

# Direct measurement of lensing amplification in Abell S1063 using a strongly lensed high redshift HII Galaxy

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## ABSTRACT

ID11 is an actively star forming extremely compact galaxy and Ly $\alpha$  emitter at  $z=3.117$  that is gravitationally magnified by a factor of  $\sim 17$  by the cluster of galaxies Hubble Frontier Fields AS1063. Its observed properties resemble those of low luminosity HII galaxies or Giant HII regions like 30 Doradus in the LMC.

Using the tight correlation between the Balmer-line luminosities and the width of the emission lines (typically  $L(H\beta) - \sigma(H\beta)$ ) valid for HII galaxies and Giant HII regions to estimate its total luminosity, we are able to measure the lensing amplification of ID11. We obtain an amplification of  $23 \pm 11$  similar within errors to the value of  $\sim 17$  estimated or predicted by the best lensing models of the massive cluster Abell S1063.

We also compiled from the literature luminosities and velocity dispersions for a set of lensed compact starforming regions. There is more scatter in the  $L - \sigma$  correlation for these lensed systems but on the whole the results tend to support the lensing models estimates of the magnification.

Our result indicates that the amplification can be independently measured using the  $L - \sigma$  relation in lensed Giant HII regions or HII galaxies. It also supports the suggestion, even if lensing model dependent, that the  $L - \sigma$  relation is valid for low luminosity high- $z$  objects. Ad-hoc observations of lensed starforming systems are required to accurately determine the lensing amplification.

**Key words.** Galaxies: starburst; Galaxies: clusters; Galaxies: lensed

## 1. Introduction

Gravitational lensing is a powerful tool to study the properties of distant low luminosity objects and to estimate the mass profiles of clusters of galaxies. However, as reviewed by Kneib & Natarajan (2011) and discussed by Birrer et al. (2016) each mass mapping method has its own approach that translates into uncertainties in the recovered mass maps. On top of this most if not all methods suffer from mass-sheet degeneracy leading also to non-unique estimates of the total mass of the clusters (see figure 1 of Prieue et al. 2016). To circumvent this, Bertin & Lombardi (2006) and Sonnenfeld et al. (2011) explored possible methods to make *direct* measurements of the magnification. In particular, they proposed using the Fundamental Plane of elliptical galaxies as a standard rod, or the Tully-Fisher relation for spiral galaxies as a standard candle. Unfortunately both methods suffer from important weaknesses that hamper their use at high redshifts, like the uncertainty regarding the possible evolution of

the Fundamental Plane, or the observational challenges of applying the Tully-Fisher relation to high- $z$  spiral galaxies. In fact any distant estimator or standard candle can be used in lensed systems to measure its magnification. Indeed SNIa have already been used to directly measure the cluster magnification (Rodney et al. 2015). HII galaxies have also been used; Fosbury et al. (2003) found inconsistencies between the lensing models and the intrinsic luminosity predicted by the Melnick et al. (2000)  $L - \sigma$  correlation for two massive star forming regions in the “Lynx arc”.

Recently Caminha et al. (2015) reported the discovery of multiple images of a strong lensed star forming galaxy at  $z=3.117$  located behind the Hubble Frontier Fields1 cluster Abell S1063 (AS1063). This galaxy named ID11 is one of the lowest luminosity Ly  $\alpha$  blobs found to date.

In a recent paper Vanzella et al. (2016) reported new high quality observations of ID11. Spectroscopy with MUSE and X-SHOOTER on the VLT indicates that ID11 is a compact ( $R_{eff} \simeq 67$  pc), young (age  $< 20$  Myr), low mass ( $M < 10^7 M_{\odot}$ ) and dust-

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free galaxy, thus strongly resembling low redshift HII galaxies or Giant HII regions like 30 Doradus in the LMC (Terlevich & Melnick 1981; Terlevich et al. 1991).

A key property of HII galaxies and Giant HII regions is that they follow a tight correlation between the widths of their emission lines, and their Balmer-line (typically  $H\beta$ ) luminosities, the  $L-\sigma$  correlation as shown in Figure 1 (see Chávez et al. 2014, for a detailed discussion and list of references). Having shown that the  $L-\sigma$  correlation provides a powerful cosmological probe, we have engaged on a programme to measure the emission line widths and luminosities of a large sample of HII galaxies out to redshifts of  $z \sim 3$  using multi-object IR spectrographs on the VLT and Keck telescopes (see Terlevich et al. 2015).

