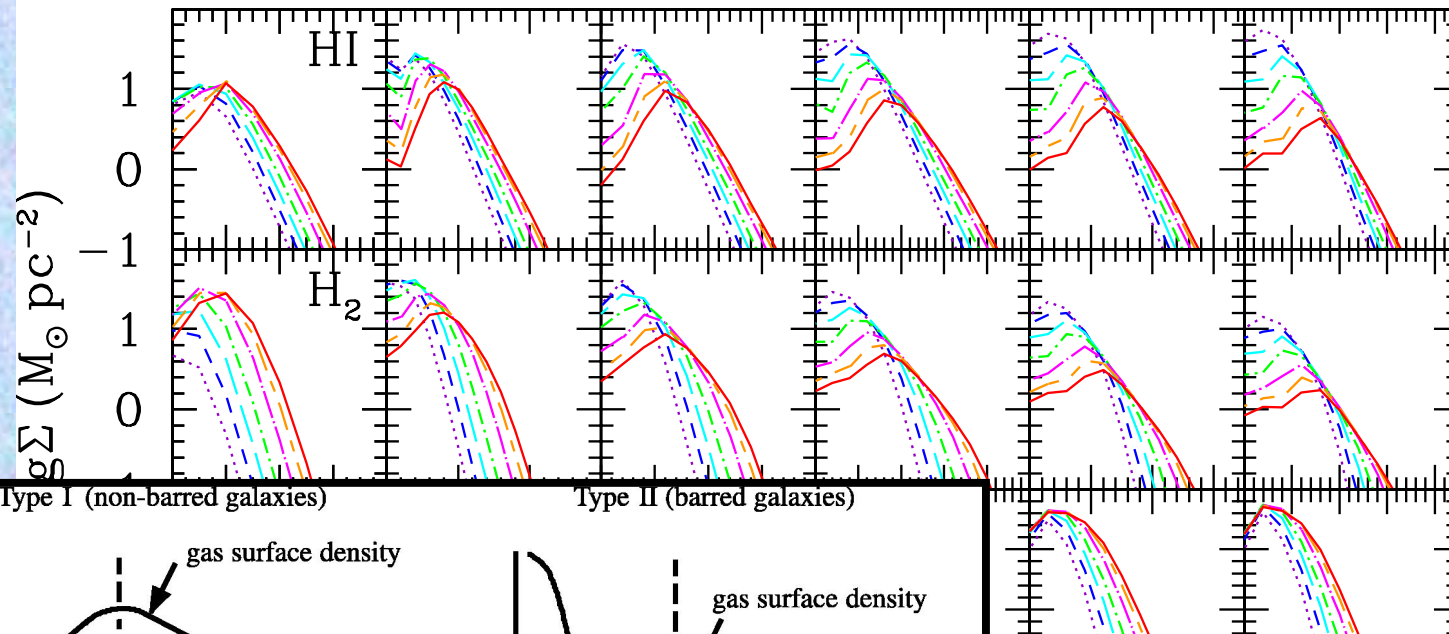


The evolution  
of the SF  
efficiency  
measured as  
SFR/MH<sub>2</sub>  
along the  
redshift

## Evolution of disks along redshift



# Evolution of disks along redshift



**The generic form of  
molecular gas radial  
distributions found by  
Nishiyama et al. (2001)**

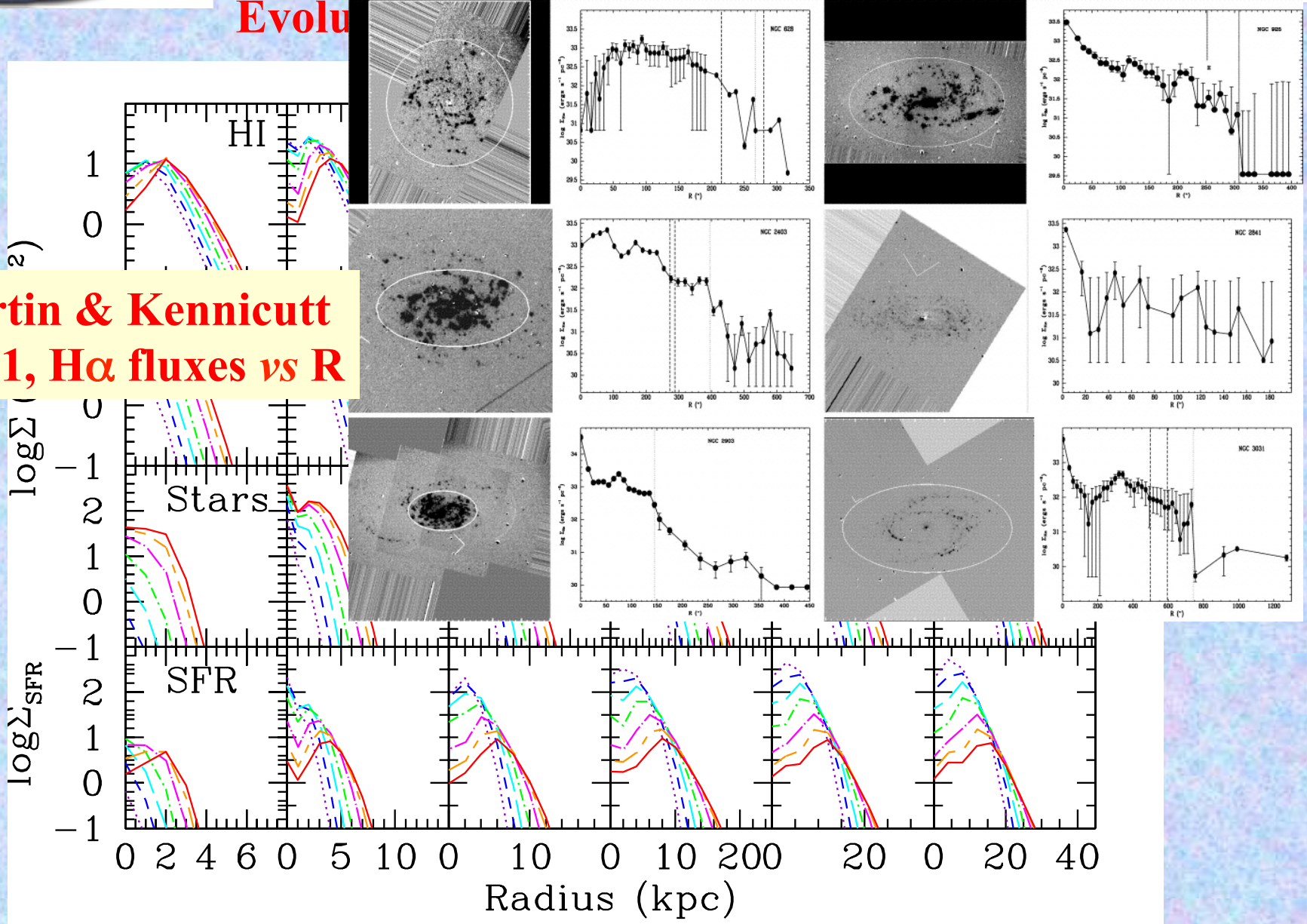
Radius (kpc)

GH14-IFS techniques and analysis

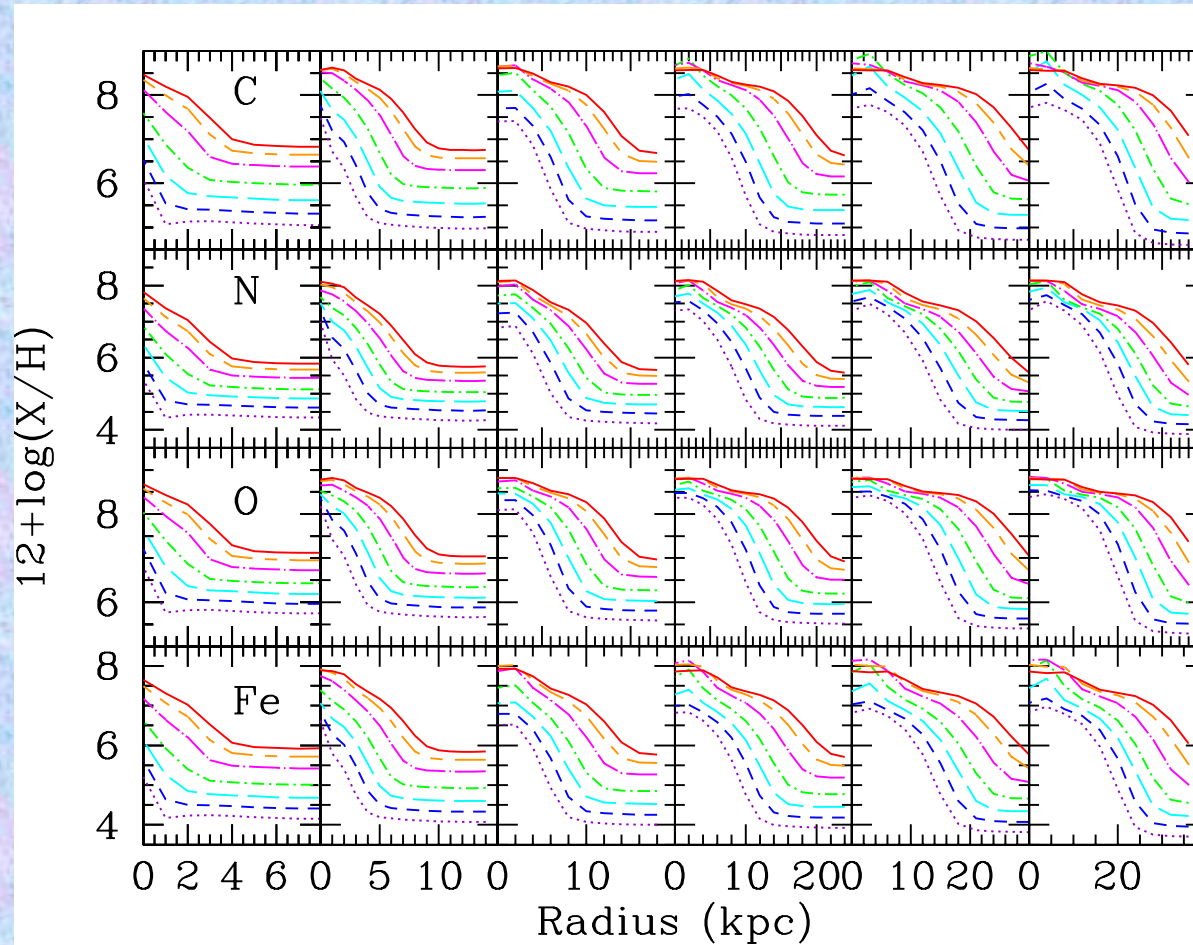


**Evolu**

**Martin & Kennicutt  
2001, H $\alpha$  fluxes vs R**



## The evolution of the abundance radial distributions along z



**Flat radial  
gradients for low  
evolved galaxies,  
and for the most  
evolved galaxies**

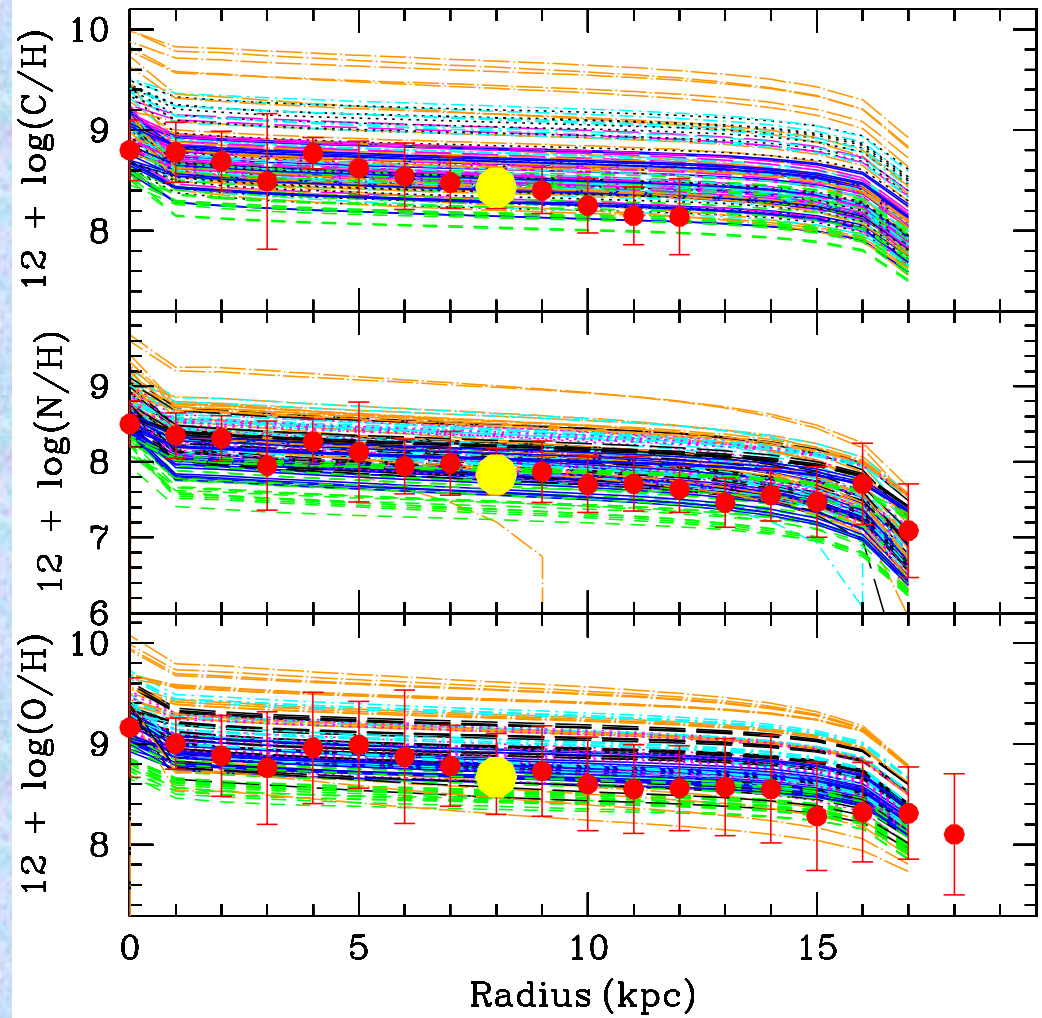
**The inner radial  
distributions  
flatten compared  
with the discs**

**Our models show a maximum oxygen abundance  $12+\log(\text{O}/\text{H}) \sim 8.9-9.0$  (Pilyugin et al)**

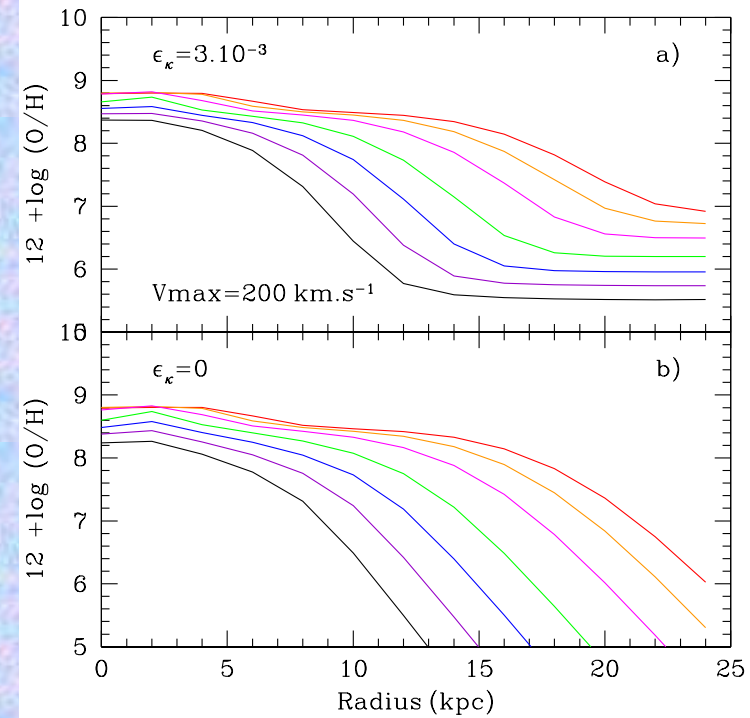
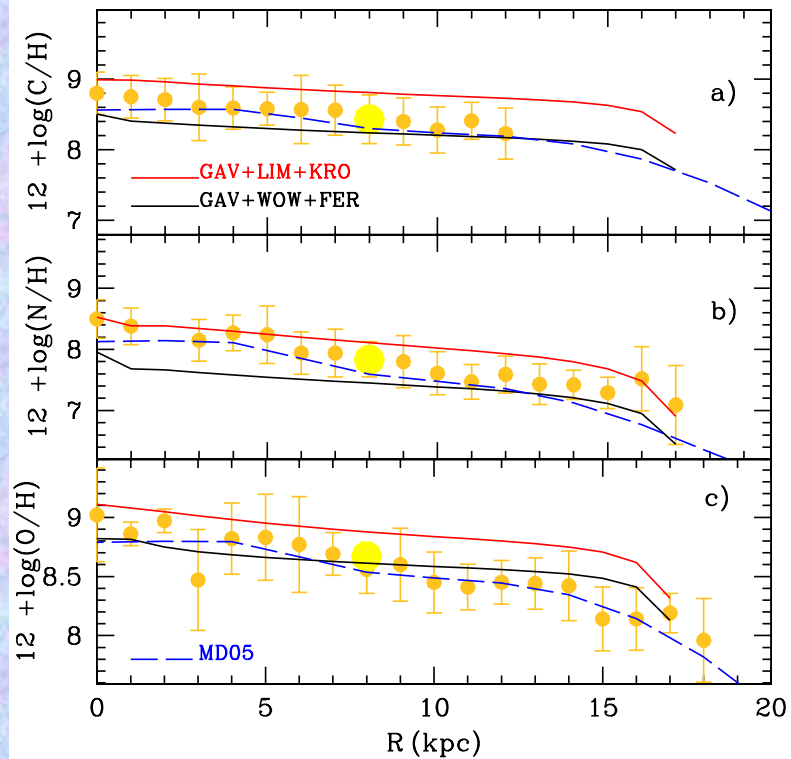
**There is also a minimum abundance**



**IMF & stellar yields:**  
**no effect on the radial**  
**gradient of**  
**abundances, only**  
**variations on the**  
**absolute values of**  
**abundances**

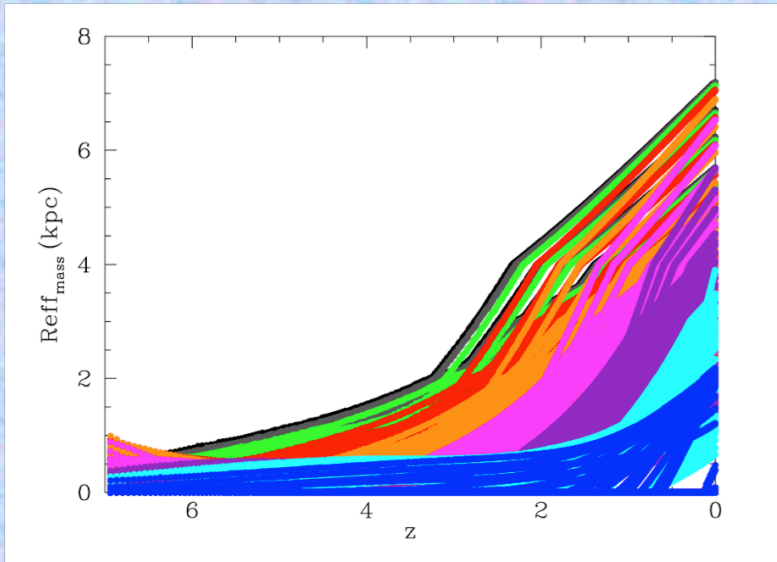






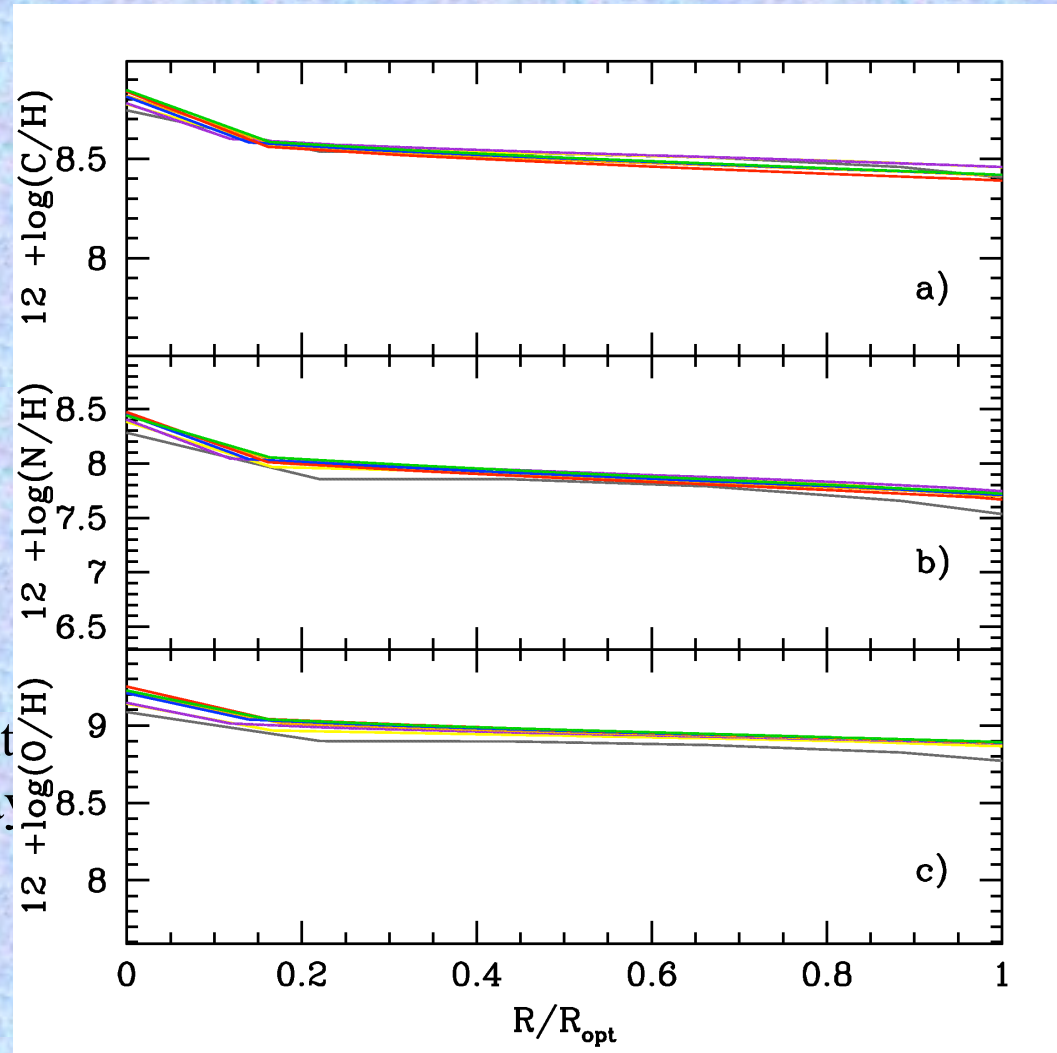
A variation of the infall rate, now smoother than in our old models, changes the radial gradient which is flatter now