As the  $L-\sigma$  correlation is valid up to redshifts of at least  $z \sim 2.5$  (Melnick et al. 2000; Siegel et al. 2005; Terlevich et al. 2015), and prompted by Vanzella et al. (2016) results on ID11, we decided to use the  $L-\sigma$  relation to measure directly the lensing amplification in Abell S1063 and simultaneously check its validity for low luminosity high- $z$  starforming regions.

## 2. Results

The measurements for the relevant lines from Vanzella et al. (2016) are reproduced in Table 1, where the line widths have already been corrected for instrumental broadening. The fluxes obtained combining two of the lensed images of the galaxy have not been corrected for internal reddening, but the authors indicate that the extinction in this object is negligible. They do not quote observational errors, but judging by the S/N, the error in the  $H\beta$  flux is of the order of 25%. The errors in the [OIII] line widths are of the order of 2-3  $km s^{-1}$  and much larger for the weaker  $H\beta$ . Therefore we use the [OIII] line width for this exercise.

In order to apply the  $L-\sigma$  relation we need to correct the line-widths for thermal broadening. This correction is in general quite small for oxygen, but the detection of HeII  $\lambda 1640 \text{ \AA}$  in emission in ID11 indicates that the ionized gas must be extremely hot. In fact Vanzella et al. (2016) reported a metallicity of  $12+\log(O/H) < 7.8$  and an electron temperature of  $T_e = 26500 \pm 2600 \text{ K}$  from the [OIII]  $\lambda 1666 \text{ \AA}$ /[OIII]  $\lambda 5007 \text{ \AA}$  ratio. Although this value of the electron temperature is on the high side compared to that of most low metallicity HII regions, we have used it to compute the thermal broadening of the oxygen lines as  $\sigma_{th} = 3.5 \text{ km s}^{-1}$ .

The velocity dispersion of ID11, obtained from the weighted average of the two [OIII] lines is  $FWHM = 51.4 \text{ km s}^{-1} \pm 2.0 \text{ km s}^{-1}$ , and corrected for thermal broadening is

$$\sigma_{[OIII]} = \sqrt{(51.4/2.355)^2 - 3.5^2} = 21.5 \pm 0.9 \text{ km s}^{-1} \quad (1)$$

which for the present purposes is not significantly different from the observed value of  $21.8 \text{ km s}^{-1}$ .

For giant HII regions and HII galaxies the Balmer lines are observed to be systematically broader than [OIII] by about  $1.4 \text{ km s}^{-1}$  (Hippelein 1986), so a correction must be included before using the  $L-\sigma$  relation of Chávez et al. (2014) that is defined for  $H\beta$ . Thus, for ID11 we estimate that the velocity dispersion of the Balmer lines is:  $\sigma_{H\beta} = 23.0 \text{ km s}^{-1}$

The  $L-\sigma$  relation as calibrated in Chávez et al. (2012) using 92 Giant HII regions and HII galaxies is

$$\log L(H\beta) = 4.97 \pm 0.10 \times \log(\sigma_{H\beta}) + 33.25 \pm 0.15 \text{ erg s}^{-1} \quad (2)$$

**Table 1. Observations of ID11 from Vanzella et al. (2016)**

Line	Flux ( $10^{-17} \text{ erg s}^{-1} \text{ cm}^{-2}$ )	S/N	FWHM (km/s)	EW ( $\text{\AA}$ )
$H\beta$	0.31	4	—	110
[OIII]4959	0.90	12	54	340
[OIII]5007	2.35	33	51	860

which for  $\sigma_{H\beta} = 23 \text{ km s}^{-1}$  predicts  $\log L(H\beta)_{pred} = 40.02 \pm 0.22 \text{ erg s}^{-1}$ ; the error has been computed as:

$$\epsilon_{\log(LumH\beta)} = \sqrt{(\log\sigma)^2 \times \epsilon_a^2 + a^2 \times \epsilon_{\log\sigma} + \epsilon_b^2} \quad (3)$$

where  $a$  is the slope and  $b$  the intercept of the  $L-\sigma$  relation and  $\epsilon_a$ ,  $\epsilon_b$  and  $\epsilon_{\log\sigma}$  are the errors in the slope, the intercept and the velocity dispersion respectively.