A flattening of the radial gradient appears in the O distributions: It seems due to the infall rate of enriched gas from the halo

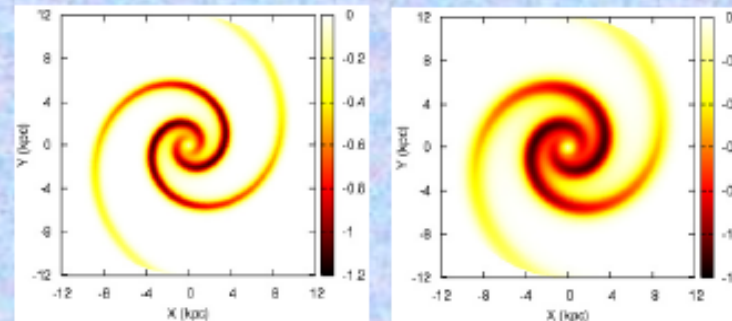
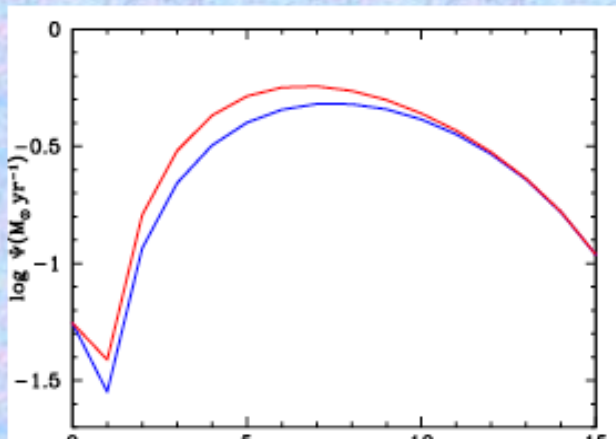
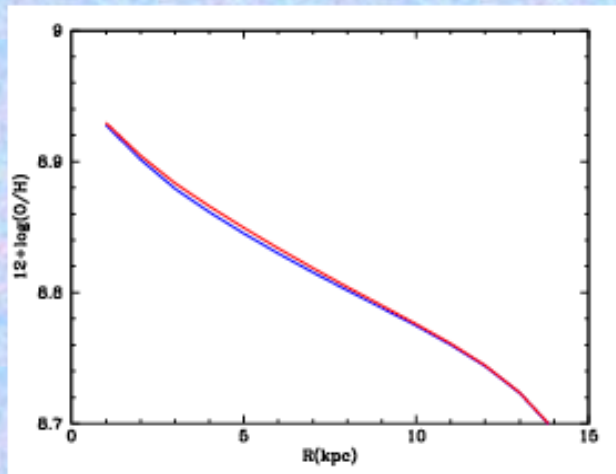


The radial gradients for the same  $\epsilon_M$  and  $\epsilon_H$  and different Mvir models, when measured with normalized distances, are equivalent

By observing different radial gradient with a normalized radial scale we may distinguish different efficiencies to form molecular clouds or stars in galaxies



## Next step: 2D Chemical evolution models



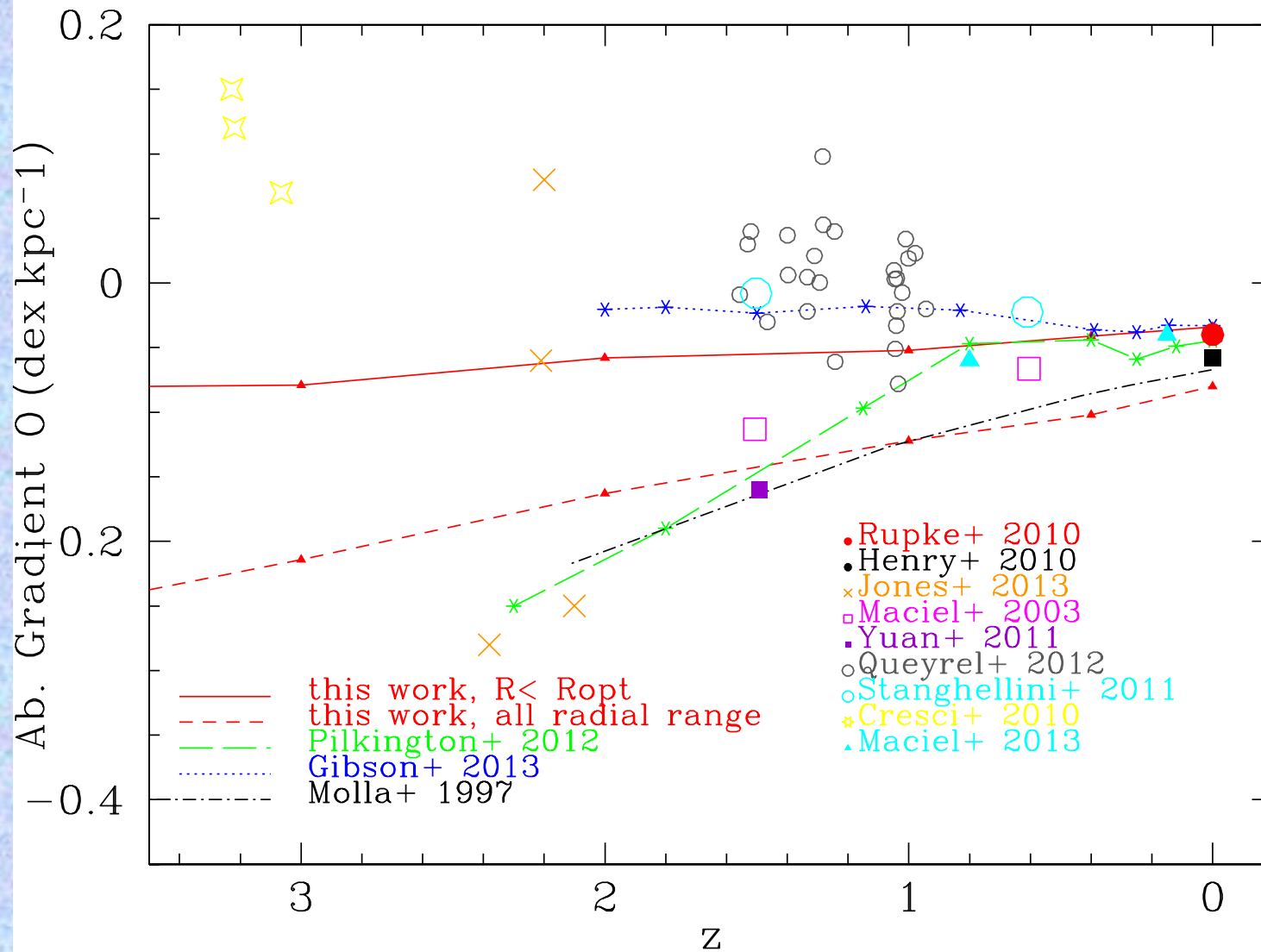
**Fig. 2.** Map of the perturbing potential in the plane of the galaxy. The colors represent the values of  $\Phi_1(R, \varphi)$  in arbitrary units. The picture on the *left* is the potential with  $\sigma = 2.5$  kpc and on the *right*  $\sigma = 4.7$  kpc. For  $i = 14^\circ$  we have on the left  $\sigma_{\perp} = 0.6$  kpc and on the right  $\sigma_{\perp} = 1.1$  kpc.

“The surface density of a zero-thickness disk can be represented mathematically as the sum of an axisymmetric or unperturbed surface density  $\Sigma_0(R)$ , and a perturbed surface density  $\Sigma_1(R, \phi)$ , which represents the spiral pattern in a frame that rotates at angular speed  $\Omega_p$ . The azimuthal coordinate at the rotating frame of reference is  $\phi = \theta - \Omega_p t$ , where  $\theta$  is the angle at the inertial frame” (Junqueira et al. 2013)

$$\Sigma_1(R, \theta - \Omega_p t) = \sum_s e^{i[m(\theta - \Omega_p t) + f_m(R)]},$$



1. We are computing models for a wide range of total masses and efficiencies.
2. New models seem being in better agreement with observations of molecular clouds and star formation rate radial distributions, therefore they will be better estimates of the “expected values”
3. Different IMFs or stellar yield sets only change the absolute values of abundances but not the shape of the radial gradients.
4. A realistic infall rate of gas to form disks is essential to reproduce the observed radial distributions: the infall rate determines the radial gradients of abundances
5. Similar efficiencies produce similar radial gradients of elemental abundances when measured in normalized radius: the mass of each galaxy does not determine the radial gradient
6. Abundances are local: caution is necessary when global quantities are compared with some other local
7. The radial gradient changes following the spatial range and also with time
8. The evolution with redshift and the comparison with new data will allow to discriminate between galaxy formation scenarios.
9. To be calculated: the spectral energy distributions and the corresponding magnitudes, colors, brightness profiles and spectral absorption stellar indices