The more recent calibration of the  $L-\sigma$  relation by Terlevich et al. (2015) with a larger sample of HII galaxies including high redshift ones with redshifts between 0.6 and 2.33 is,

$$\log L(H\beta) = 5.055 \pm 0.097 \times \log(\sigma_{H\beta}) + 33.11 \pm 0.145 \text{ erg s}^{-1} \quad (4)$$

in this case we obtain  $\log L(H\beta)_{pred} = 39.99 \pm 0.21 \text{ erg s}^{-1}$ , again propagating the errors with equation (3).

The observed  $H\beta$  flux of ID11 from Table 1 is  $F(H\beta) = 3.1 \times 10^{-18} \text{ erg s}^{-1} \text{ cm}^{-2}$  (assuming negligible extinction as reported by Vanzella et al. 2016). At a redshift of  $z = 3.117$  and for the cosmology adopted in Chávez et al. (2014) ( $H_0 = 74.3$ ;  $\Omega_m = 0.3$ ;  $\Omega_0 = 1$ ), this flux corresponds to a photometric luminosity of  $L(H\beta)_{obs} = 41.37 \text{ erg s}^{-1}$ . Thus, the measured amplification is, from equation (2)

$$\mu = 10^{(41.37 \pm 0.1 - 40.02 \pm 0.22)} = 22 \pm 11 \quad (5)$$

or, from equation (4)

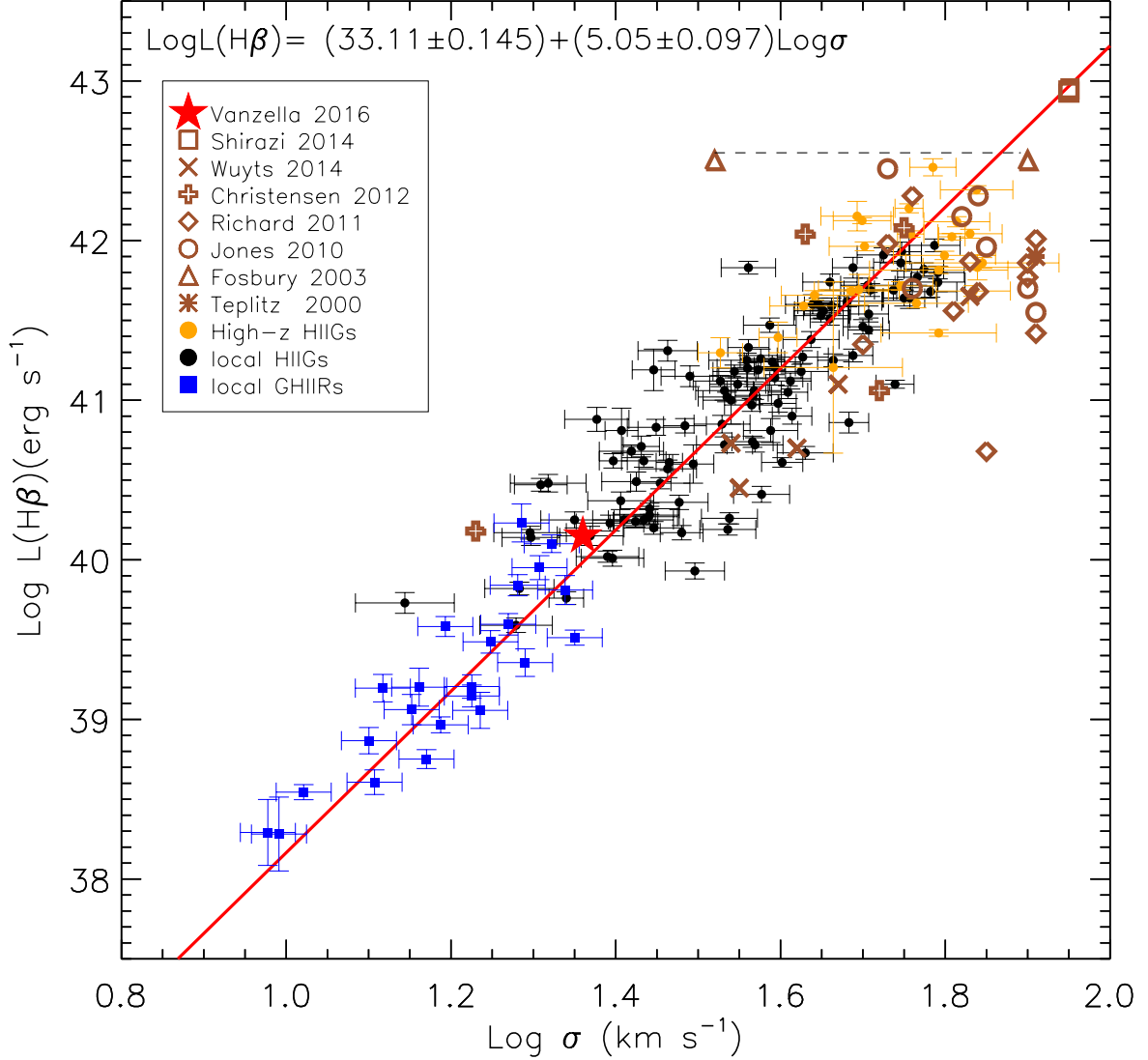
$$\mu = 10^{(41.37 \pm 0.1 - 39.99 \pm 0.21)} = 24 \pm 12 \quad (6)$$

in remarkable agreement with the magnification of  $\mu \sim 17$  reported by Vanzella et al. (2016) from the cluster lensing models of Caminha et al. (2015).

We have assumed a photometric error of 0.1 dex in the observed  $H\beta$  flux, but the uncertainty in our predicted luminosity stems basically from the dispersion of the  $L-\sigma$  relation, so it is unlikely that more and better data will yield a more stringent test of the lensing model with just one lensed HII galaxy.

The fact that the model demagnified luminosity ( $\log L(H\beta) = 40.15$ ) agrees so well with the value expected from the  $L-\sigma$  relation from the observed ionized gas velocity dispersion ( $\log L(H\beta) = 40.02$ ), provides strong confirmation that ID11 is either a bona-fide HII galaxy or a Giant HII region. This can be seen in Figure 1, where we reproduce the  $L-\sigma$  correlation from Terlevich et al. (2015) including nearby and high redshift HII galaxies as well as Giant HII regions in nearby galaxies with accurate distances determined with Cepheids.

ID11 (shown by the red star) lies in the transition region between giant HII regions and HII galaxies. Given that the deep HST images of ID11 of Vanzella et al. (2016) reveal no indication of an underlying galaxy, we concur with them in classifying ID11 as a low-luminosity HII galaxy at  $z = 3.117$ .



**Fig. 1.** the  $L-\sigma$  relation for HII Galaxies and Giant HII regions. Orange dots are HII galaxies with redshifts between 0.6 and 2.4. ID11 is represented by the red star near the centre of the plot at  $\sigma_{[H\beta]} = 23.0 \text{ km s}^{-1}$  and at the observed luminosity de-amplified by 0.06  $L(H\beta)_{obs} = 40.15 \text{ erg s}^{-1}$ . ID11 lies in a region of the diagram that is populated by low luminosity HII galaxies and luminous Giant HII regions. The open brown triangles joined by a dashed line are Fosbury's Lynx Arc data, with  $\sigma$  determined from the semi-forbidden lines and from CIV (see text). Other lensed systems are plotted with a variety of symbols as listed in the inset. The brown cross near ID11 corresponds to A4.1. The brown line at the top is the fit to 131 HII Galaxies and Giant HII regions from Terlevich et al. (2015) shown by the red solid line.

### 3. Discussion

As mentioned in the introduction, this is not the first time the  $L-\sigma$  relation is used in this context. Fosbury et al. (2003) found inconsistencies between the lensing models and the intrinsic luminosity predicted by the Melnick et al. (2000)  $L-\sigma$  correlation on two compact and luminous star forming regions in the ‘‘Lynx arc’’. Fosbury et al. (2003) used the line profiles of two UV semi-forbidden lines,  $OIII\lambda 1666\text{\AA}$  and the  $CIII\lambda\lambda 1907, 1909\text{\AA}$  doublet that gave values of the instrumental corrected velocity dispersions of 35 and  $30 \text{ km s}^{-1}$  respectively. They also reported model corrected velocity dispersions of the absorption