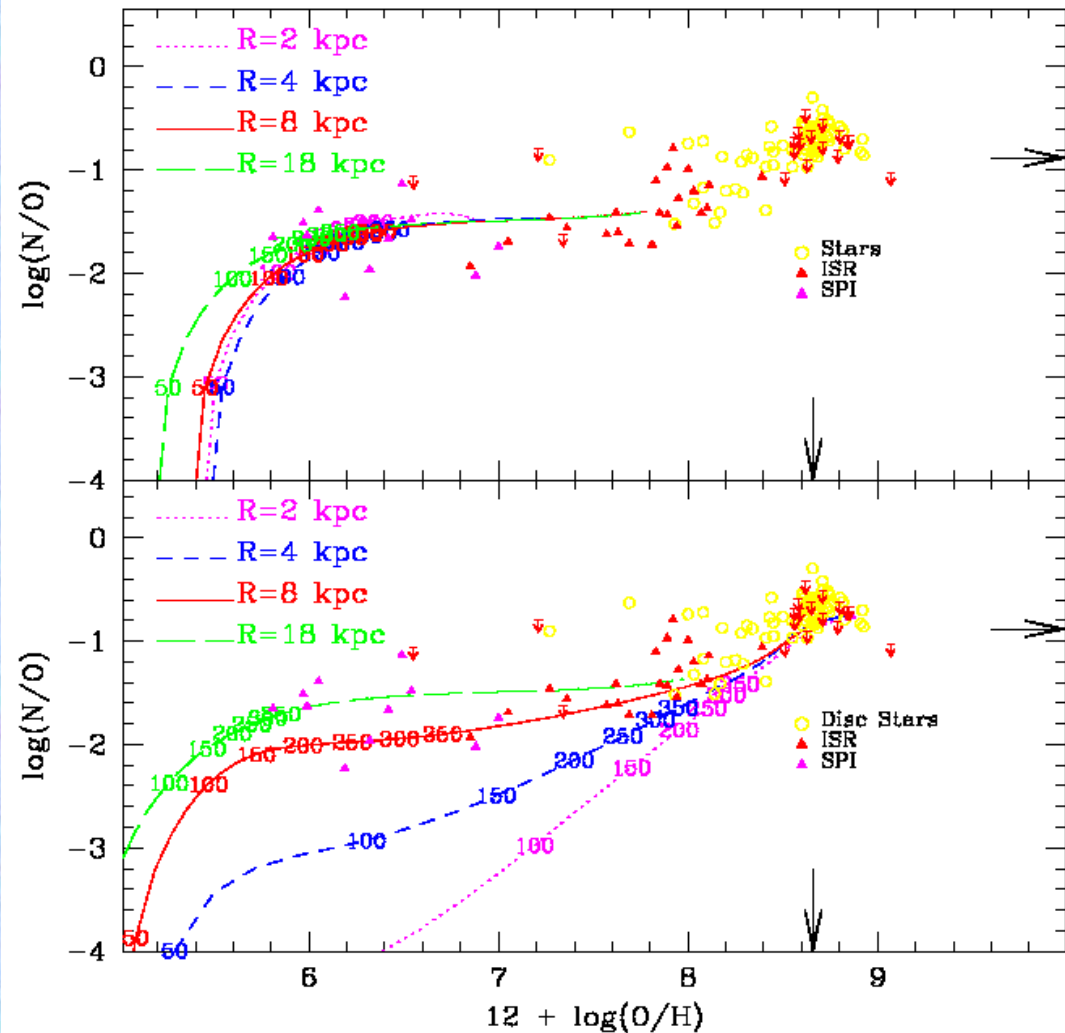


# The N/O vs O/H

In the disk, the most evolved region (magenta line) has an evolutionary track which is different than the one from the outer less evolved disk regions (green line)

A dispersion will appear with different SFR efficiencies

In the halo all tracks are similar with a flat behaviour, falling over data

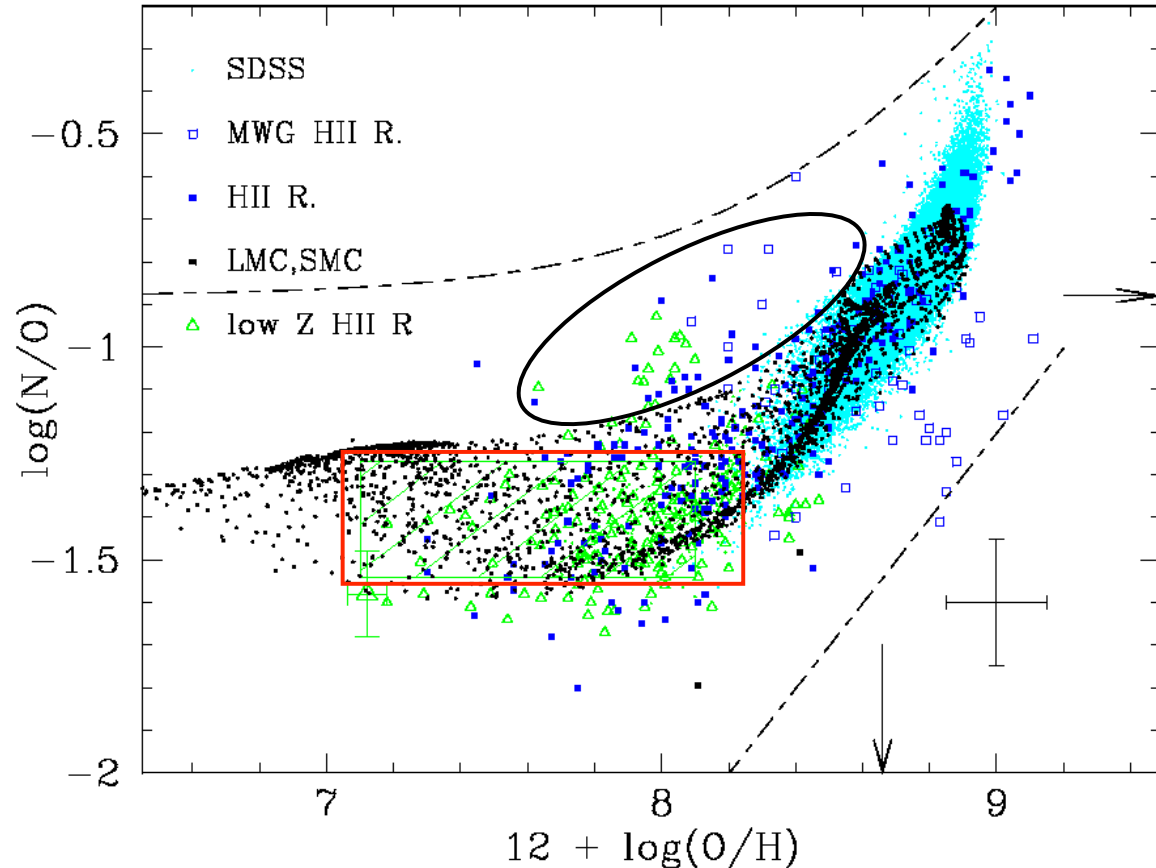




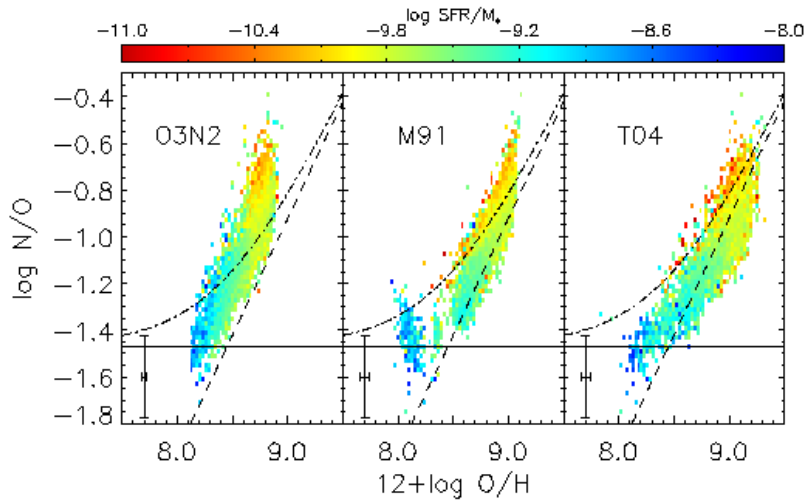
# Nitrogen over Oxygen

Using this grid of models, we have obtained these results in the plane N/O vs O/H for the whole set of models and all computed time steps (Mollá et al. 2006).

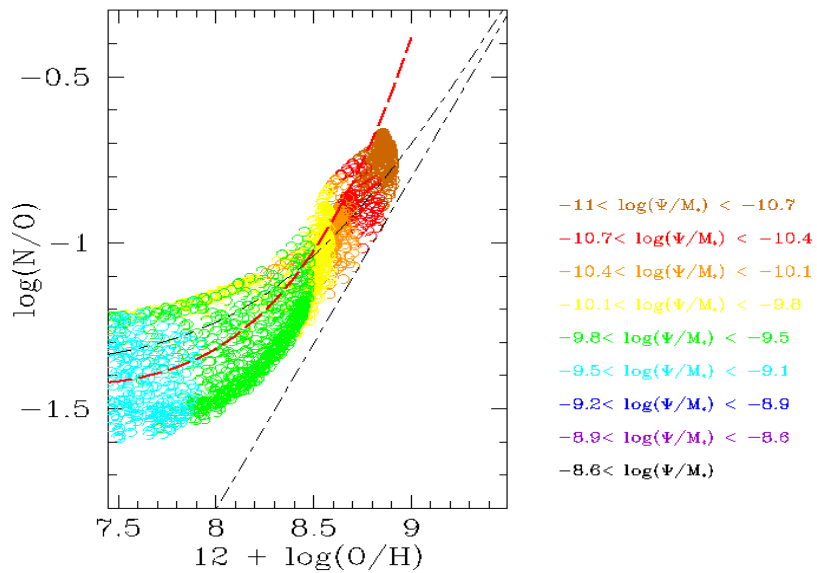
The present day abundances distribution in the plane N/O vs O/H compared with data from Galactic and extragalactic HII regions



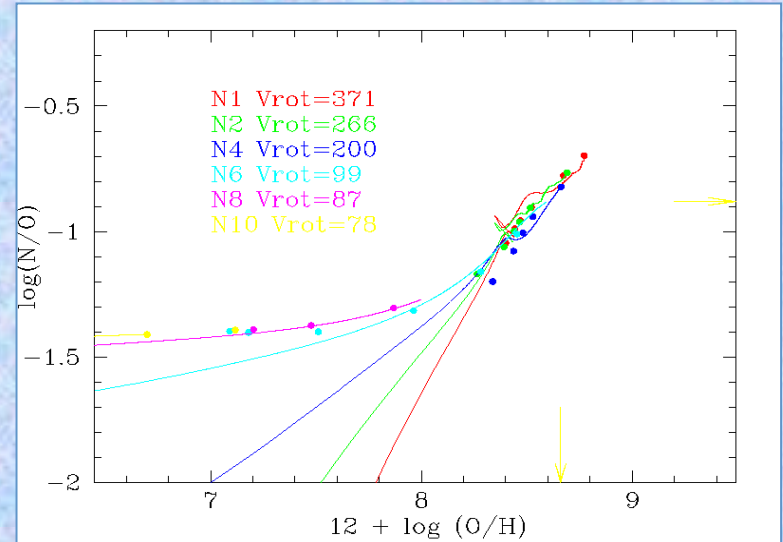
# THE RELATION N/O-SFR-SFH



Galex data (Mallery et al. 2007)

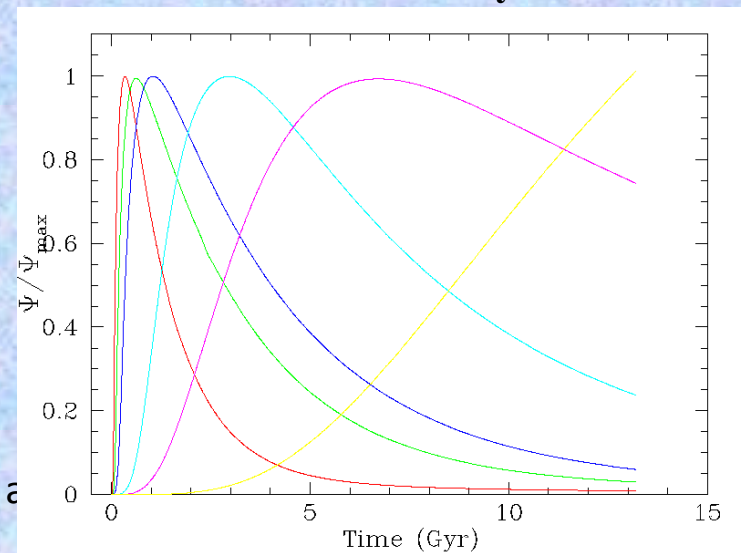


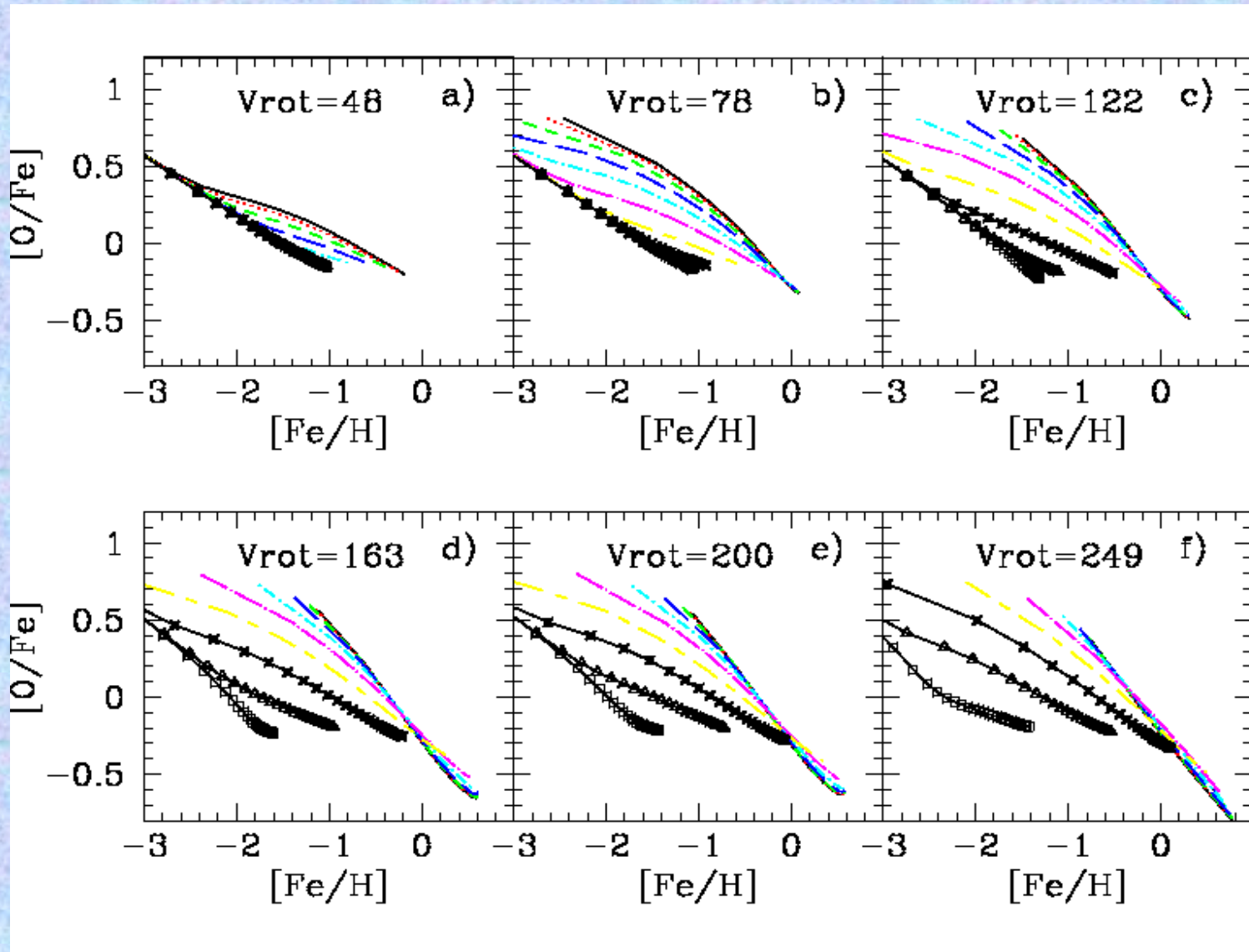
GH14-IFS techniques a



a) Tracks of the lowest mass galaxy with the smallest star formation efficiency.

b) Tracks of the most massive galaxy and the highest star formation efficiency.

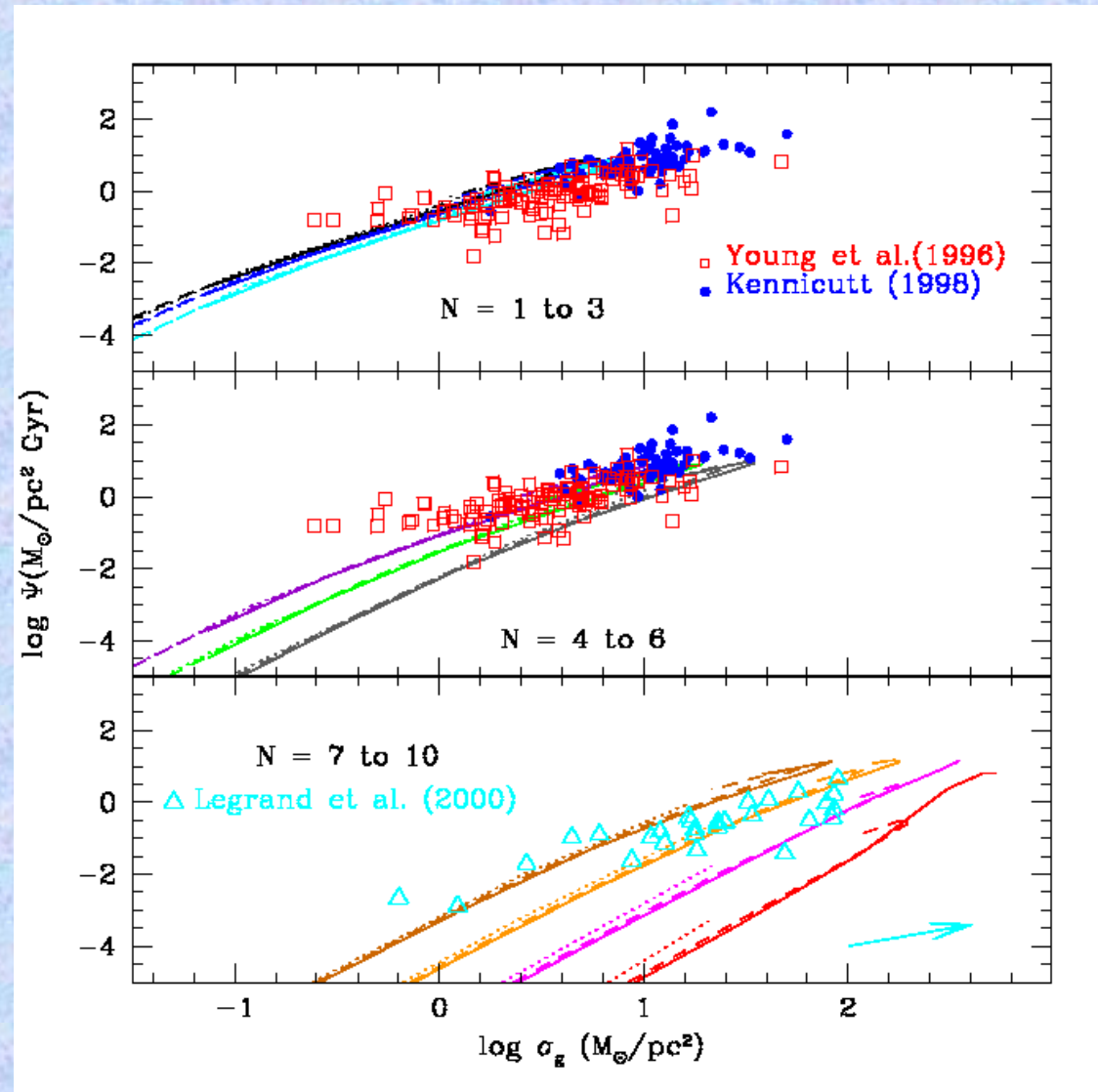






## The star formation rate vs the gas density

The relation simulates a Kennicutt law, with different threshold density for every morphological type galaxy.