affected  $Ly\alpha \lambda 1216\text{\AA}$  and  $CIV\lambda 1550\text{\AA}$  permitted lines of 150 and  $80 \text{ km s}^{-1}$  respectively. In many starforming galaxies,  $Ly\alpha$  is clearly asymmetric, a fact that renders its use for determining the line profile and hence velocity dispersions, very uncertain. The issue has been discussed extensively (and models constructed to reproduce it) in our own old work on  $Ly\alpha$  emission (e.g. Kunth et al. 1998; Tenorio-Tagle et al. 1999; Mas-Hesse et al. 2003, etc.) and for high redshift objects (Pettini et al. 2000; Rhoads et al. 2000, among others). On the other hand while CIV  $\lambda 1550\text{\AA}$  is also a resonance line, resonance scattering and collisional de-excitation should affect it less than in the case of  $Ly\alpha$ ,

because carbon is far less abundant than hydrogen and therefore has smaller optical depths – even more so in low metallicity systems.

To investigate further this issue we compiled from the literature luminosities and velocity dispersions for a set of lensed compact starforming regions. The sample is listed in Table 2. The lensed systems are also shown in Figure 1.

While ID11 and notably also A4.1 fall in the transition region between HII galaxies and giant HII regions the rest of the lensed systems are among the most luminous starforming systems and occupy a region of the diagram corresponding to the most luminous HII galaxies. The “Lynx arc” result from Fosbury et al. (2003) is shown with two different values of the velocity dispersion, the lower value corresponding to the semi-forbidden lines and the higher value corresponding to the fit to the permitted CIV  $\lambda$  1550Å line. There is more scatter in the lensed systems but on the whole the results tend to support the lensing models estimates of the magnification apart from the “Lynx arc” result when using the semi-forbidden lines.

There is a crucial general point that we need to make regarding this exercise:

The luminosity in these young bursts of star formation evolves quickly in time scales of few megayears moving their position away from the  $L$ – $\sigma$  correlation to lower luminosities and smaller equivalent widths (EW) of H $\beta$  or H $\alpha$  (Melnick et al. 2000; Bordalo & Telles 2011). This fact may be related to the scatter of the Richard et al. (2011) points below the  $L$ – $\sigma$  relation (Figure 1). To obtain and publish the EW of H $\beta$  or H $\alpha$  of star forming systems is therefore highly recommended in order to allow for an evolution correction to be performed.

## 4. Conclusions

Regarding the intrinsic properties of ID11, Figure 1 implies that it is either a luminous Giant HII region like 30 Doradus in the LMC or those found in spiral galaxies like M101, or a low luminosity HII galaxy. Given that the deep HST images of ID11 show no indication of an underlying galaxy, we confirm Vanzella et al. (2016) conclusion that ID11 is a low-luminosity HII galaxy at  $z=3.117$ .

The  $L$ – $\sigma$  relation spans more than three orders of magnitude in luminosity, which allows us to observe a significant number of objects at large redshifts without recourse to gravitational telescopes, hence the power of the relation as a cosmological probe (Plionis et al. 2011; Terlevich et al. 2015; Chávez et al. 2016). But, of course, only the most luminous HII galaxies can be observed at higher redshifts with the current generation of 8-10m telescopes, so gravitationally amplified objects such as ID11 provide us with the unique chance to verify that at high redshift the correlation holds also for low luminosity and possibly low metallicity HII galaxies.

Using an independent method based on the standard candle provided by the  $L$ – $\sigma$  relation valid for HII galaxies and Giant HII regions, we have **measured** the amplification affecting the star forming system ID11 by the Abell cluster S0163 as  $23 \pm 11$  coinciding with the value of  $\sim 17$  obtained by Vanzella et al. (2016) from the strong lensing model of Caminha et al. (2015).

Our result suggests that we can use Giant HII regions in high- $z$  lensed galaxies as instruments for studying gravitational lenses and that the combination of the  $L$ – $\sigma$  standard candle plus detailed lensing models can provide a practical method to break the mass-sheet degeneracy in the estimates of the total mass of clusters of galaxies.