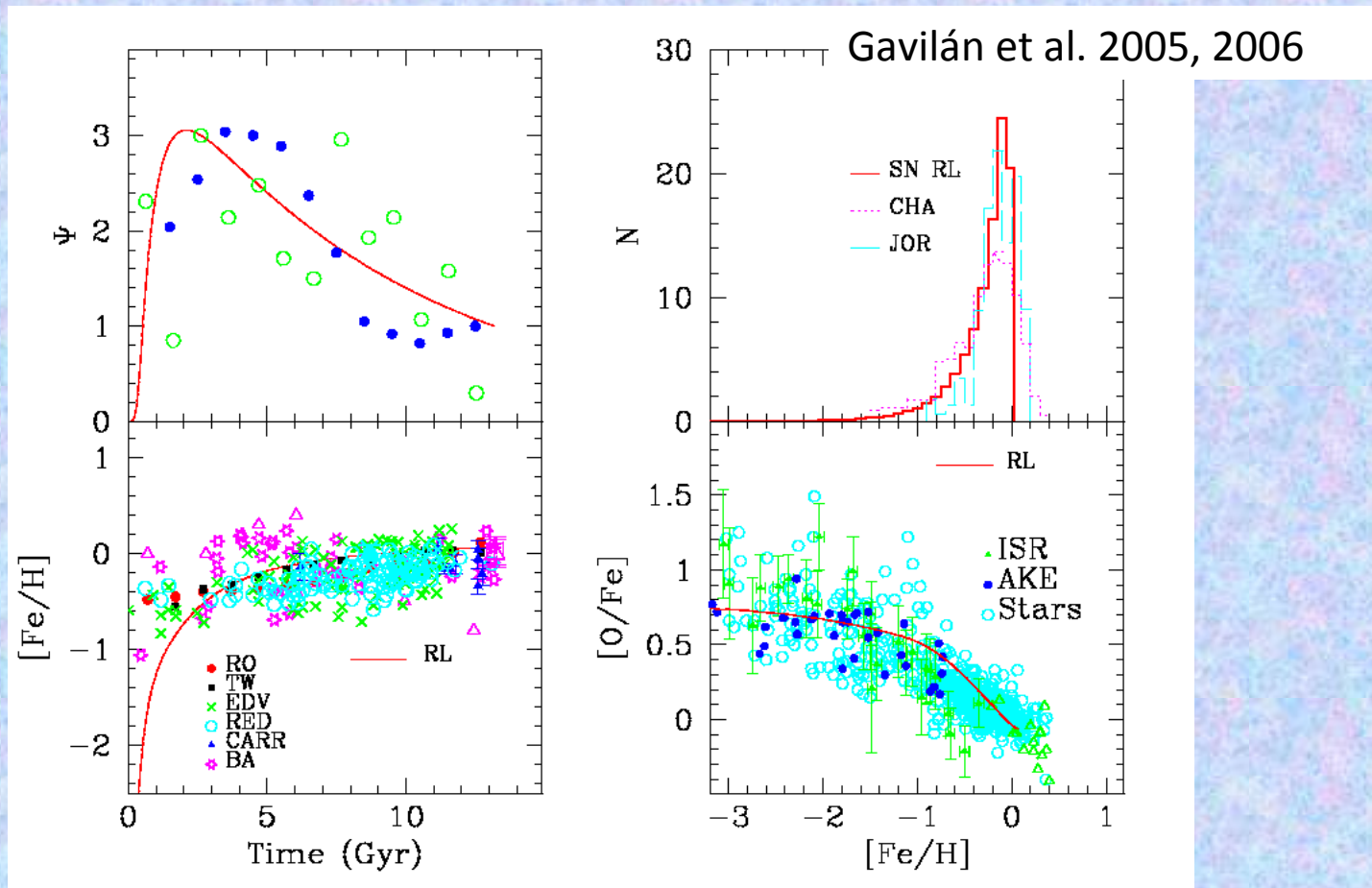


## HOWEVER

- Although the radial gradient of abundances is well reproduced in the models, our results depend on the fitting of gas stars and star formation profiles...
- ..and the molecular gas and the star formation rate show radial distributions decreasing in the inner disk, at variance of observed. They are not well tuned compared with observations
- It seems that we need a slower evolution...

WE NEED BETTER MODELS

## Calibration: the model against the Solar Vicinity data



- The age-metallicity relation and the star formation history for the solar region
- The metallicity distribution does not show the G-dwarf problem



## Our MD05 grid of models

- **Mollá & Díaz (2005):** a grid of chemical evolution models depending on the galaxy total mass and on the efficiency of star formation rate
- **Radial distributions of mass** calculated from the Universal Rotation Curve from Persic, Salucci & Steel (1996)
- **Efficiencies to form molecular gas and stars changed simultaneously:** each  $N$  defined a set  $(\epsilon_M, \epsilon_H)$
- **A by-parametric grid of 44 radial mass distributions**, defined by the rotation velocity, ( $v_{rot}$  30 to 300 km/s) and 10 values of  $N$  ( $\epsilon_M, \epsilon_H$  in the range  $[0,1]$ ), were calculated, with the corresponding radial distributions of abundances, stars and gas densities and star formation rates.
- **Results (radial distributions of gas, abundances, star formation...), and the time evolution of each radial region**, were given as a function of the total mass of the galaxy for different values of efficiencies to form molecular cloud and stars

## SUMMARY OF MODELS GRID

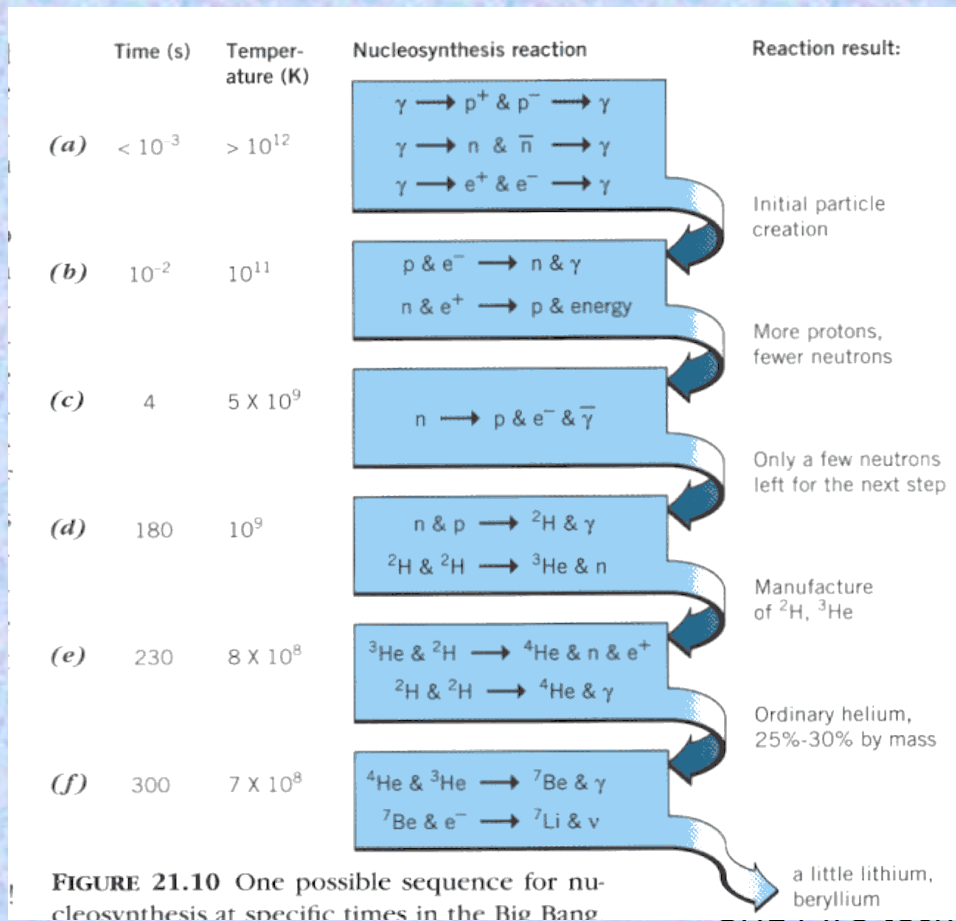
- ❑ We have used the universal rotation curve from Persic, Salucci & Steel (1996) to calculate radial mass distributions  $M(R)$
- ❑ We have computed the collapse time scale for each distribution from the relation  $\tau_{\text{col,gal}} / \tau_{\text{col,MWG}} = (M_{\text{MWG}}/M_{\text{gal}})^{0.5}$
- ❑ We have found analytical expressions for  $\varepsilon_{\mu}(T)$  y  $\varepsilon_h(T)$
- ❑ We compute models for 44 radial mass distributions, and 10 different values of efficiencies ( $\varepsilon_{\mu}$ ,  $\varepsilon_h$ ) between 0 and 1, as it corresponds to their probability meaning, for each one = 440 different models
- ❑ The results of this bi-parametric grid can be applied to any spiral or irregular galaxy of given rotation velocity or total mass in order to estimate its evolution

# Big Bang nucleosynthesis

**Time 0: singularity.**

**Enorme Pressure and Temp: quarks & gluons plasma**

**Large density: the radiation can not travel**



**FIGURE 21.10** One possible sequence for nucleosynthesis at specific times in the Big Bang

**1. Ionized Plasma Exponential expansion. Loss of pressure and temp.**

iques and analysis



# Big Bang nucleosynthesis

**Time 0: singularity.**

**Enorme Pressure and Temp: quarks & gluons plasma**

**Large density: the radiation can not travel**

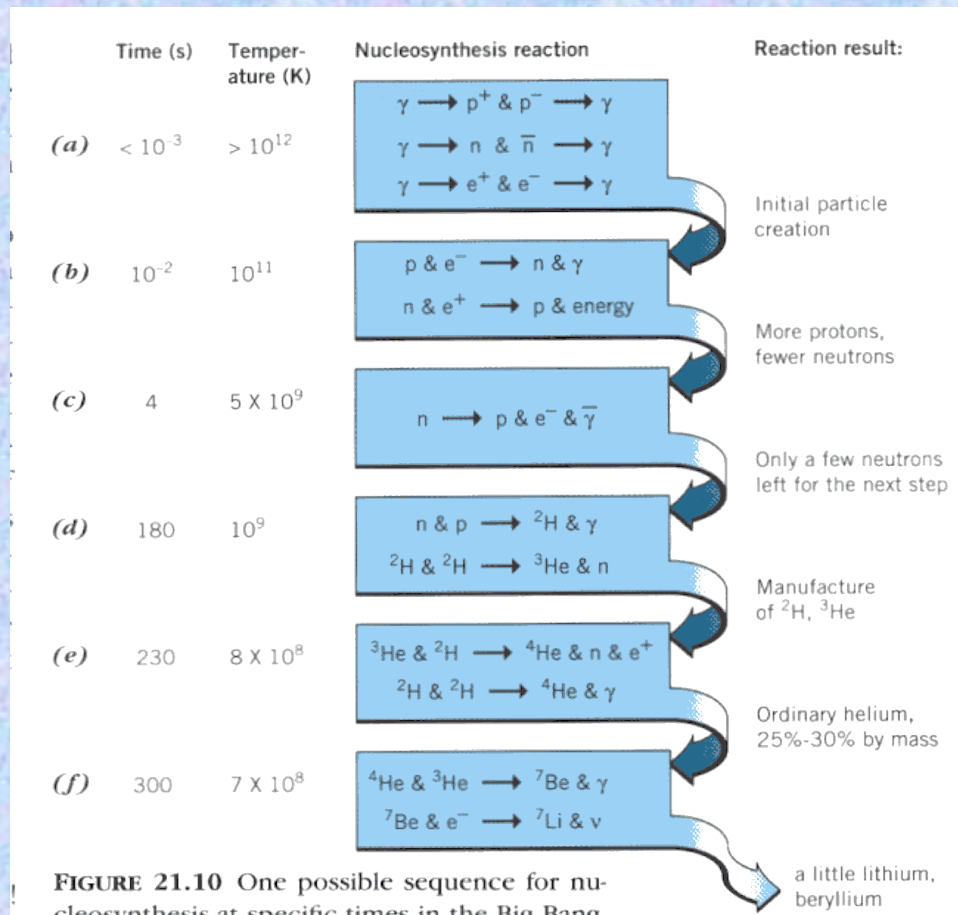


FIGURE 21.10 One possible sequence for nucleosynthesis at specific times in the Big Bang

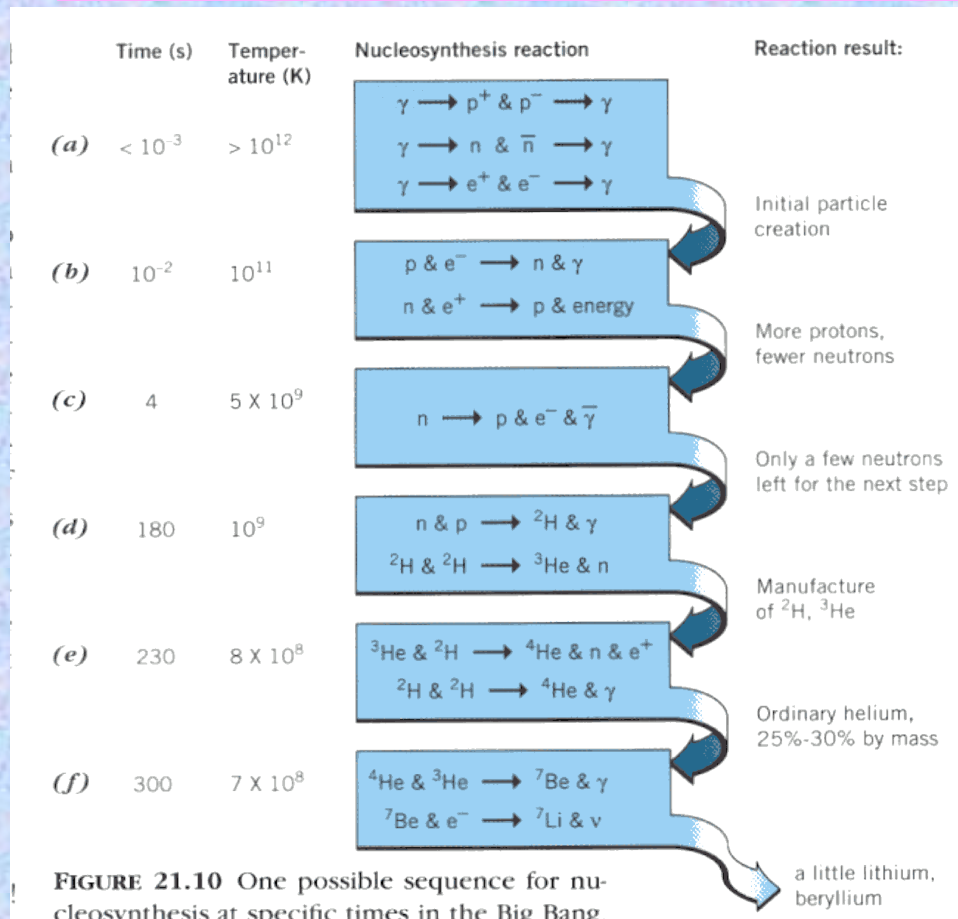
1. Ionized Plasma Exponential
2. Massive particles Barionic matter
3. Light particles: neutrons creation
4. Radiation Era: Photons unable to create more matter. Ratio nucleons
5. Formation of light nuclei (H y D):
6. Nuclear Reactions:  ${}^3\text{He}$  y  ${}^4\text{He}$ , He abundance fixed

# Big Bang nucleosynthesis

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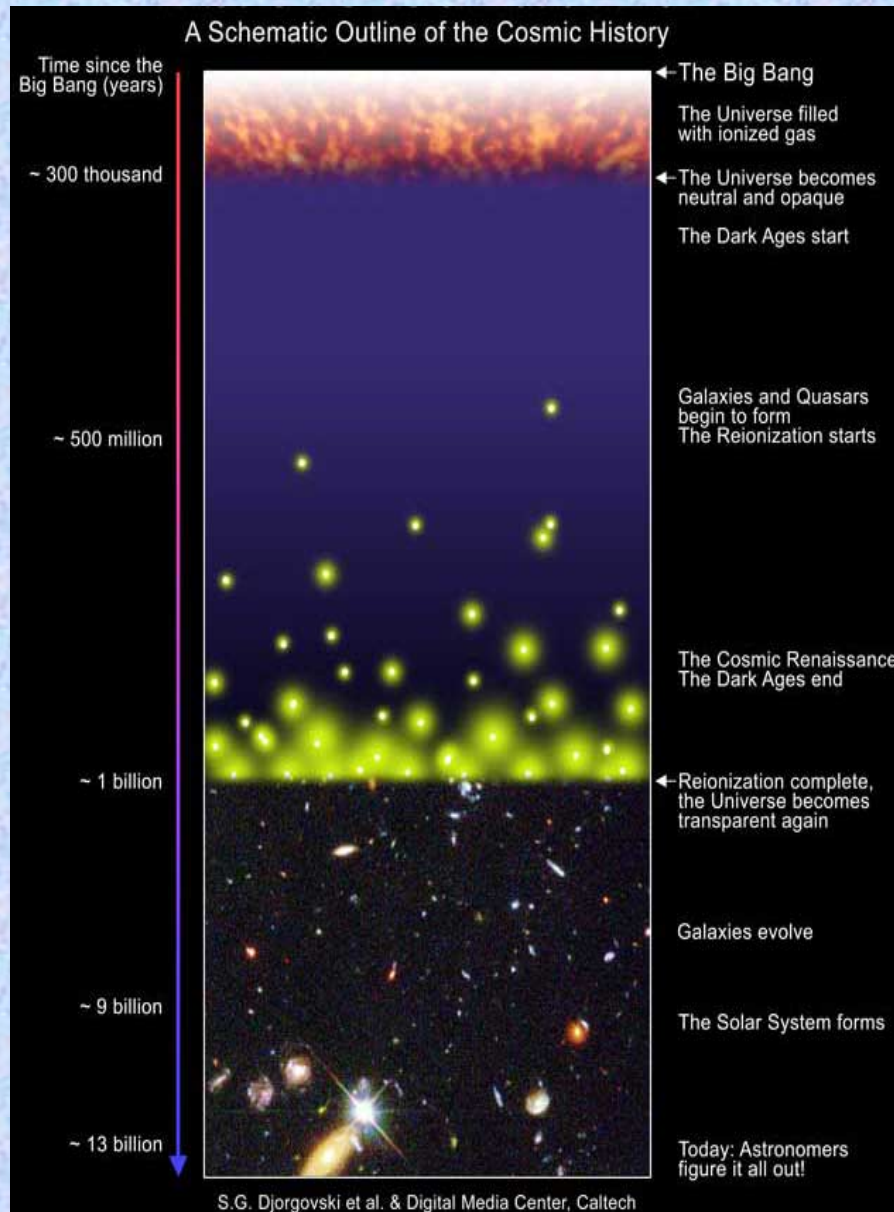
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7. Recombination Era: When  $T < 3000$  K, the process of atoms formation starts

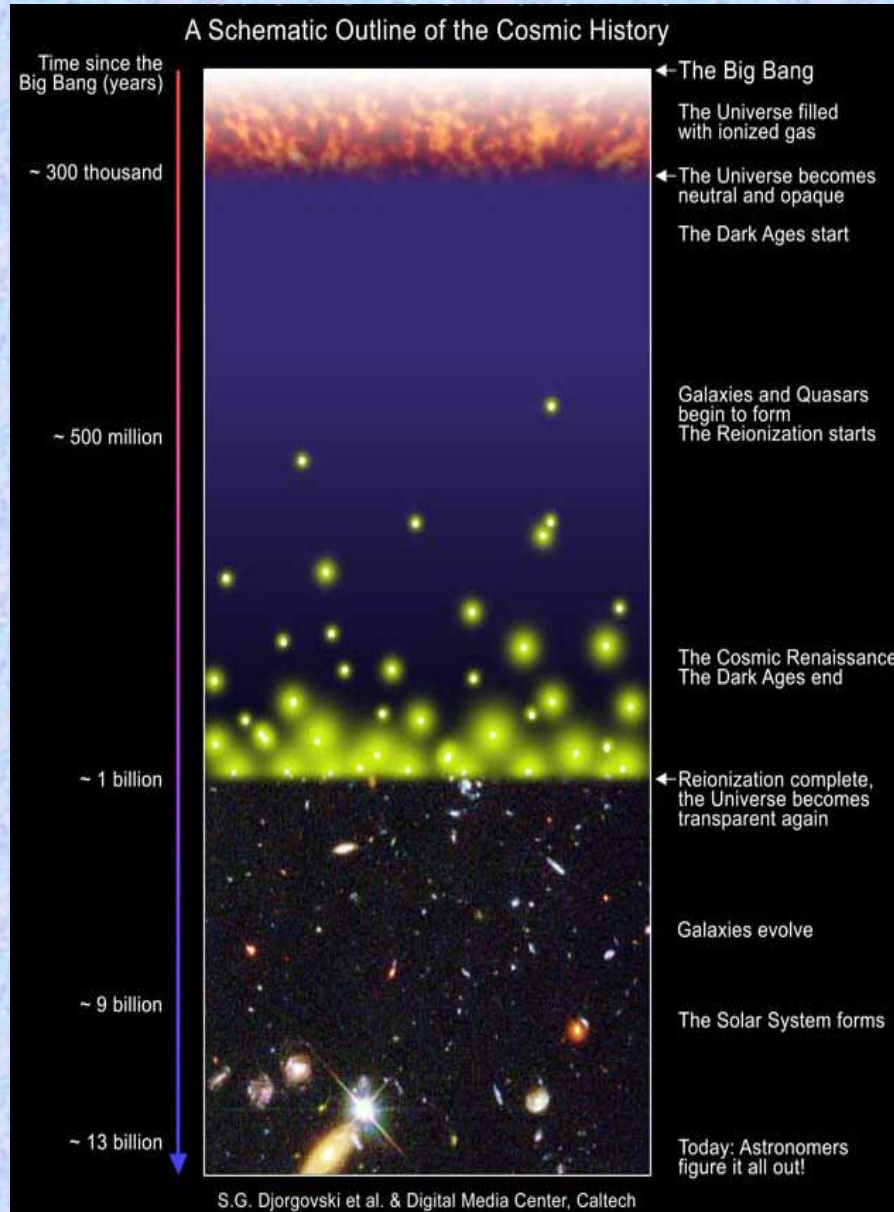
# Evolution of Universe



1. Ionized Plasma Exponential
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7. Recombination Era: When  $T < 3000$  K, the process of atoms formation
8. Radiation and matter Microwave cosmic radiation(2.7 K)