High spectral resolution *ad-hoc* observations of H $\alpha$ , H $\beta$  and [OIII] to determine the velocity dispersion and low resolution, large aperture to determine their fluxes and EW, are needed to be able to apply this method to a larger sample of lensed starforming galaxies, but this is beyond the scope of this Letter.

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**Table 2. Parameters for lensed compact regions of star formation compiled from the literature**

Name	$\log L(H\beta)$ $erg\ s^{-1}$	$\log \sigma$ $km\ s^{-1}$	$\mu$	REFERENCES
ID11	40.15	1.36	16.7	Vanzella et al. (2016)
CI0024 *	42.28	1.84	1.4	Jones et al. (2010) (1)
MACSJ0451	41.70	1.90	49.	Jones et al. (2010) (1)
MACSJ0712	41.55	1.91	28.	Jones et al. (2010) (1)
CI0949 *	42.15	1.82	7.3	Jones et al. (2010) (1)
CI0949(NE)	41.96	1.85	7.3	Jones et al. (2010) (1)
CI0949(SW)	41.70	1.76	7.3	Jones et al. (2010) (1)
MACSJ2135	42.45	1.73	28.	Jones et al. (2010) (1)
A4.1	40.18	1.23	23.0	Christensen et al. (2012) (2)
M0304	42.08	1.75	42.0	Christensen et al. (2012) (2)
M0359	41.06	1.72	18.0	Christensen et al. (2012) (2)
M2031	42.04	1.63	4.2	Christensen et al. (2012) (2)
RCSGA032727b	40.73	1.54	—	Wuyts et al. (2014) (3)
RCSGA032727d	40.70	1.62	—	Wuyts et al. (2014) (3)
RCSGA032727e	41.10	1.67	—	Wuyts et al. (2014) (3)
RCSGA032727f	40.45	1.55	—	Wuyts et al. (2014) (3)
RCSGA032727g	41.65	1.83	—	Wuyts et al. (2014) (3)
MS1512-cB58	41.90	1.91	30.0	Teplitz et al. (2000)
RXJ0848	42.50	1.52	10.	Fosbury et al. (2003) (4)
RXJ0848	42.50	1.90	10.	Fosbury et al. (2003) (5)
A68-C1	40.68	1.85	2.52	Richard et al. (2011) (6)
CEYE	41.98	1.73	3.69	Richard et al. (2011) (6)
MACS0744	41.77	1.90	3.01	Richard et al. (2011) (6)
CI0024 *	41.68	1.84	1.38	Richard et al. (2011) (6)
MACS0451	41.86	1.90	4.22	Richard et al. (2011) (6)
RXJ1053	41.87	1.83	4.03	Richard et al. (2011) (6)
A2218-Flank.	41.35	1.91	3.60	Richard et al. (2011) (6)
CI0949 *	41.42	1.91	2.16	Richard et al. (2011) (6)
A773	41.56	1.81	2.69	Richard et al. (2011) (6,7)
A2218-Mult	42.28	1.76	3.39	Richard et al. (2011) (6)
A2218-Smm	42.01	1.91	3.01	Richard et al. (2011) (6)
8OCLOCKA2	42.95	1.95	6.3	Shirazi et al. (2014)
8OCLOCKA3	42.93	1.95	4.9	Shirazi et al. (2014)

NOTE. - Names are those listed in the corresponding reference.  $\mu$  is the published magnification. Luminosities recalculated from the observed fluxes for a flat universe with:  $H_0 = 74.3\ km\ s^{-1}\ Mpc^{-1}$  ;  $\Omega_M = 0.70$

(\*) Object appears in more than one paper.

(1) Velocity dispersion from either  $H\alpha$  or  $[OIII]\lambda 5007\text{\AA}$  .

(2) Velocity dispersion is the weighted average of all lines from UV to optical excluding only  $Ly\alpha$ .

(3) Provides de-lensed luminosities but do not list the magnifications.

(4) Velocity dispersion from  $[OIII]\lambda 1666\text{\AA}$  and  $CIII]\lambda 1907, 1909\text{\AA}$  .

(5) Velocity dispersion from  $CIV\lambda 1550\text{\AA}$  .

(6) Velocity dispersion from either  $[OII]\lambda 3727\text{\AA}$ ,  $H\alpha$  or  $[OIII]\lambda 5007\text{\AA}$ ; undefined.

(7) Used  $H\beta$  flux.