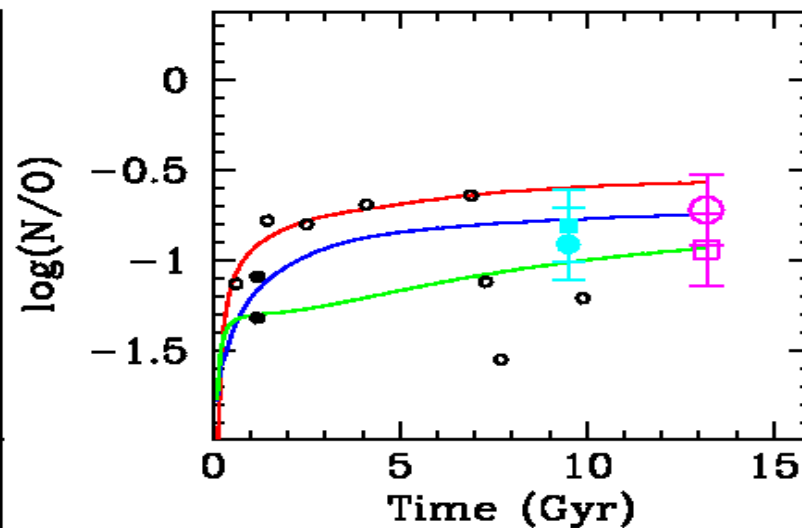
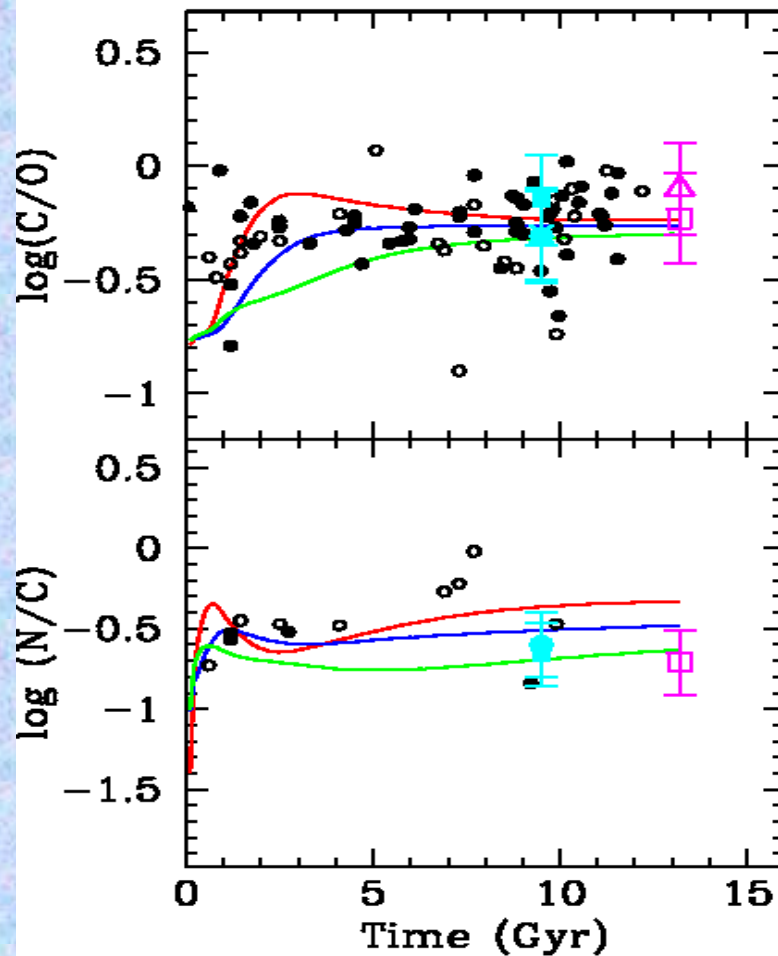


# Evolution of Universe



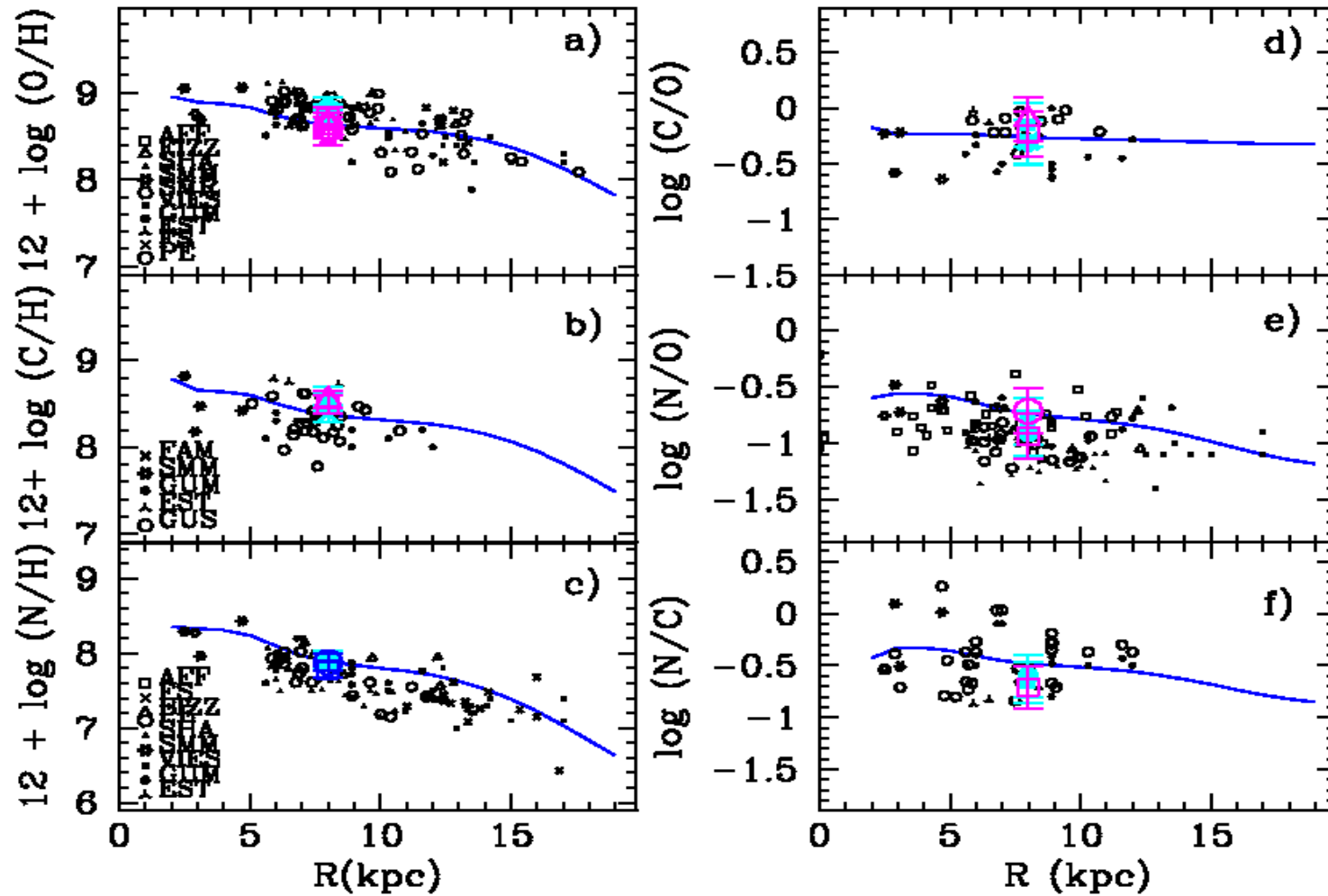
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8. Radiation and matter Microwave
9. Gravitation, Mass accumulation, galaxy formation and star formation

# THE TIME EVOLUTION OF CNO ABUNDANCES



- The elemental abundances reproduce well the observed data for the SN and also for other radial regions.
- The relative CNO abundances also are well fitted

# THE RADIAL GRADIENTS OF CNO ABUNDANCES

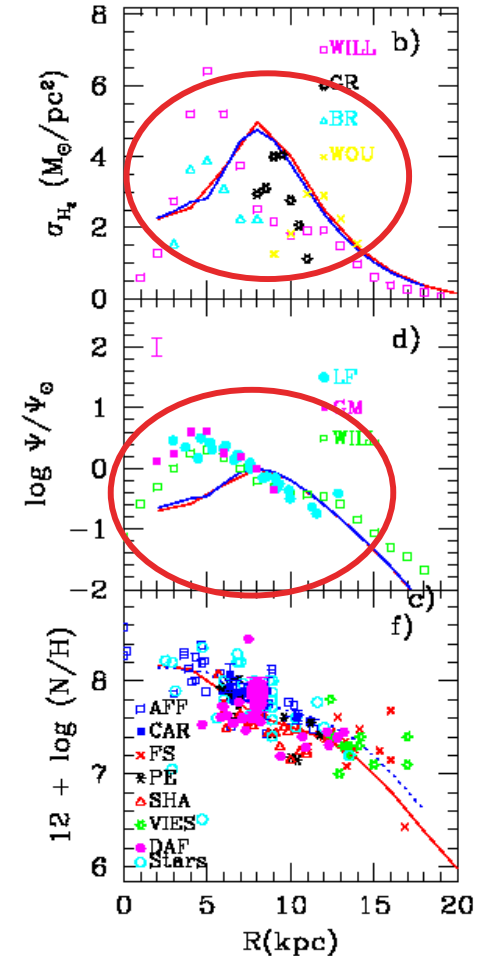
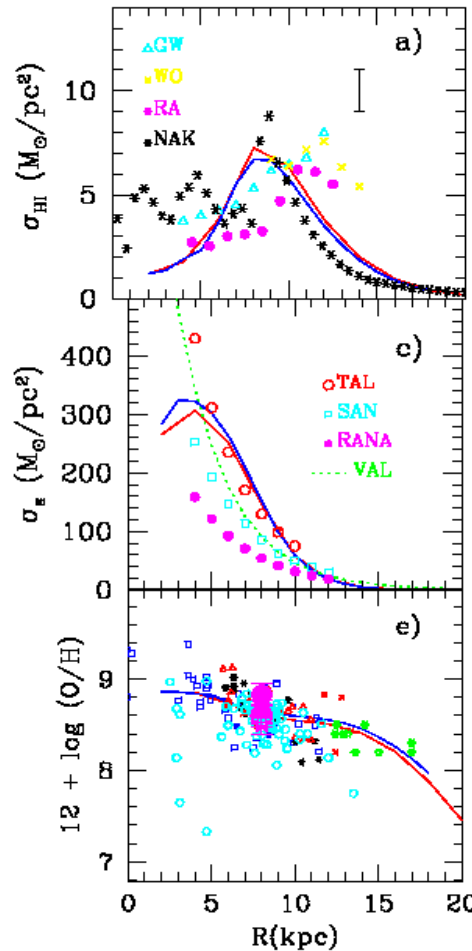




# Calibration: the model for MWG (Gavilán et al. 2005, 2006)

The model:  $V_{rot}=200$  km/s and  $N=4$  against the Galactic disk data and model

- We can obtain separately the radial distributions of diffuse and molecular gas
- The radial gradients flattens in the inner disk in agreement with data (Smartt et al. 2001)
- The star formation rate surface density is underestimated in the inner radii



## III. Calibration.

Results for particular galaxies:

1. Radial distributions for every galaxy in each time step
2. Time evolution for the calculated quantities in each radial region of the galaxies
  - Star formation history
  - Age-metallicity relation

Mollá & Díaz (2005)

